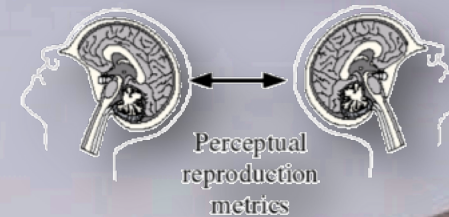


Human color encoding and image system engineering

- Types of photoreceptors
- Photoreceptors spatial arrangement
- Color-matching experiment



Color vision is interesting: Blue Man Group

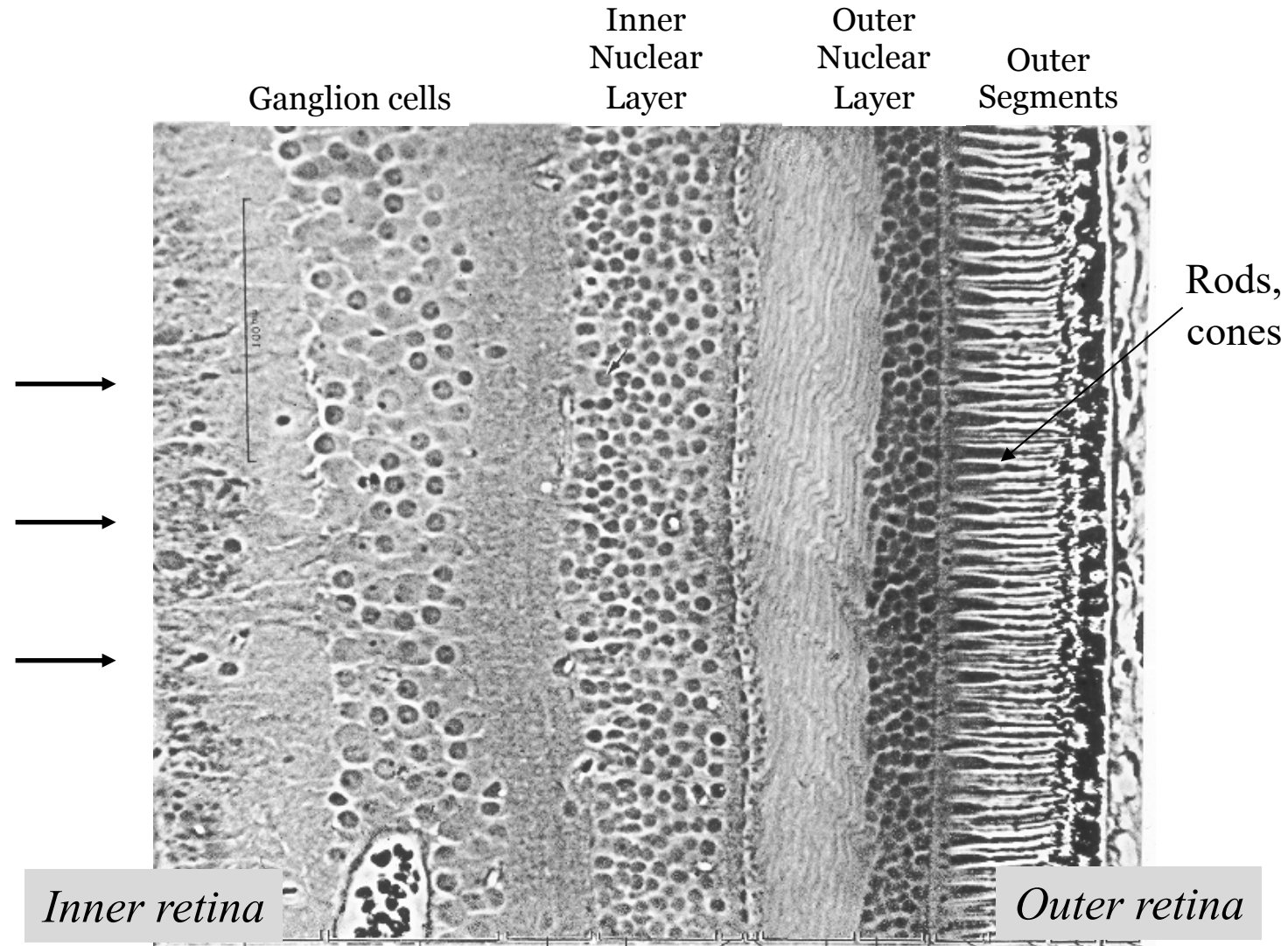
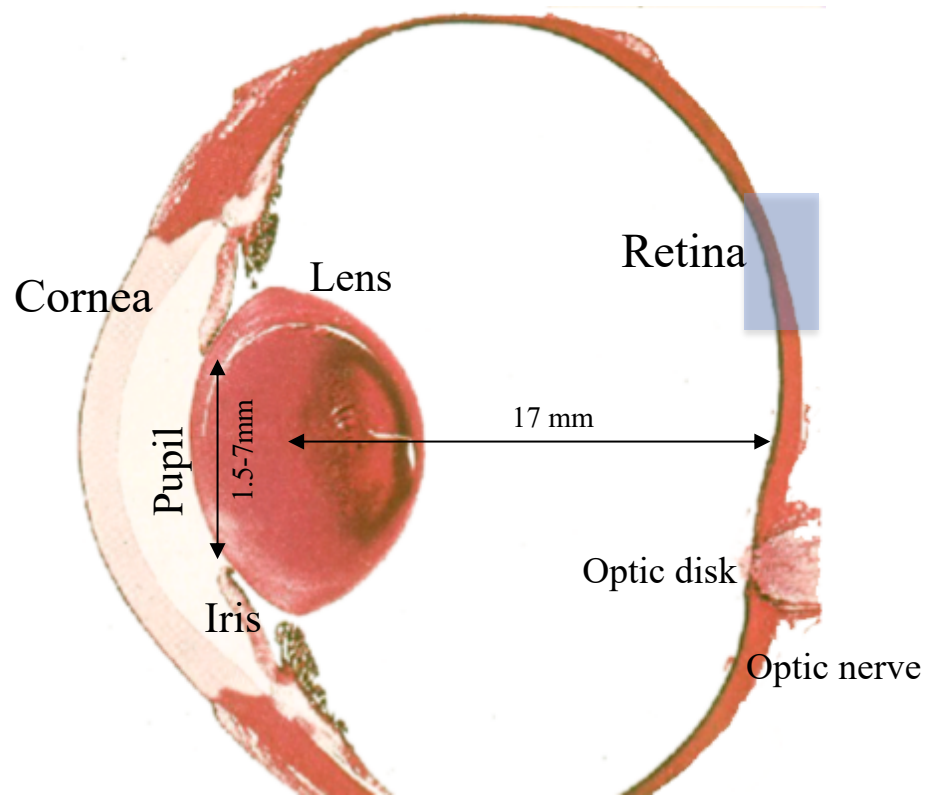
Oct. 2016: 2,614,430 views

sHc&feature=youtube_gdata_player

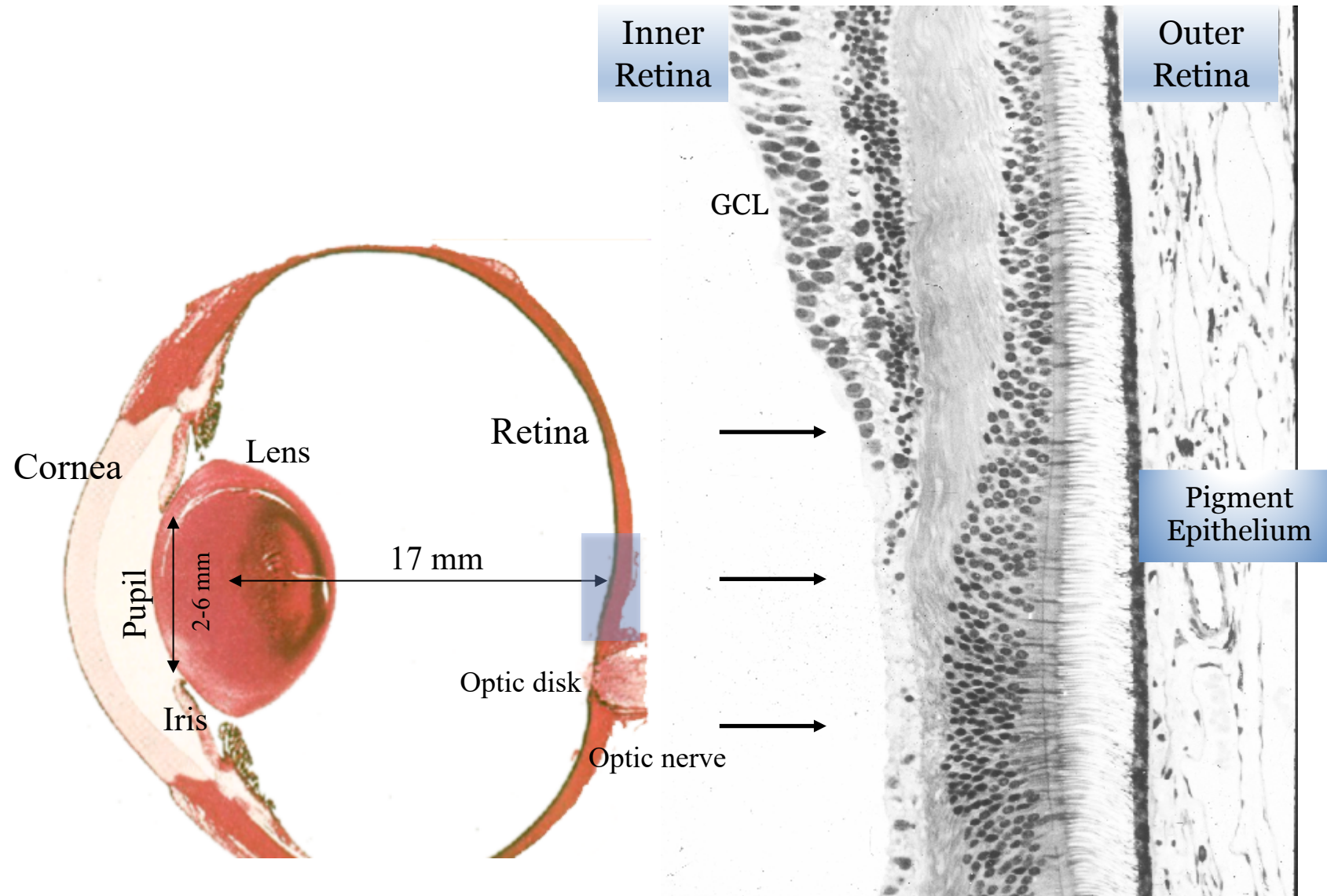


Human eye in cross-section

F-number $\sim 2.4-11$
Retinal thickness $\sim 0.4\text{mm}$



The primate fovea (pit) contains mainly cones and is specialized for high acuity and color



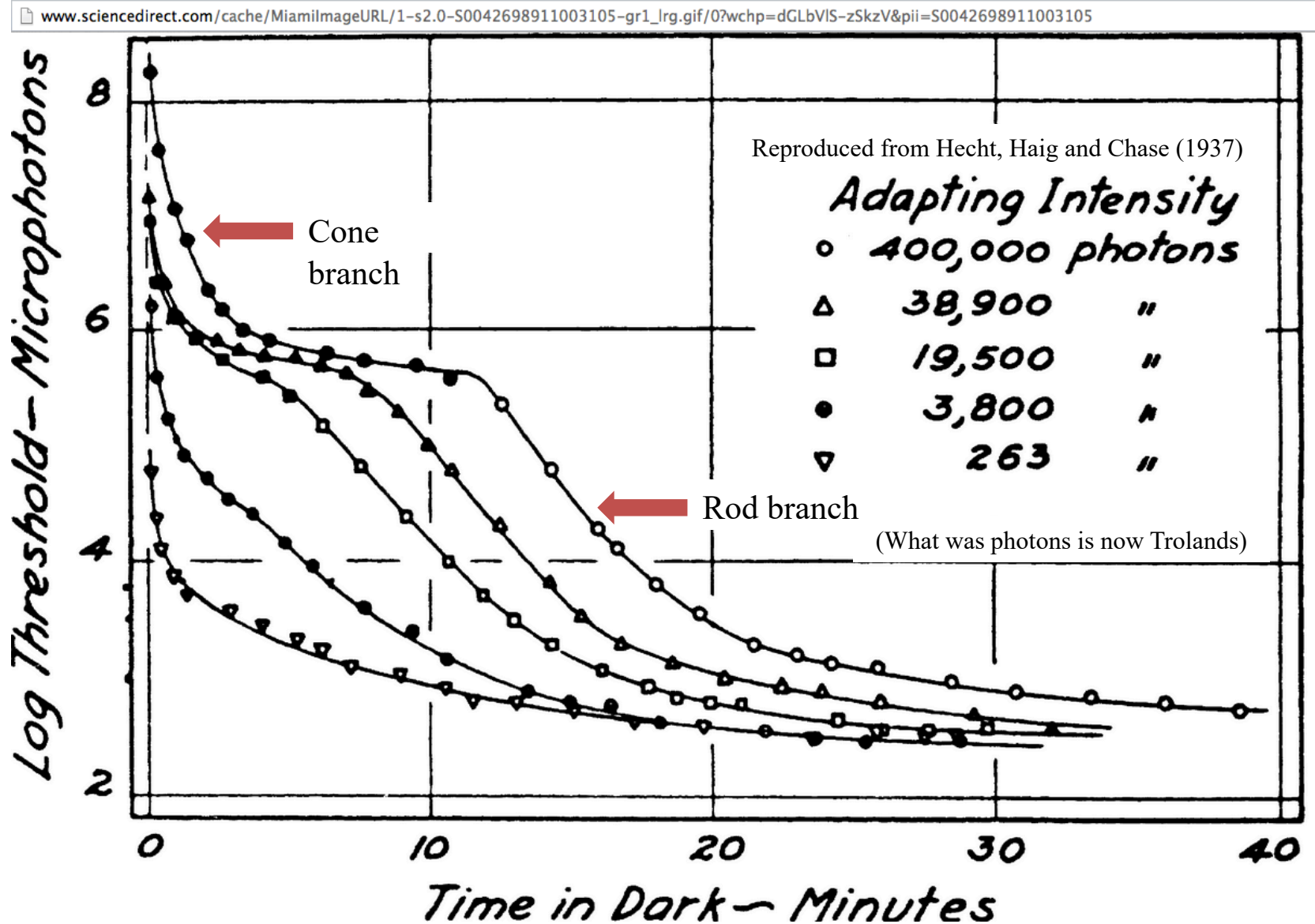
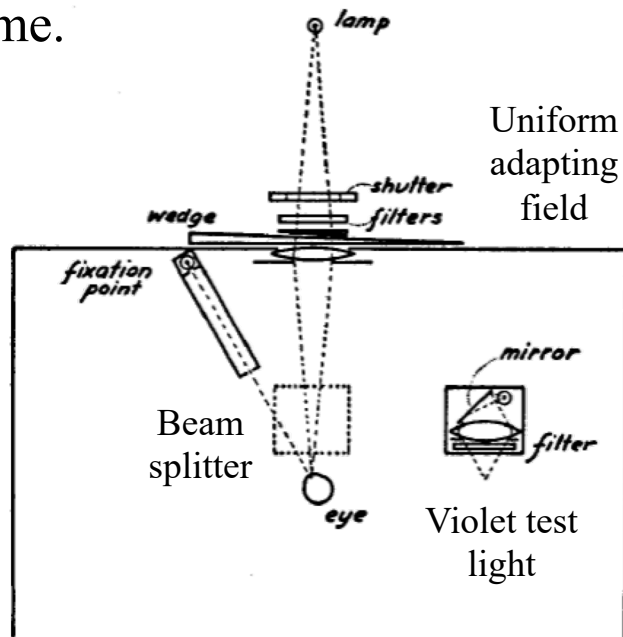
- 5 x 5 cm, 0.4 mm thick
- 5×10^6 cones
- 10^8 rods
- Foveal cone width: 1 μm
- Contacts per cone: 250
- 10^6 optic nerve fibers

Dark adaptation distinguishes cones and rods

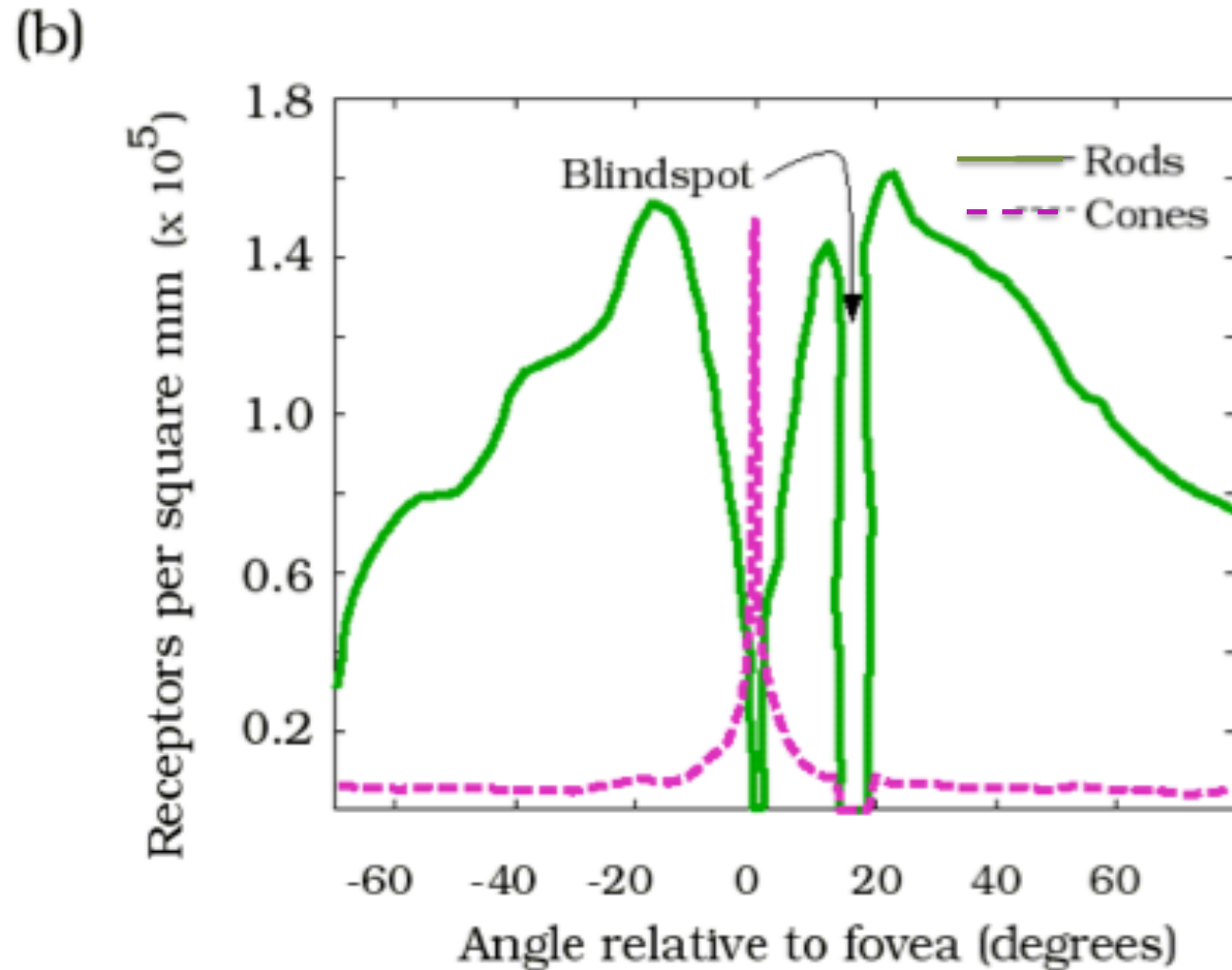
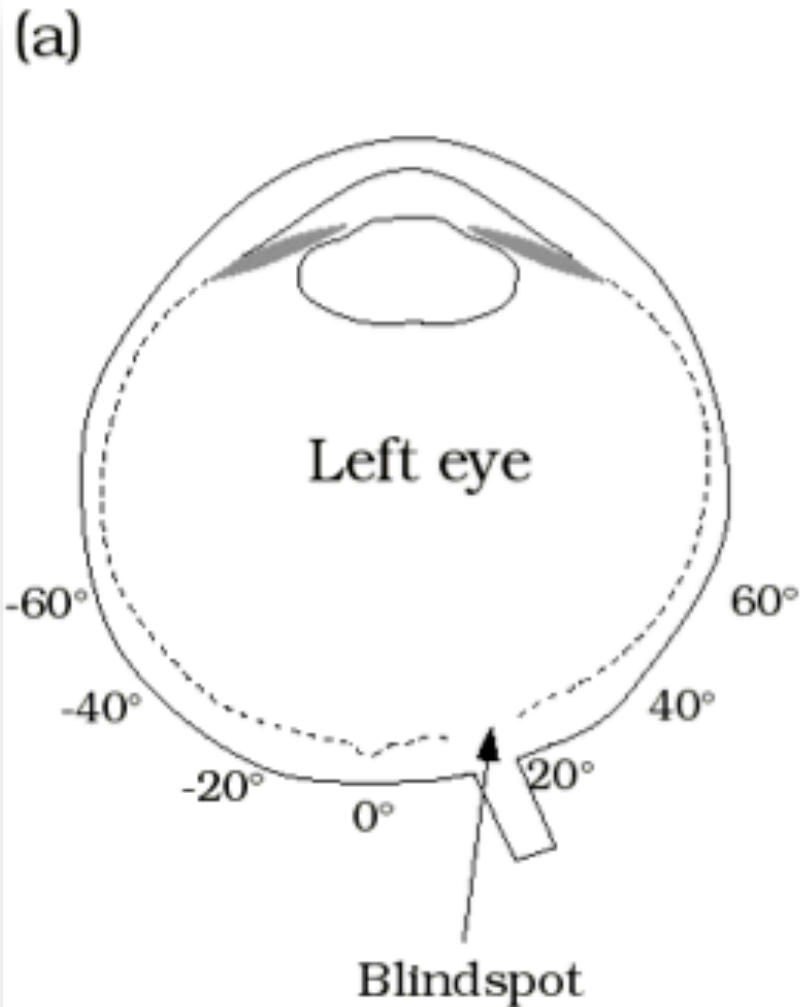
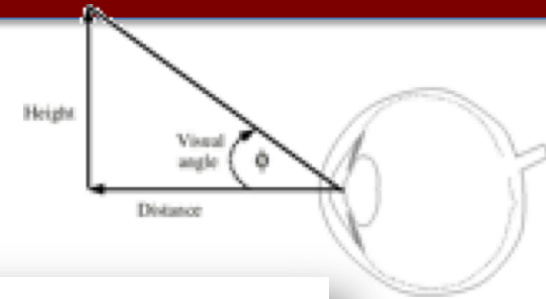
The subject is exposed to a large, (30 deg) uniform field, in the periphery.

The field is extinguished, and a violet test light is presented.

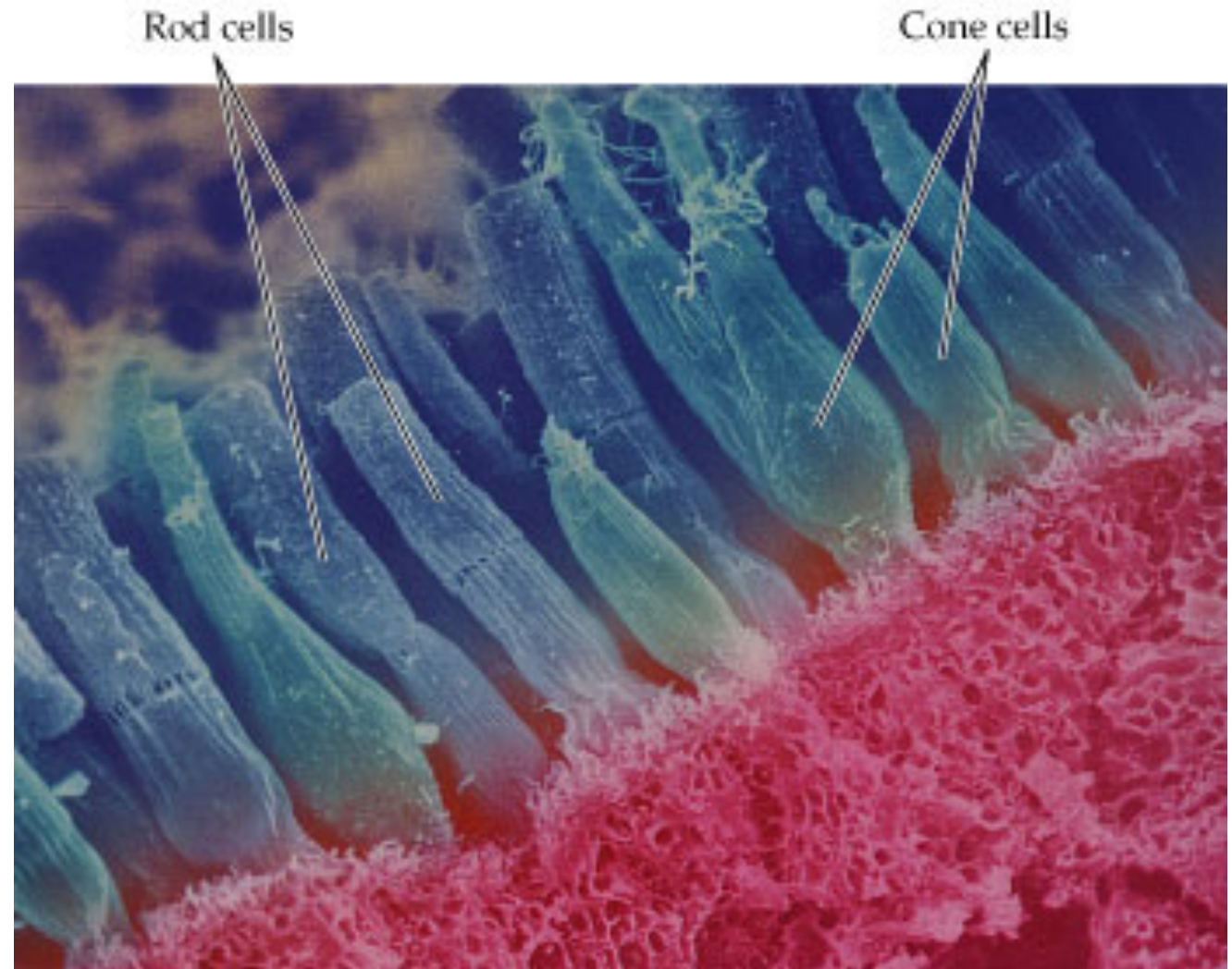
The subject adjusts the test intensity to threshold, over time.



Spatial distribution of human photoreceptors (rods and cones)



- Rods and cones seen through a scanning electron microscope.
- Each rod is about one micron across.
- Rods and cones are intermingled in the visual periphery

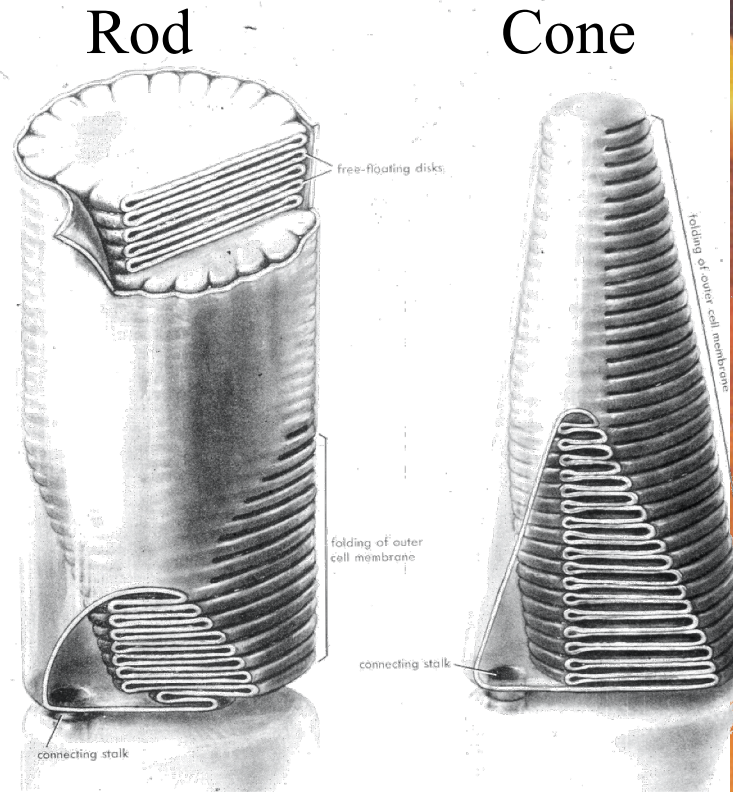


Rods and cones

<http://webvision.med.utah.edu/photo1.html>

Rods and cones in schematic, and as estimated through a scanning electron microscope.

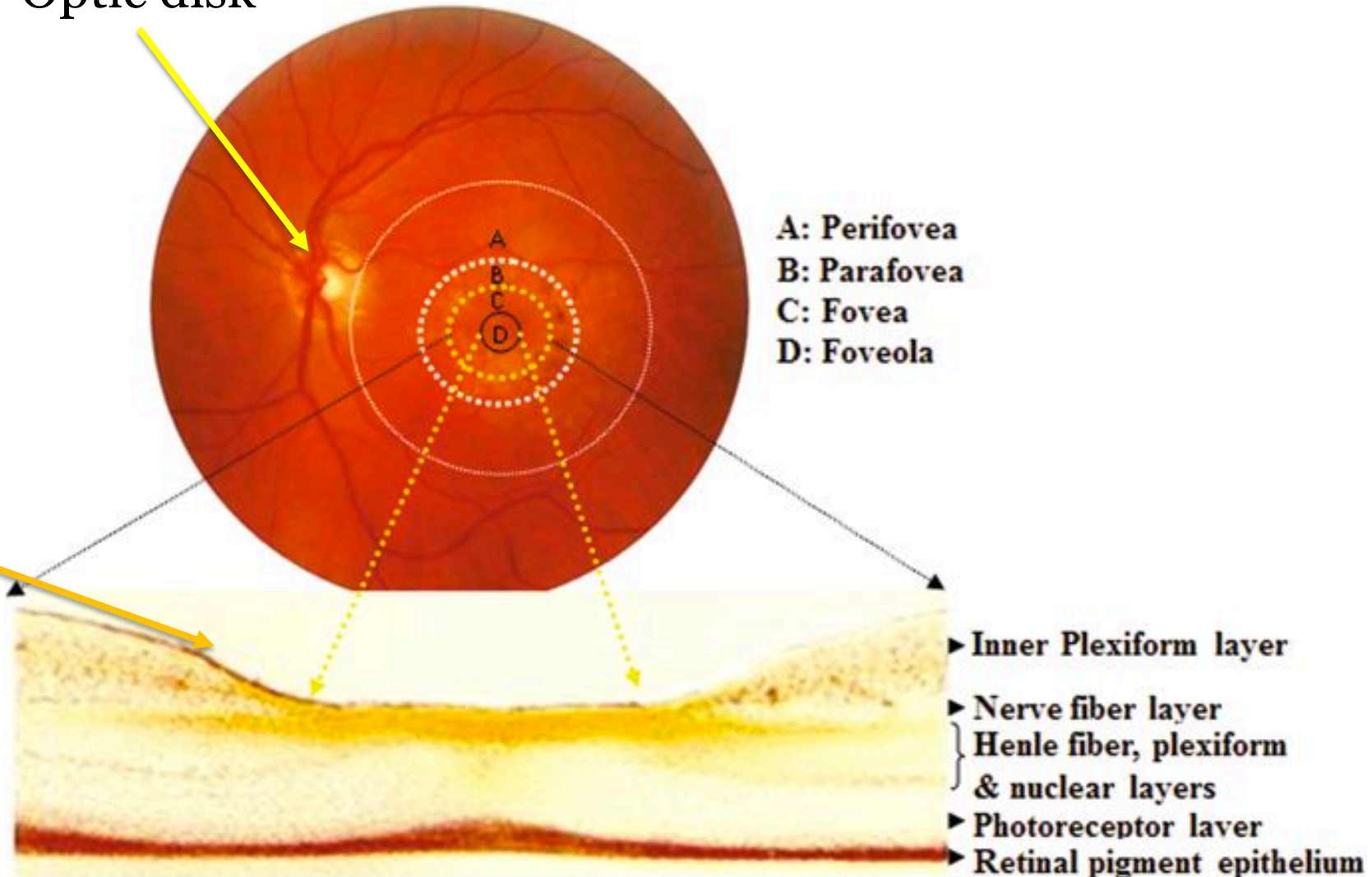
Each rod is about one micron across.



Retinal terminology

- Fundus image of the retina
- Fovea and blindspot
- Macular pigment

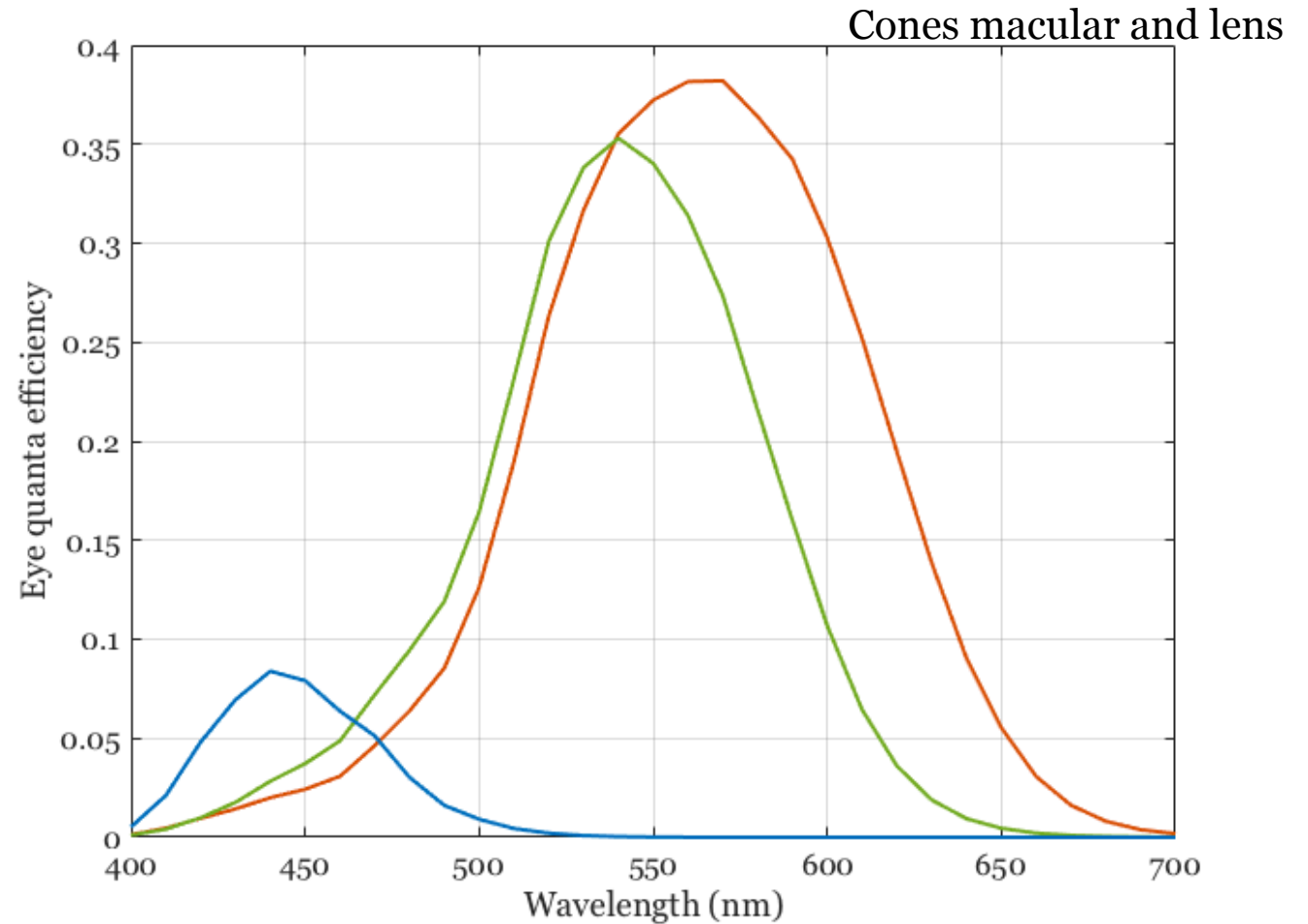
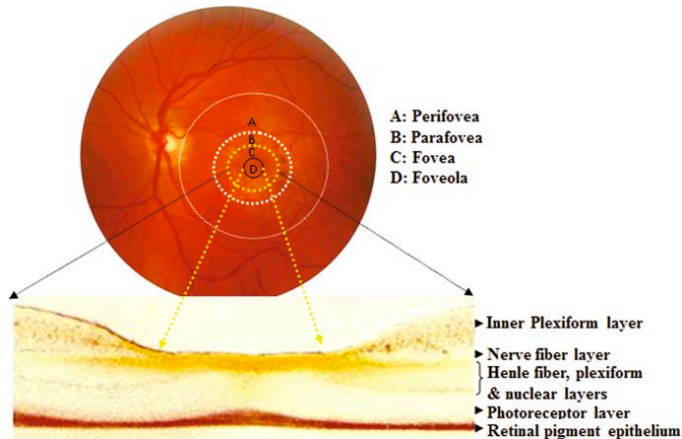
Optic disk



Henle fiber -
the layer of inner cone fibers in the central area of the retina.

Human wavelength absorptions depend on a series of factors

- Cone photopigments (L,M,S) absorption efficiency for standard pigment density
- Including the effect of the lens and macular pigment



Impact of the lens and macular pigment

The lens and macular pigment have a dramatic impact on the light that gets to the cone photoreceptors

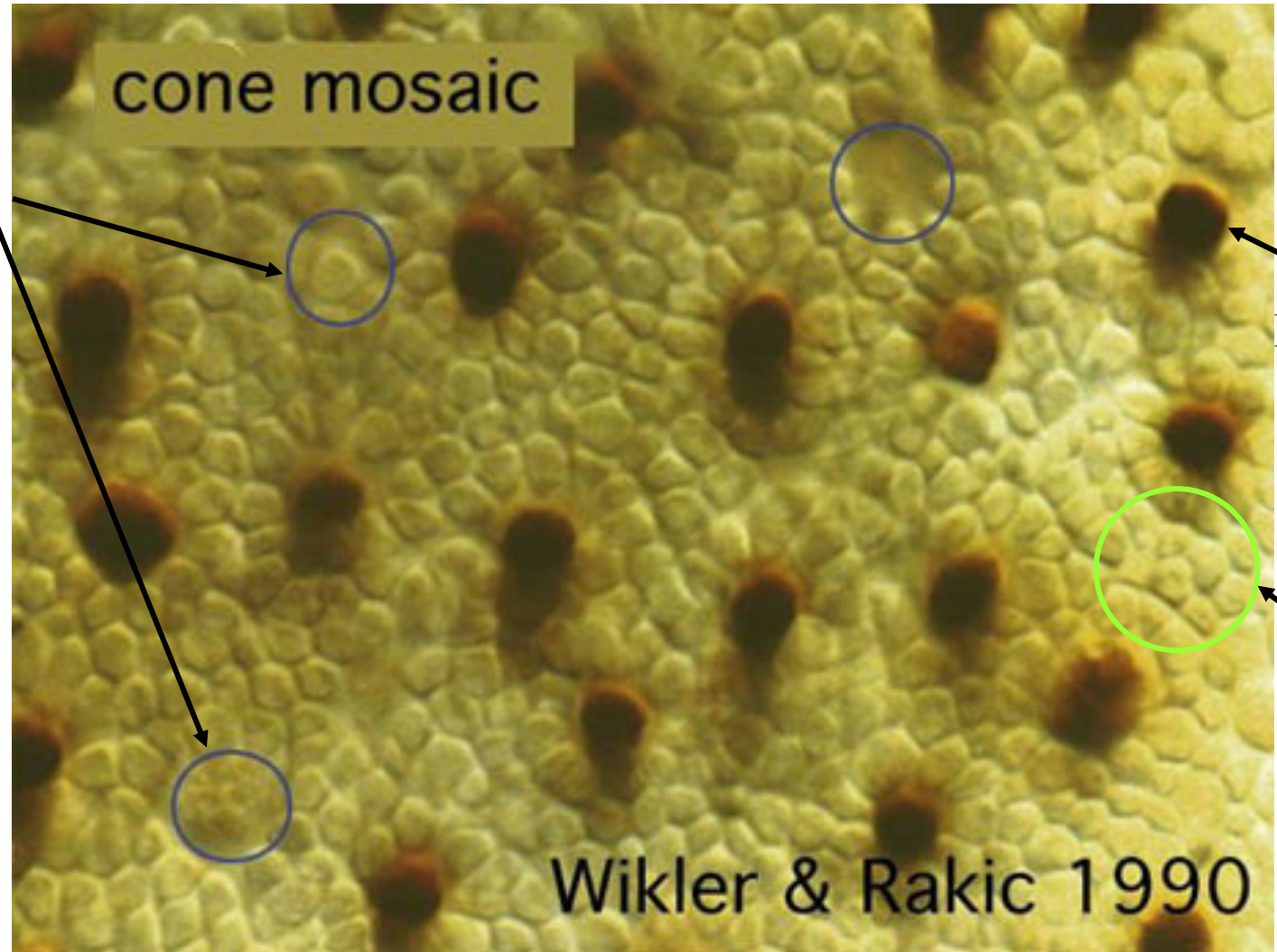


Cone mosaic

5 μm

- L,M cones stained
- S-cones not stained
- Small cross-sections are rods
- Near periphery in the retina

S cones



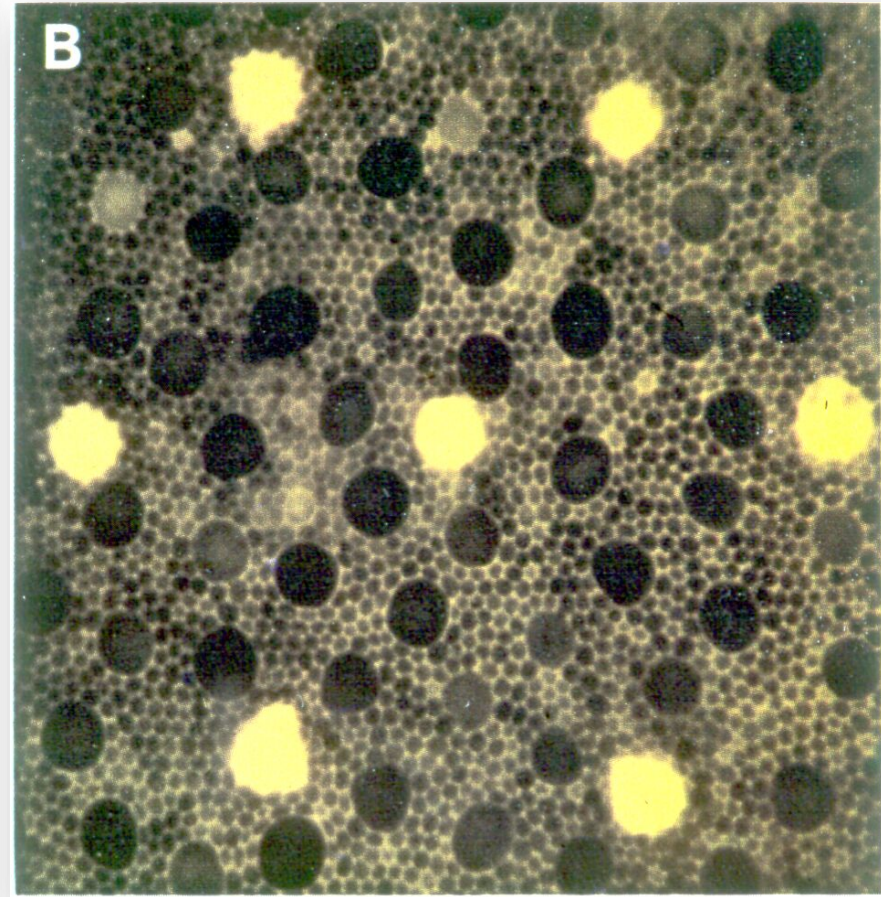
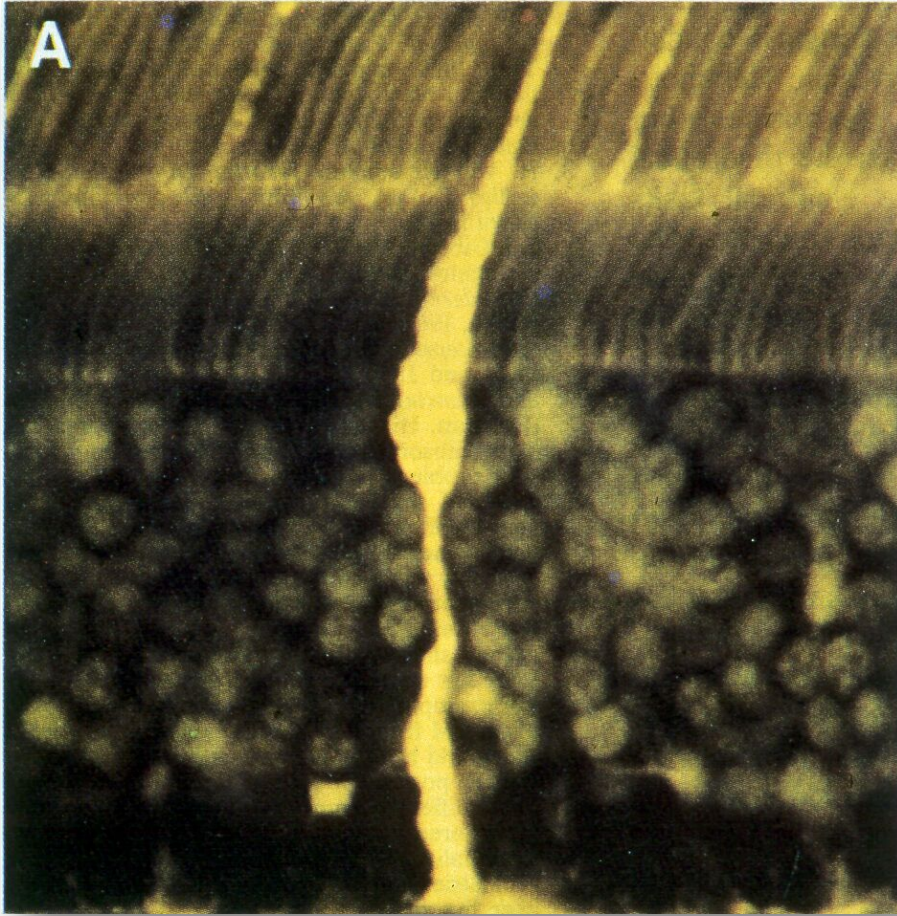
L,M cones

rods

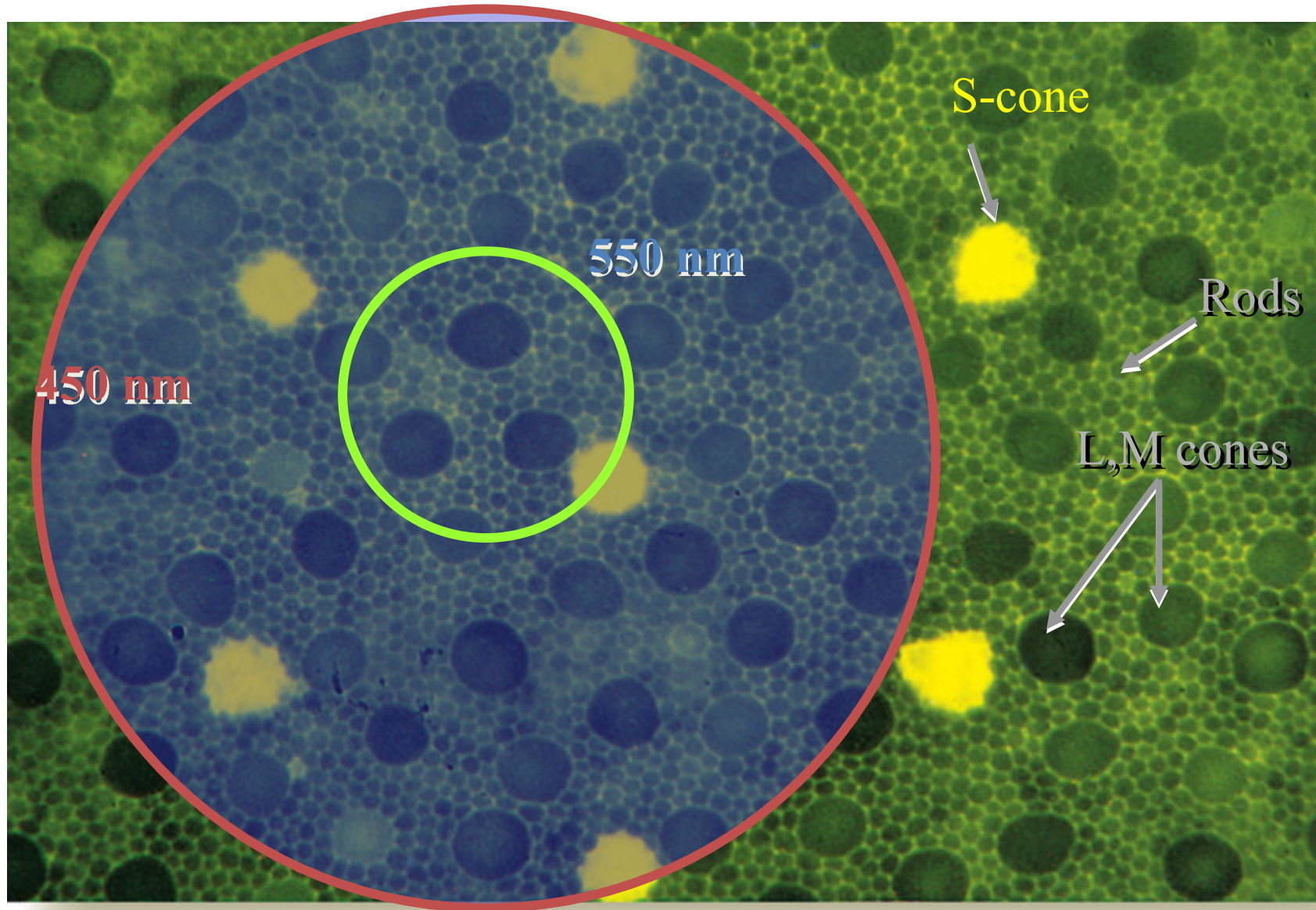
Wikler & Rakic 1990

S-cones labeled

5 μm



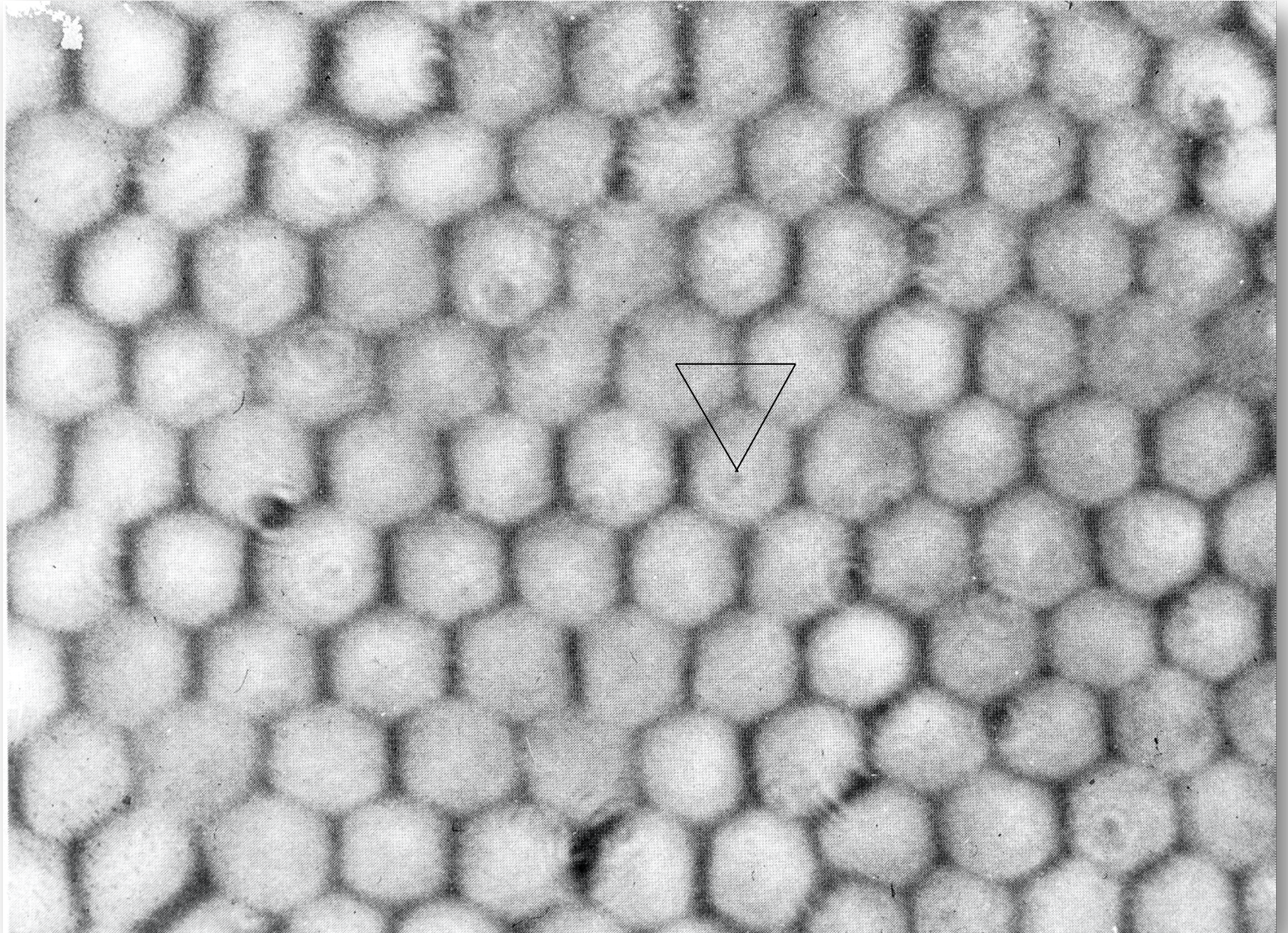
Photoreceptor mosaic



Foveal cone mosaic in central foveola

- Triangular (hexagonal) packing
- All cones
- Inner segment
- Miller et al.

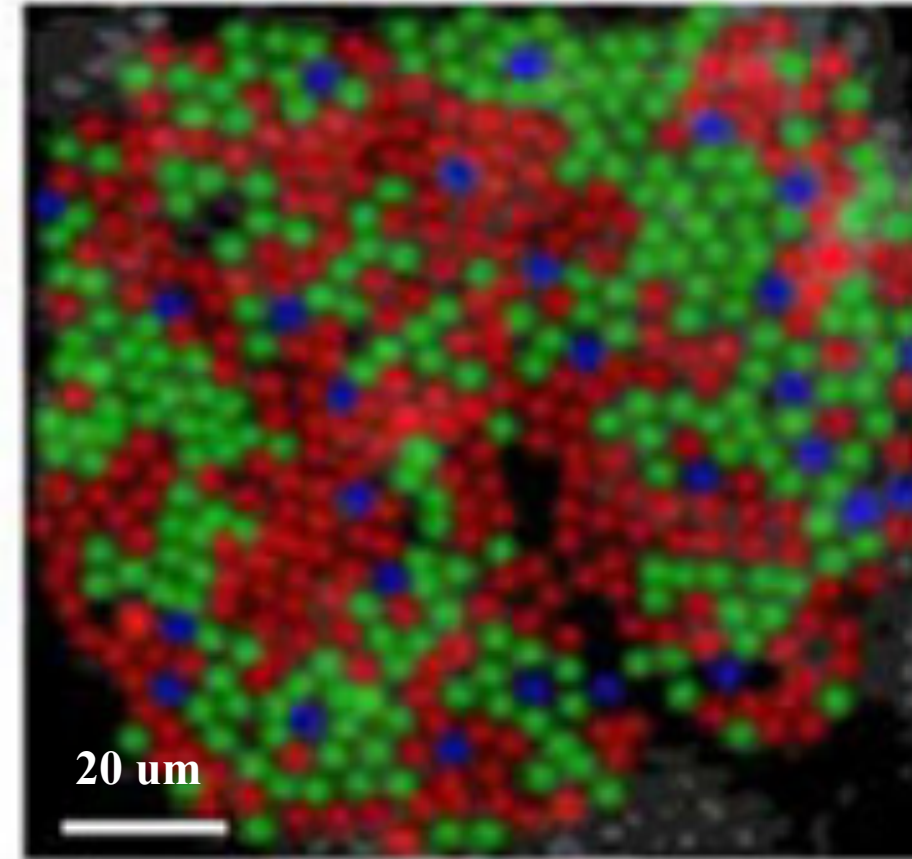
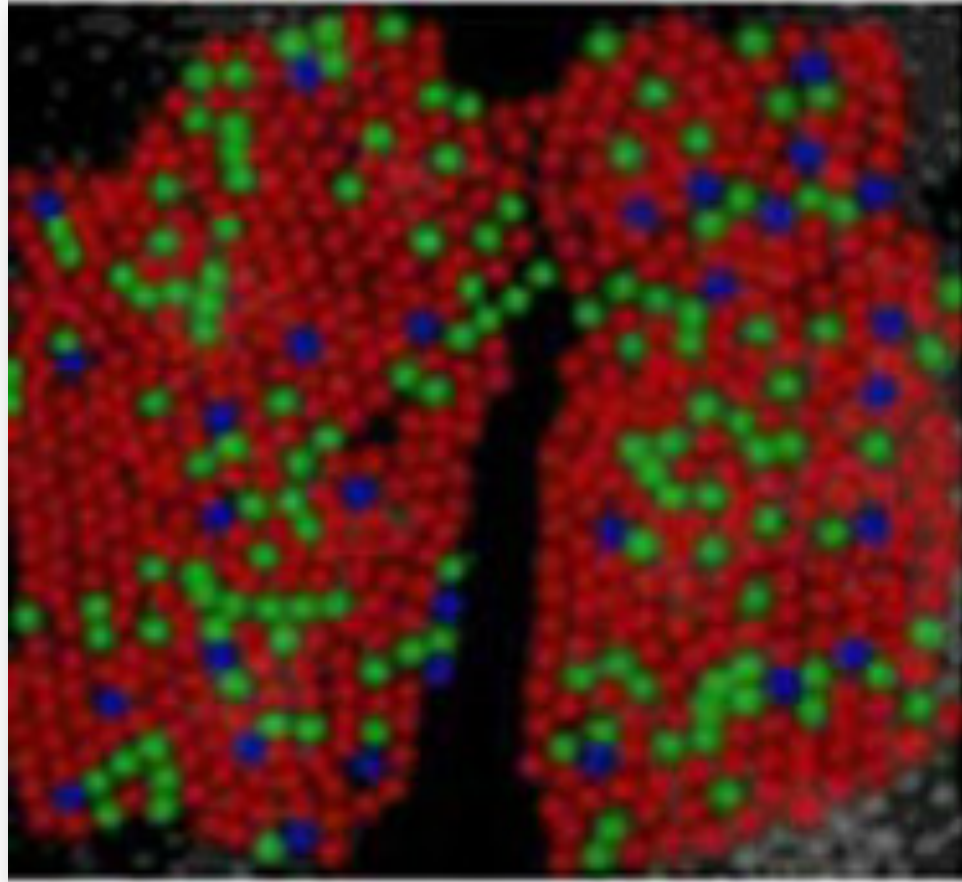
5 um



Cone receptor mosaic (Roorda and Williams, 1999)

L:M cone ratios: 3.8:1 and 1.15:1 – yet both are normal

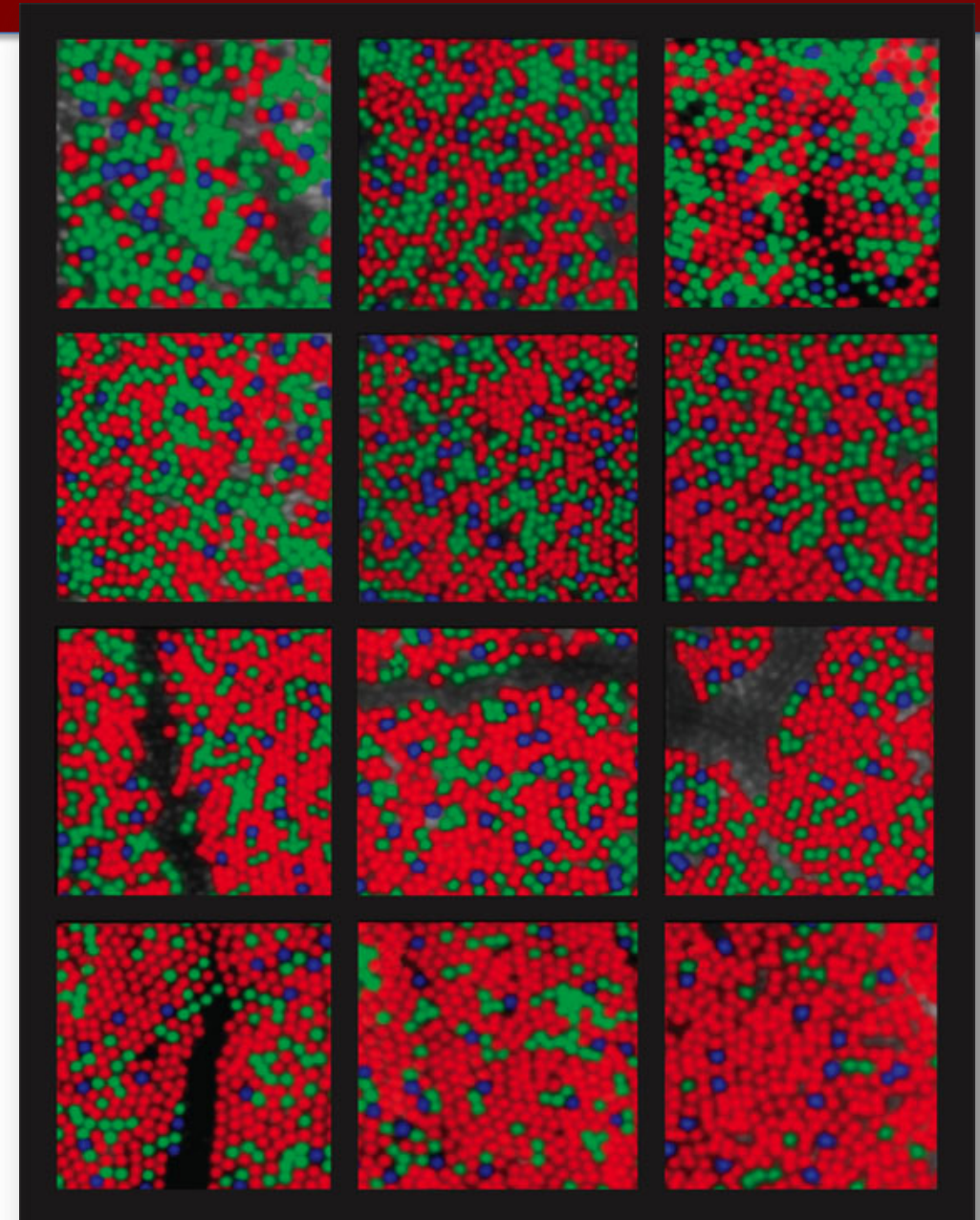
Enormous
variation in the
number of L and
M cones in
different people



Ratio of L/M cones differs greatly between normals

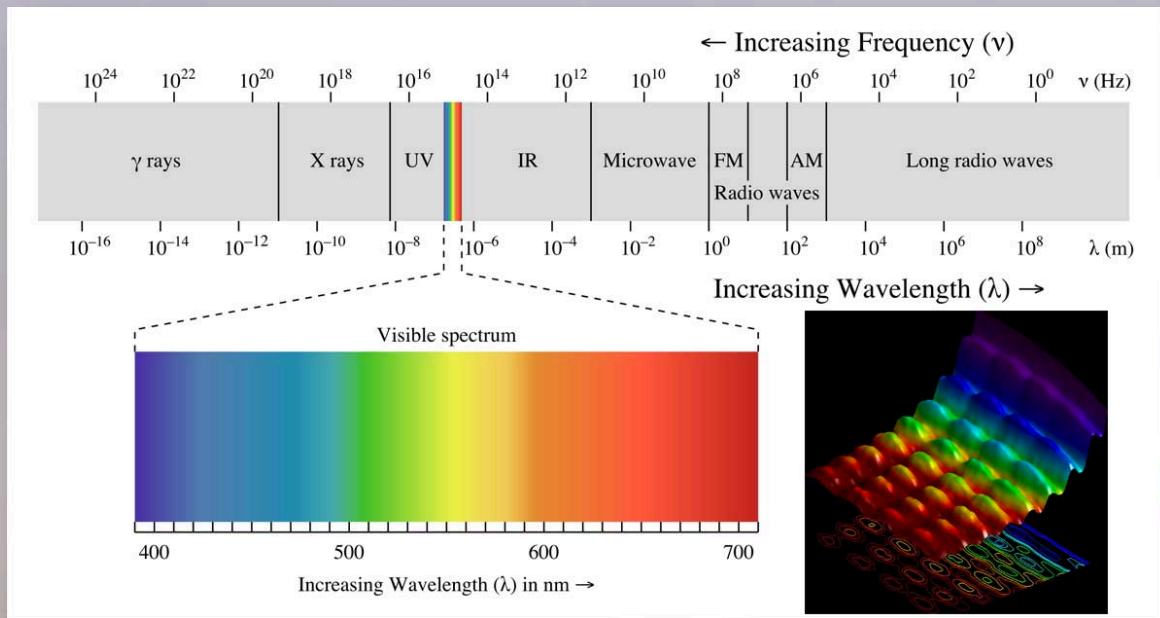
- 1 deg is about 300 microns (um)
- Cone inner segments
 - 1-2 um diameter (central fovea)
 - 3-4 um (0.6 deg eccentricity)
- If average diameter is 3 um, then ~100 cones/deg in foveola (central 1 deg)
- Nyquist is about 50 cpd

10 um

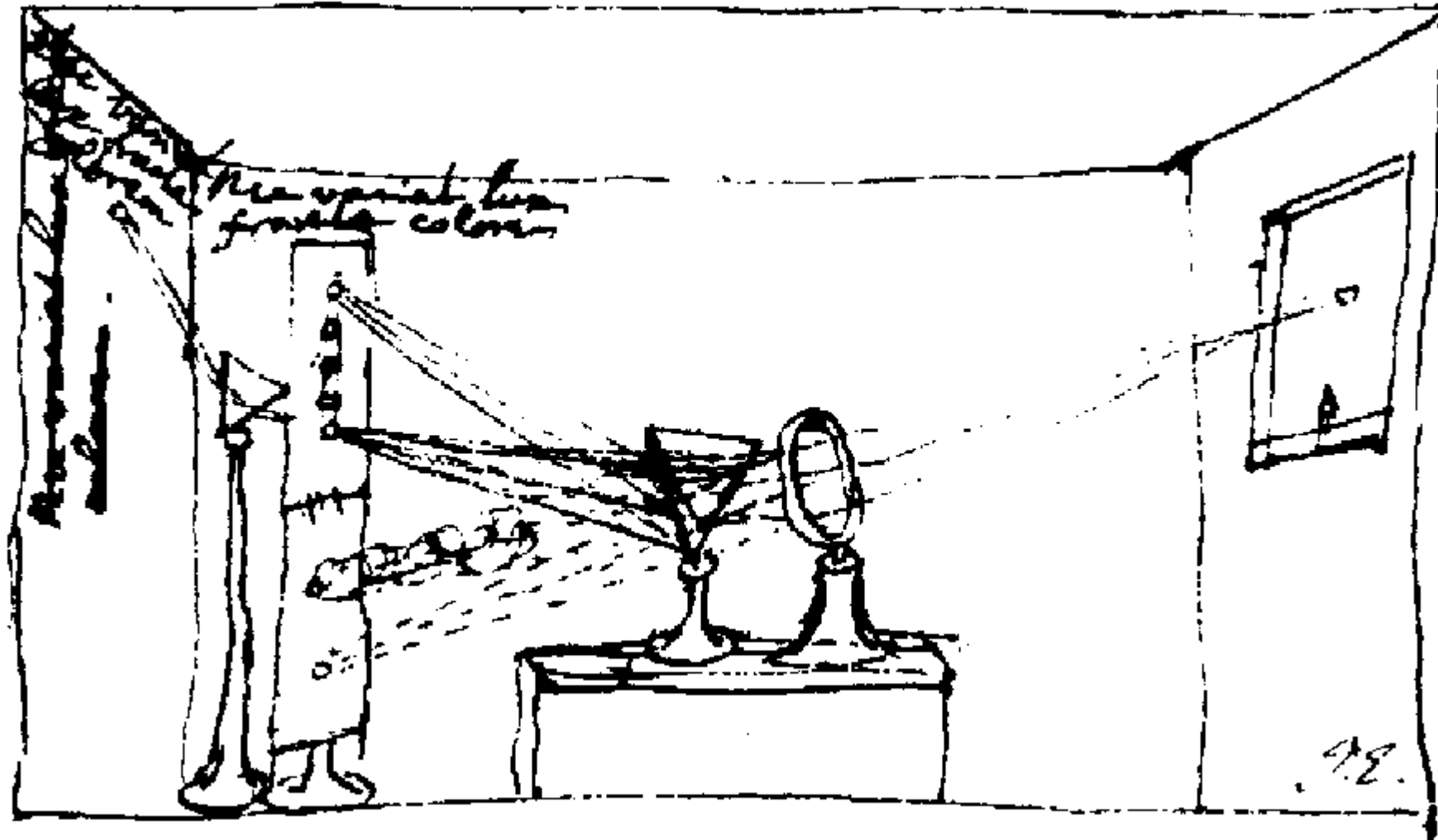


Light and superposition

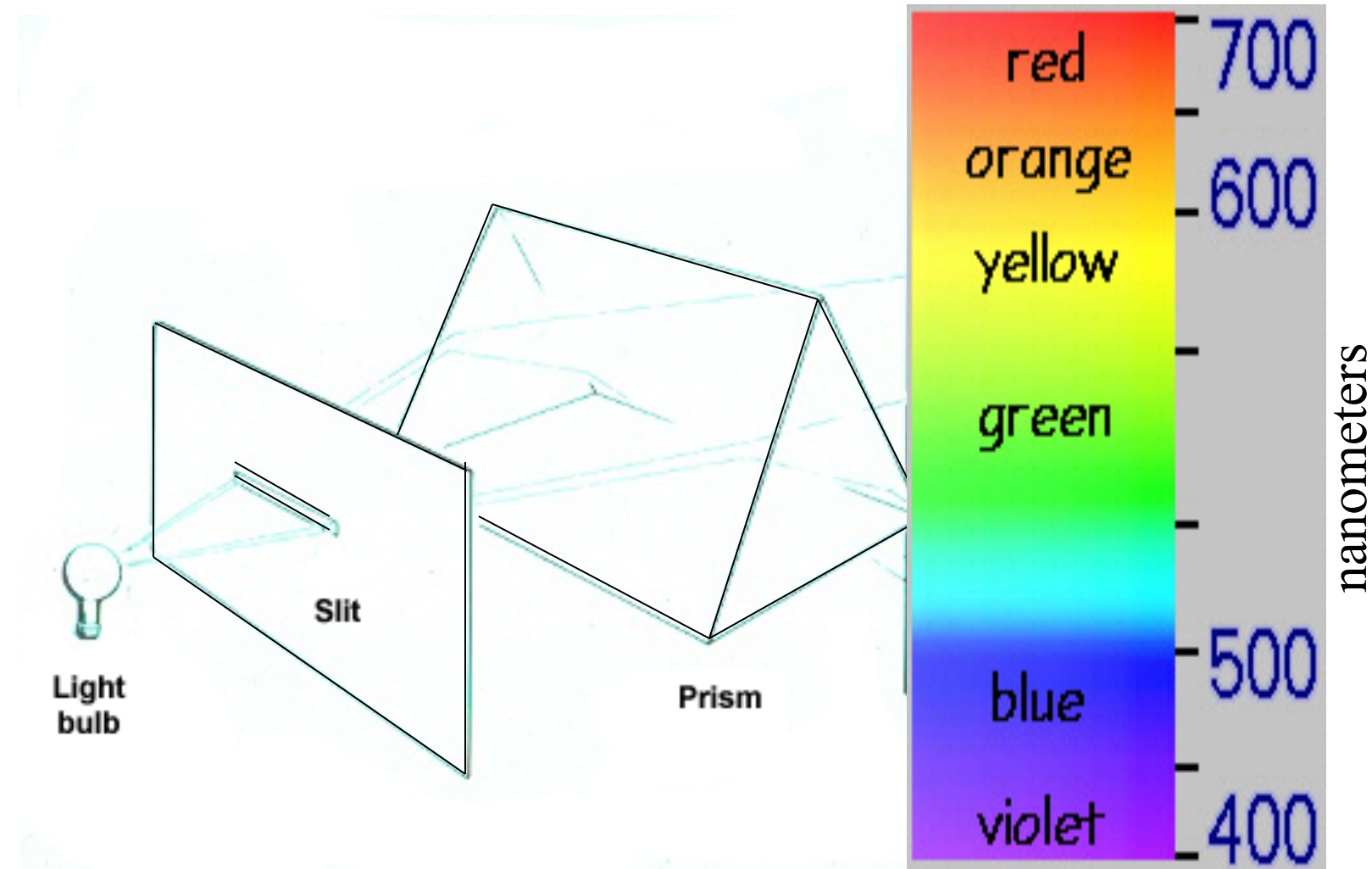
- Spectrum
- Superposition



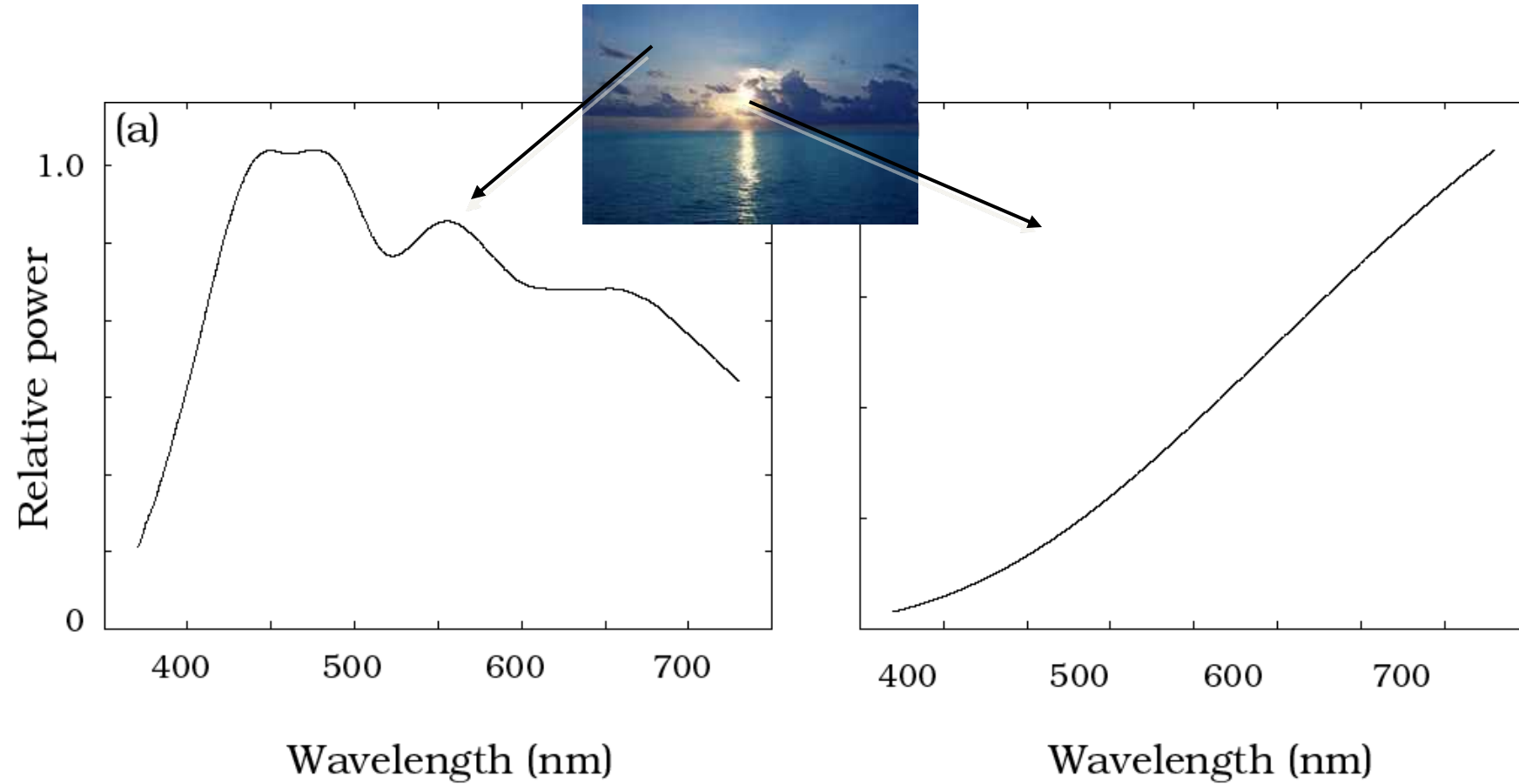
The fundamental components of light



Monochromators measure the energy at different wavelengths



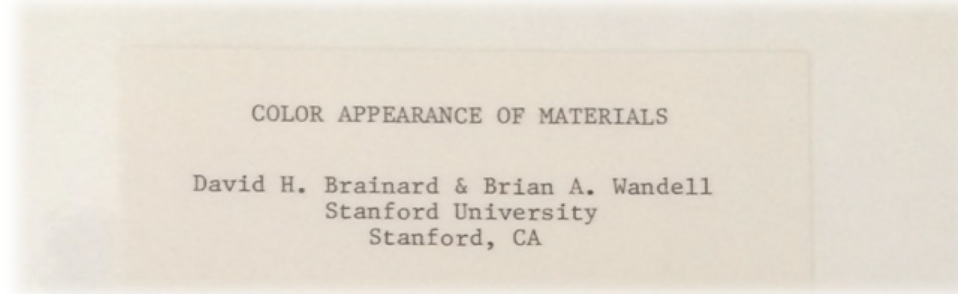
Typical daylight SPDs vary



SPD: spectral power distribution

Same objects but illuminated by two different sources

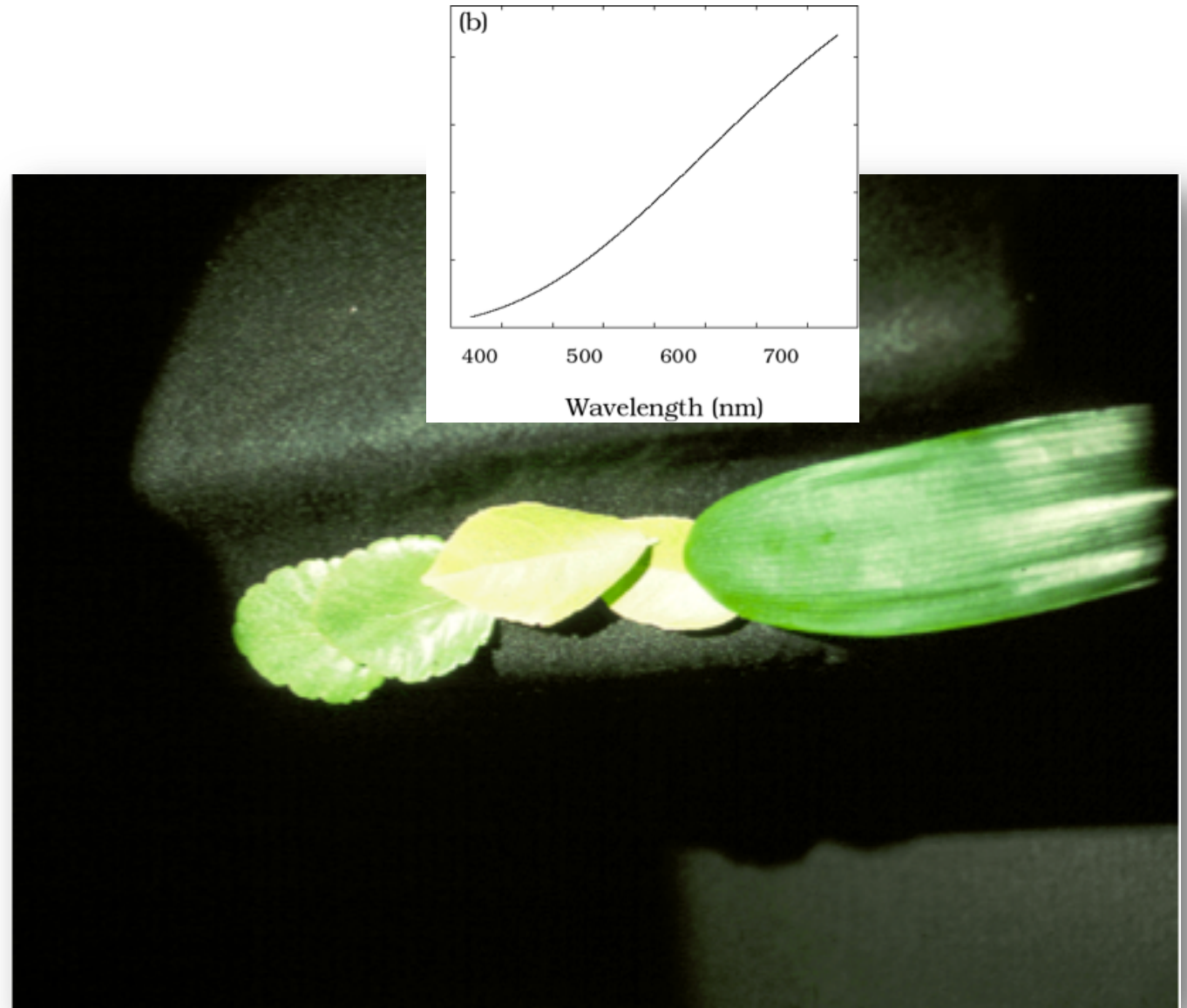
Objects and lights interact on a wavelength basis, not in RGB space



From R.M. Evans work at Kodak in the
1940s

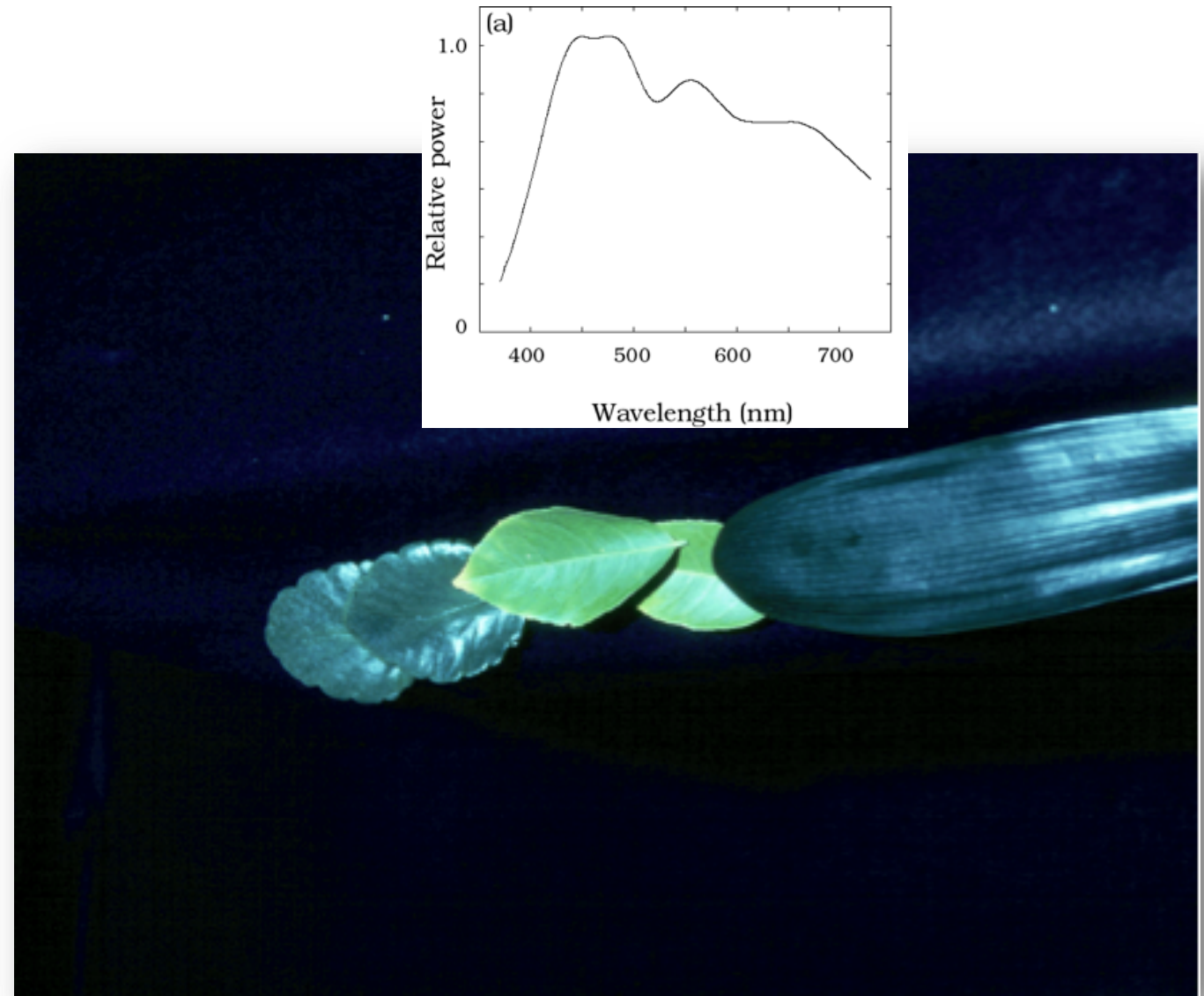
Scene radiance depends on reflectance and illumination

- People want to recognize the object – hence estimate reflectance
- The visual system interprets color in a way that accounts for the spectral properties of the illuminant

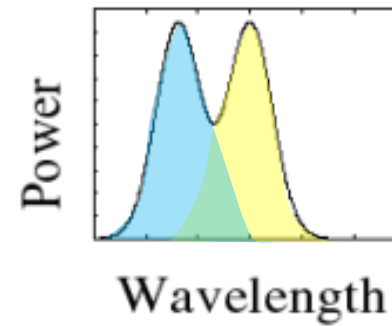
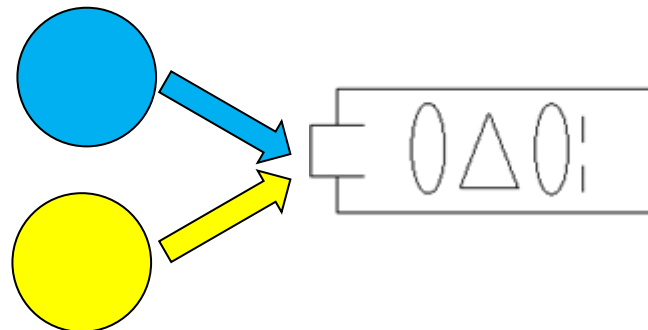
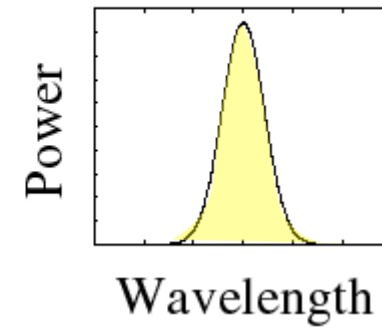
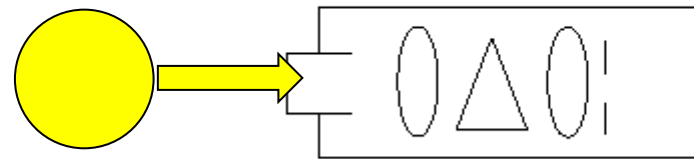
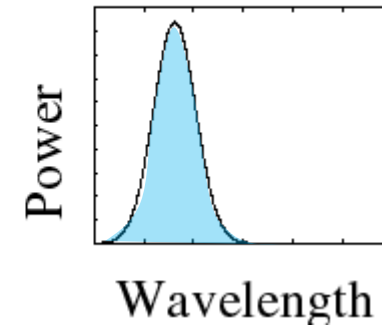
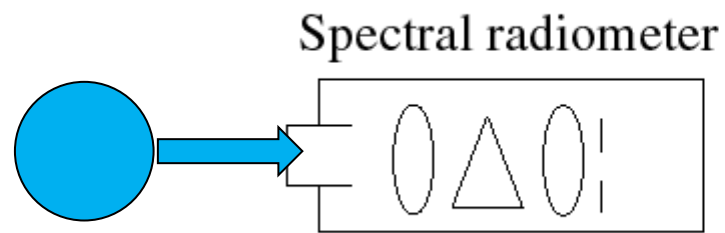


Scene radiance depends on reflectance and illumination

- People want to recognize the object – hence estimate reflectance
- The visual system interprets color in a way that accounts for the spectral properties of the illuminant

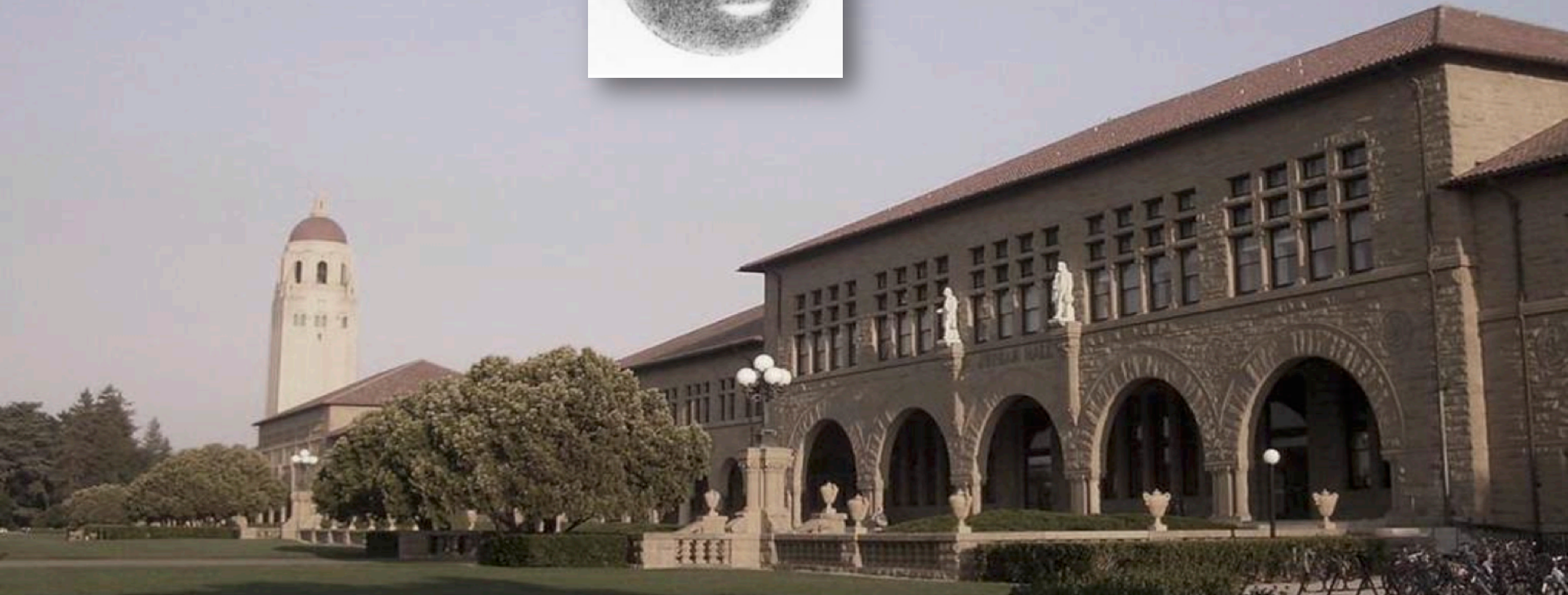


Superposition of light spectral power distributions



Rod (scotopic) color matching

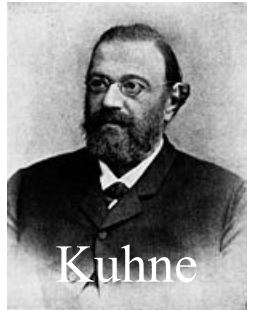
Rhodopsin
Rod color-matching



Visual purple and the optogram



Boll



Kuhne

- Boll noticed that the light-sensitive pigment in the rods of the retina had a tendency to fade in the presence of illumination
- Kuhne made optograms, such using intact rabbit retina whose retina was fixed after dark adaptation, and then fastening its head to a barred window before slicing the retina

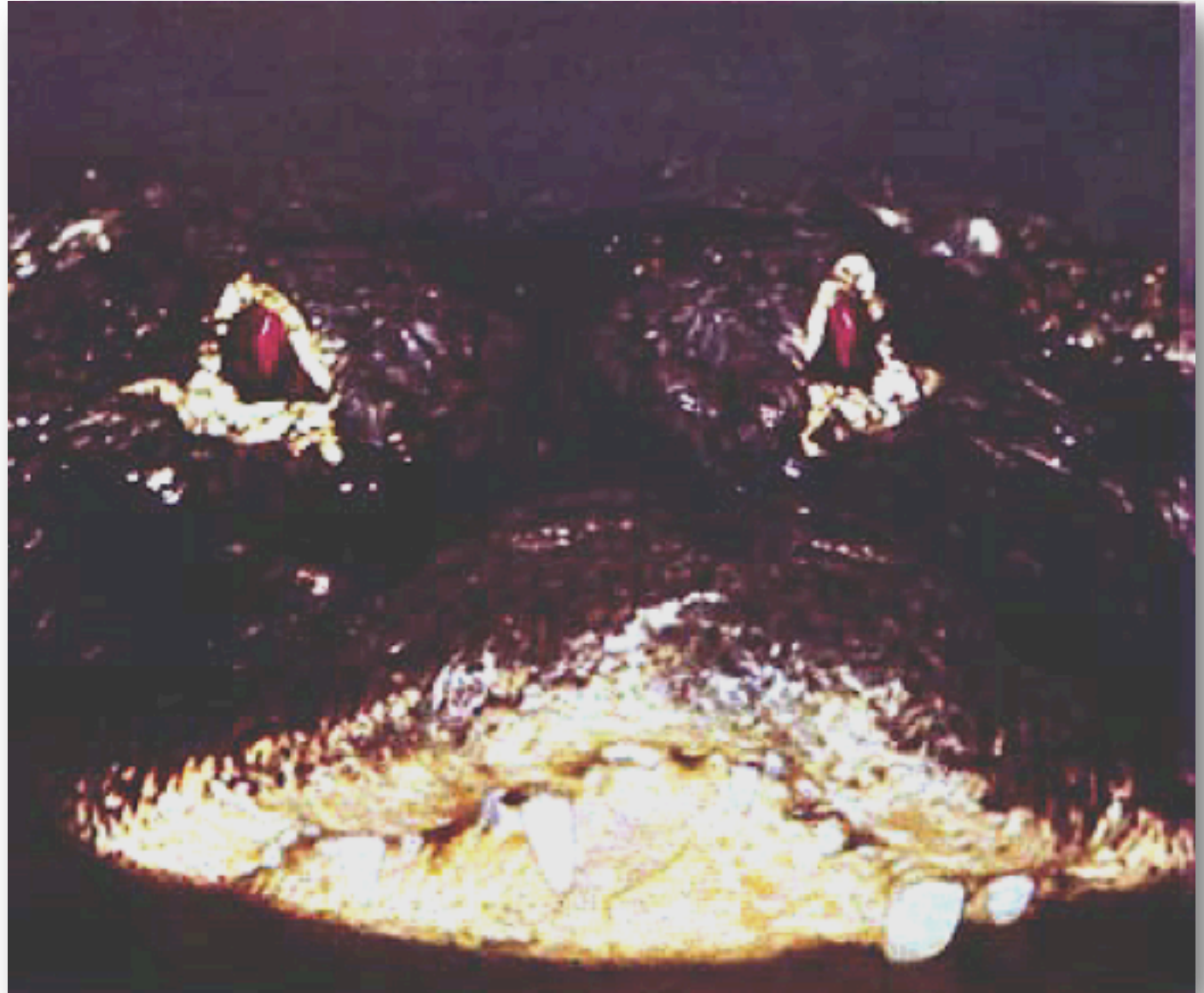


Rhodopsin: Regenerated



Rushton

The rhodopsin pigment can be seen directly in the eye of some animals



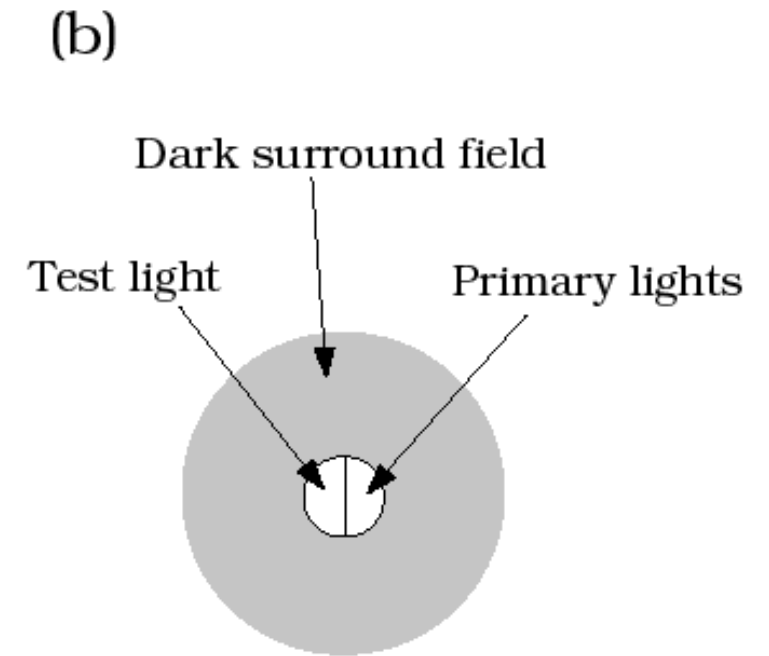
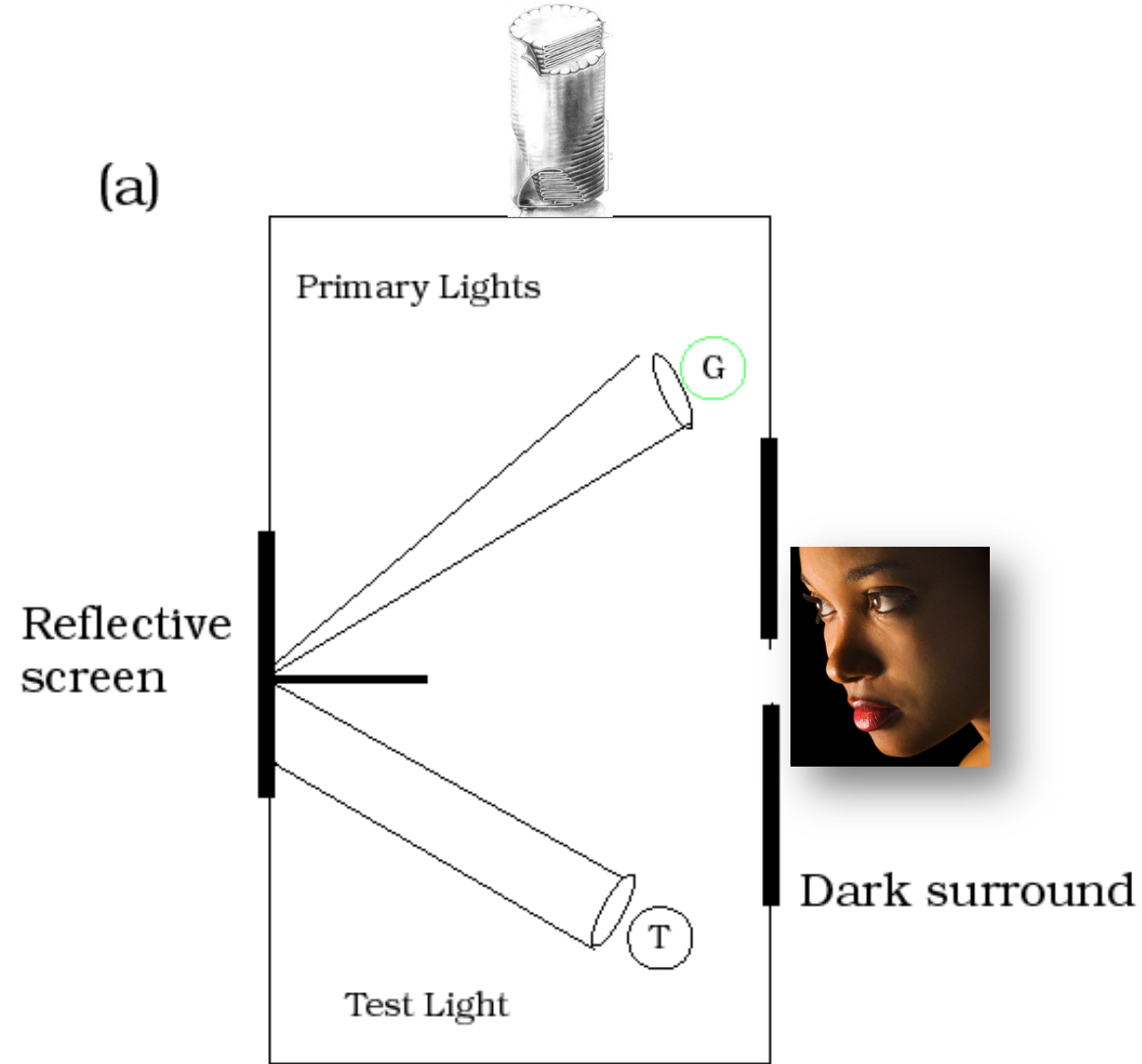
Visual purple is a synonym for rhodopsin

Rhodopsin: Bleached

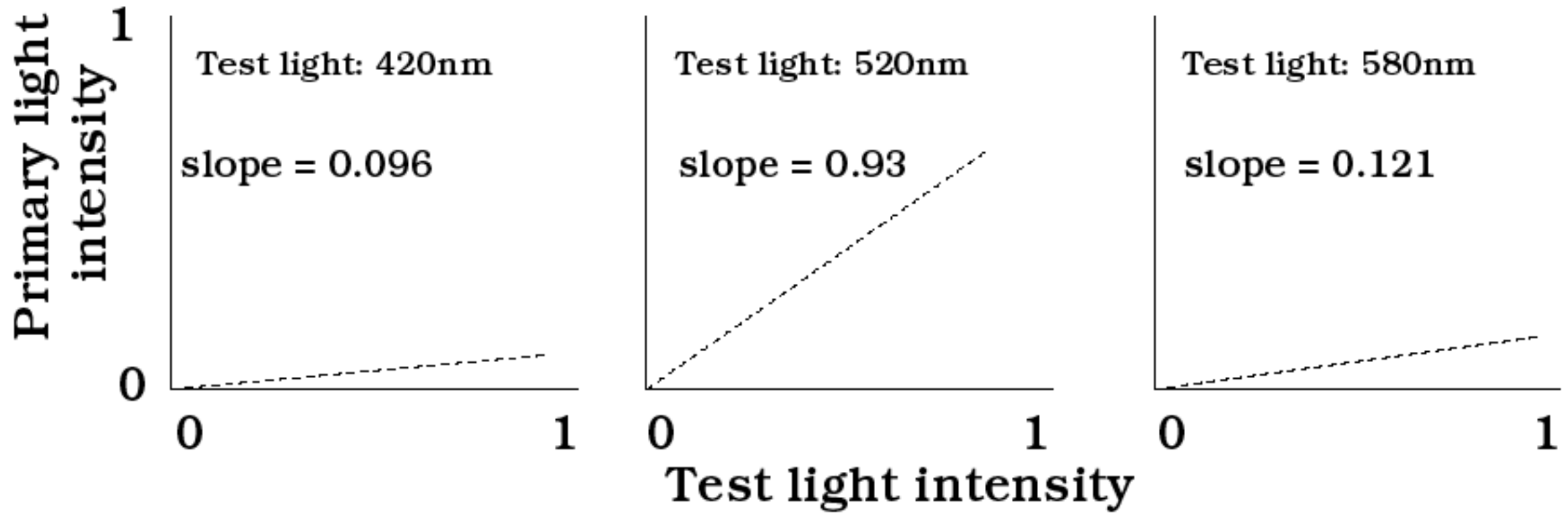
After the eye is
exposed to light, the
rhodopsin is
bleached and
invisible



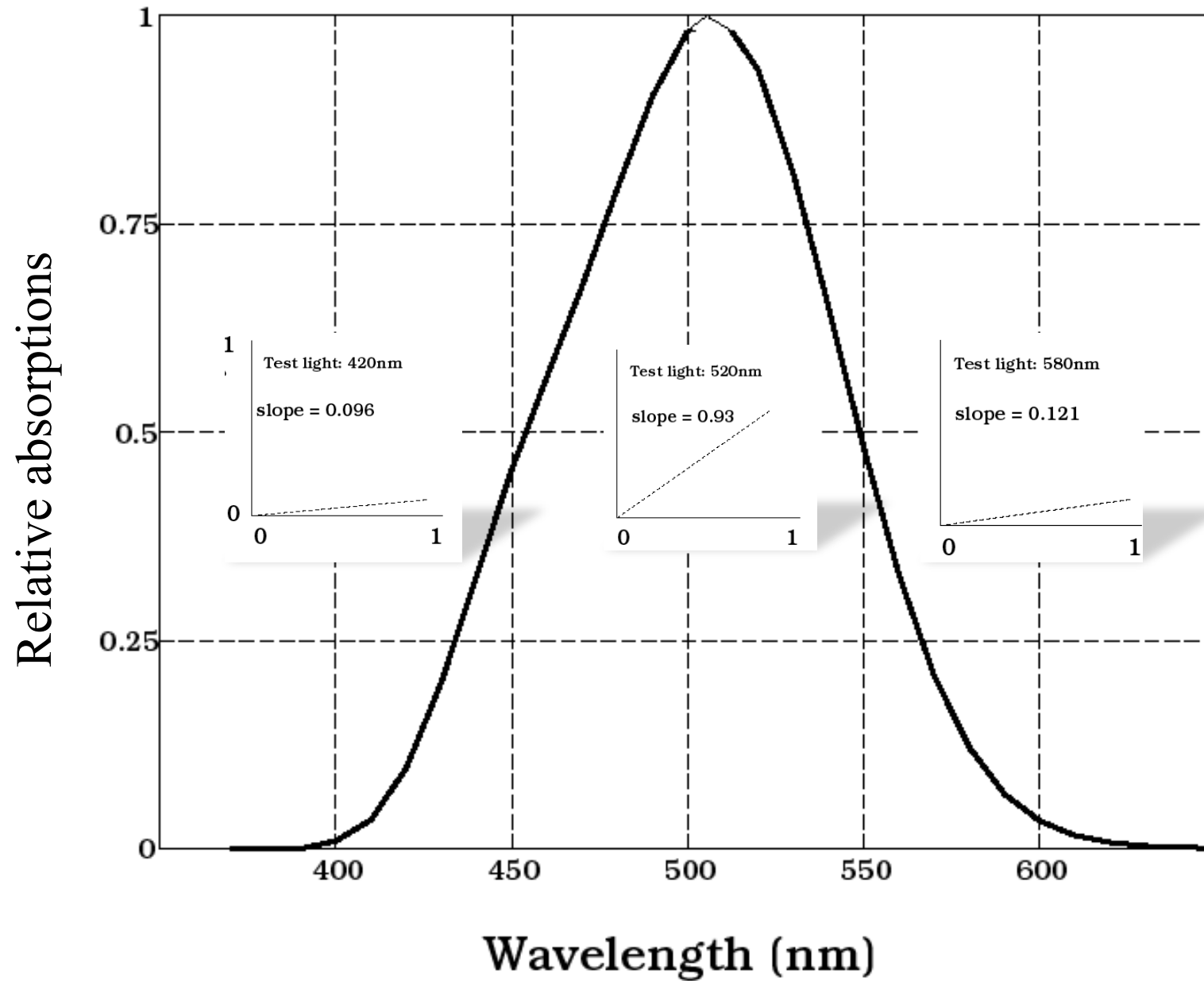
Rod color matching



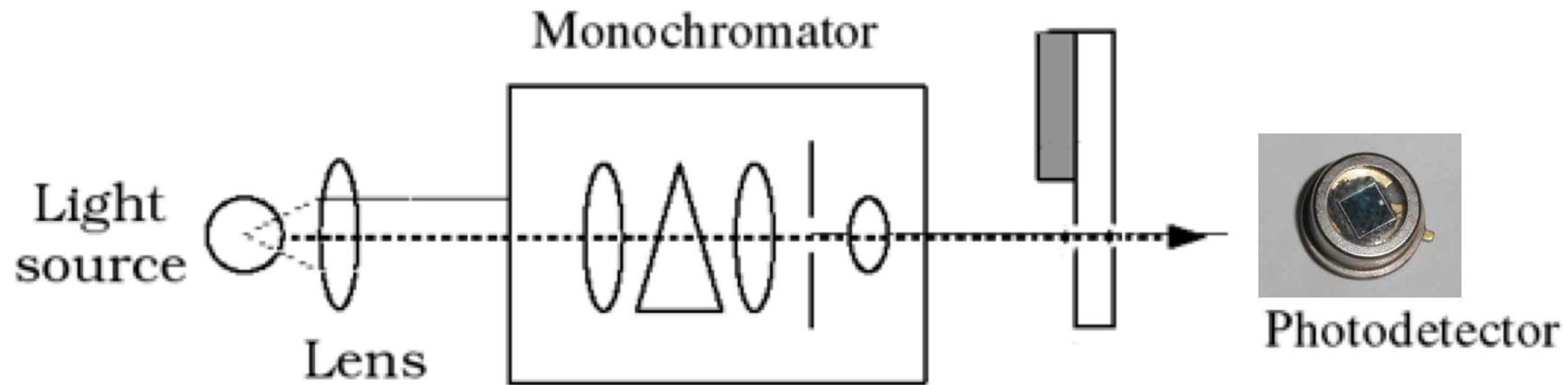
Example: Rod matches



Rhodopsin absorption curve

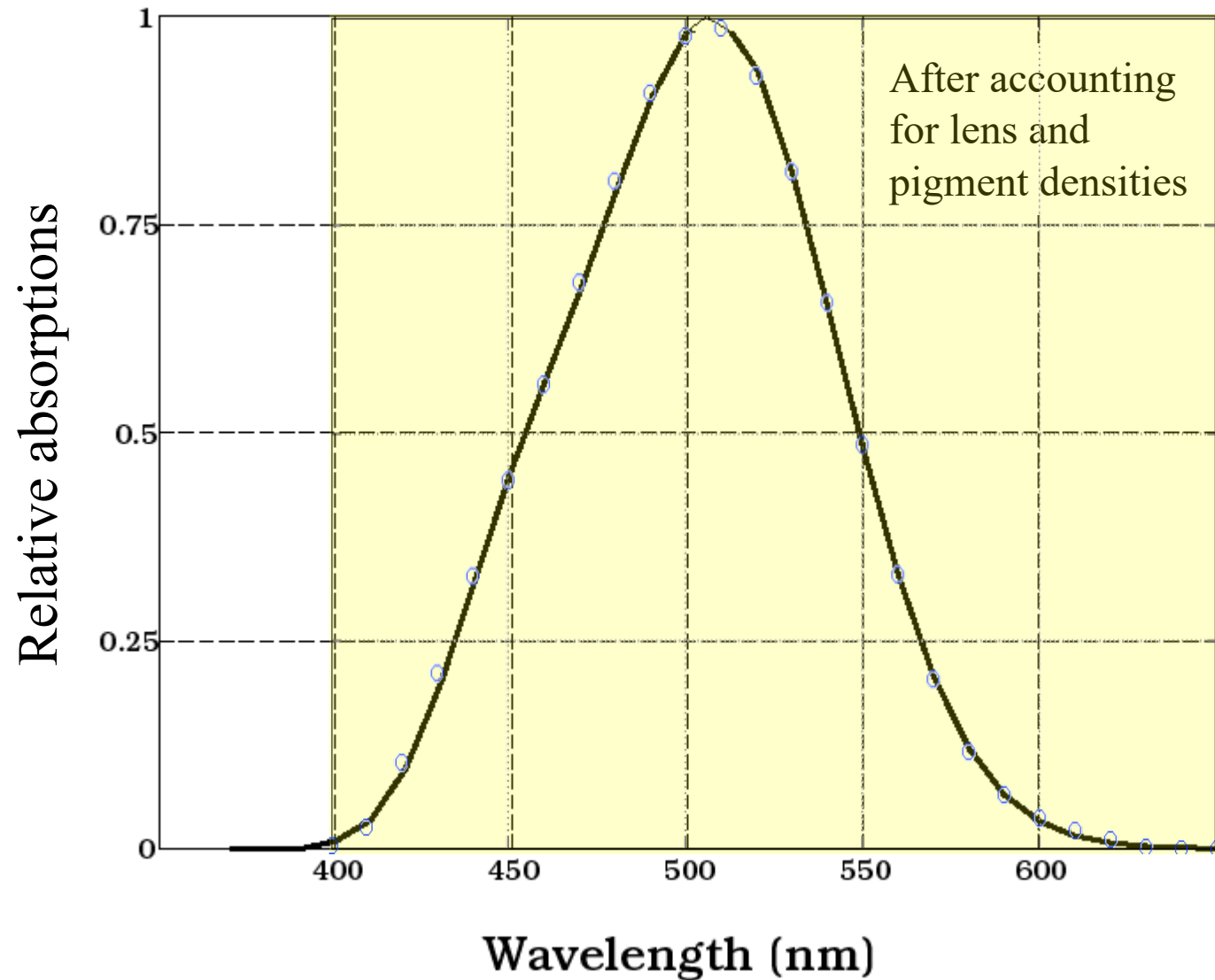


Measuring photopigment absorptions



Absorption = ratio of signals

Human light sensitivity through the rods matches the rhodopsin absorption curve



Cone (photopic) color matching

Photopic color-matching

Metamerism

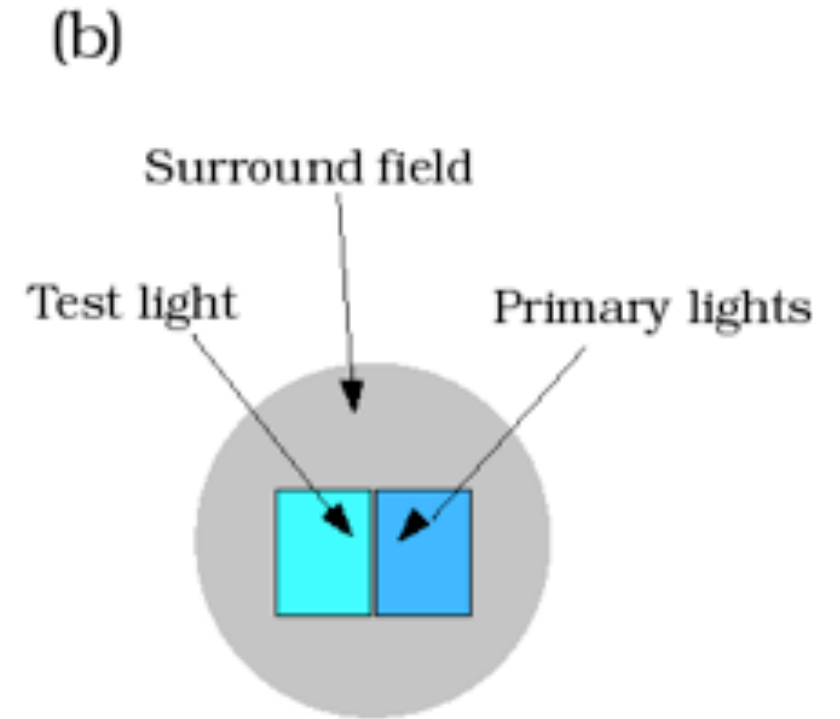
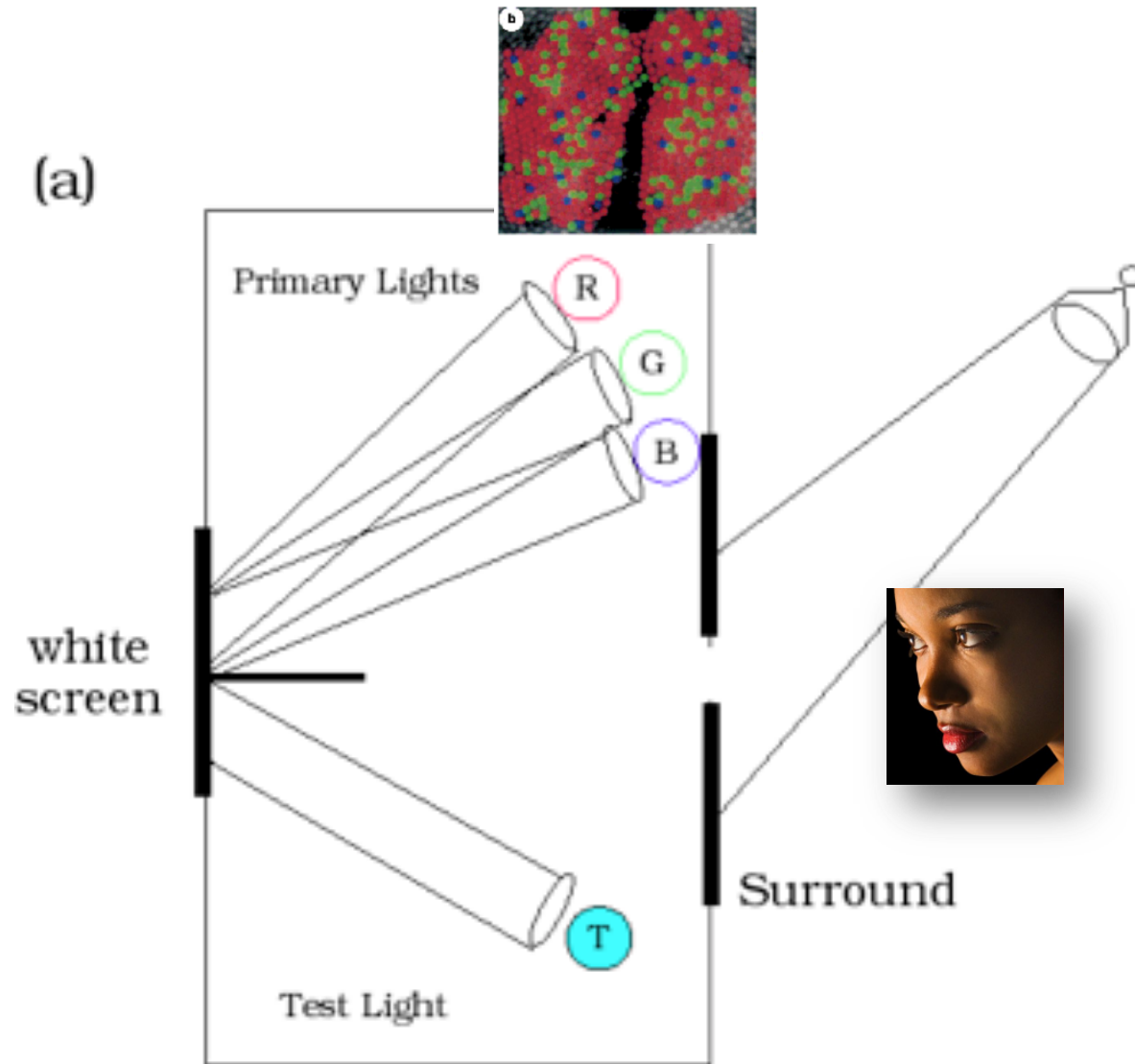
CMF and additivity





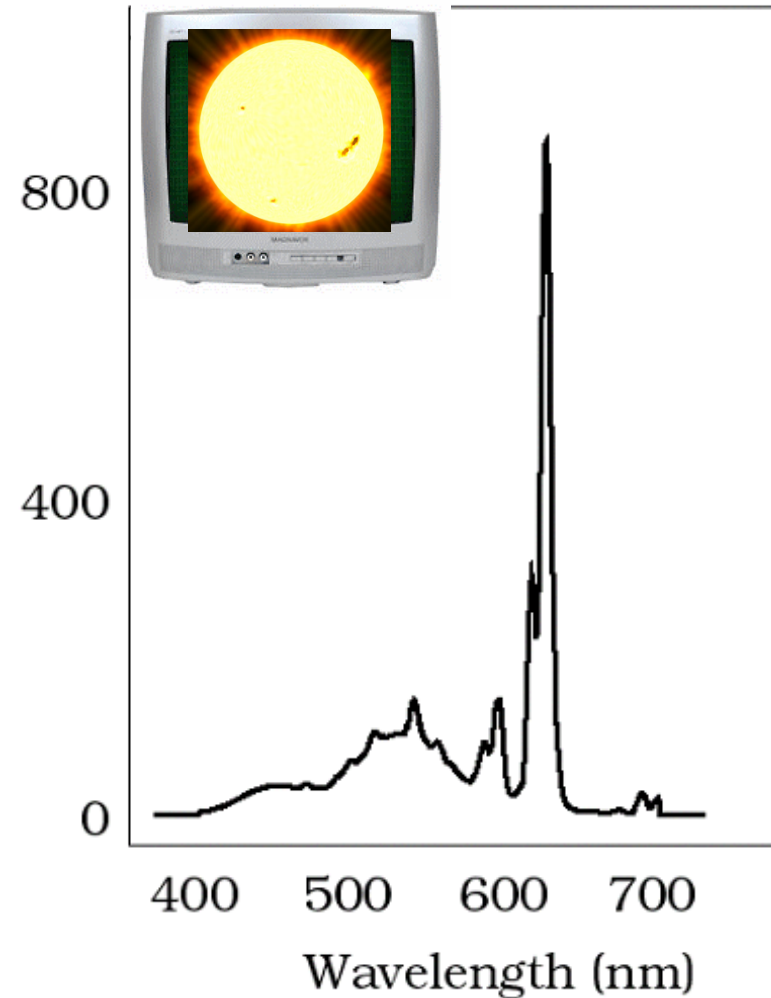
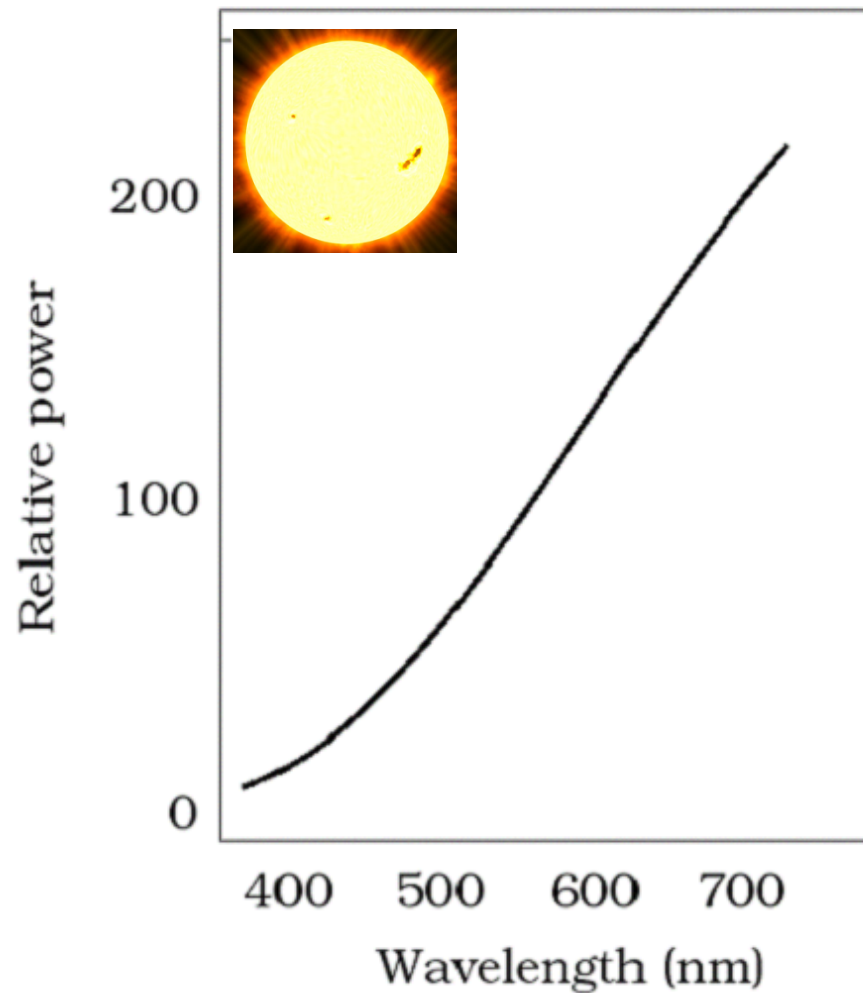


Cone color matching experiment (cone vision)



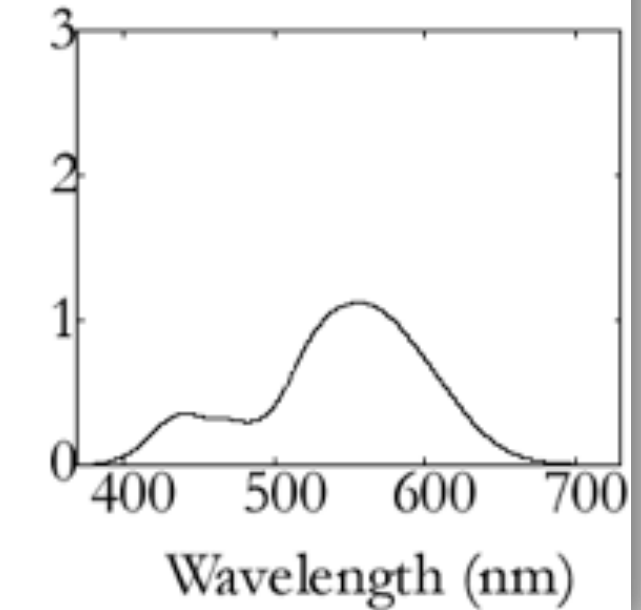
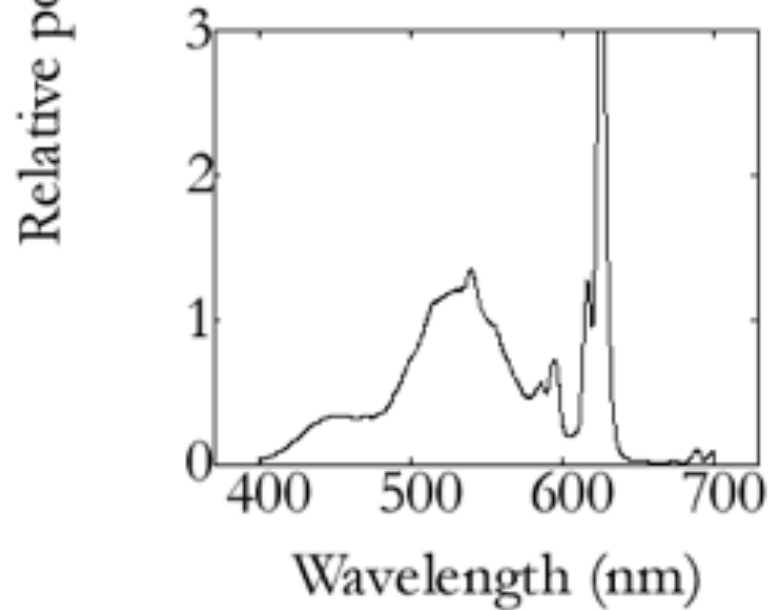
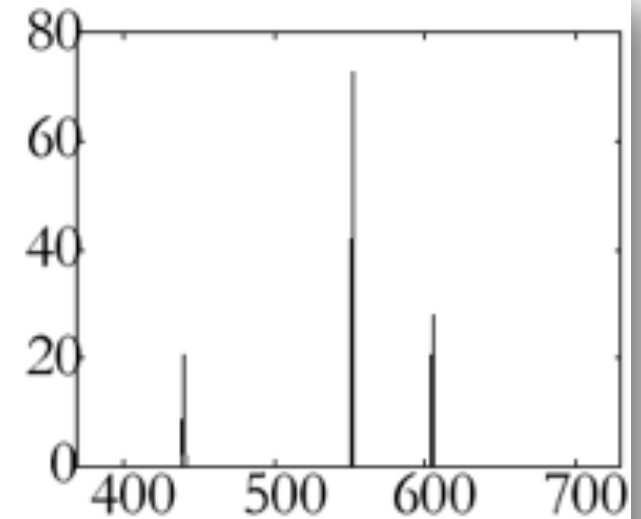
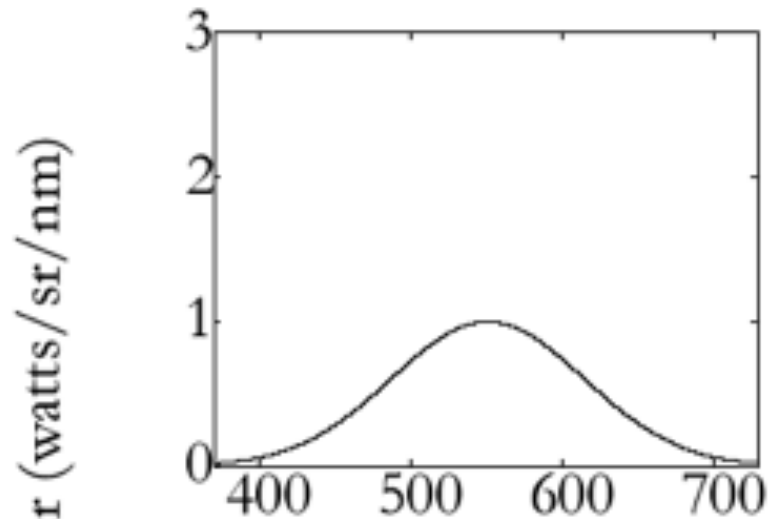
Metamerism

Color matching is an important illusion that is understood quantitatively

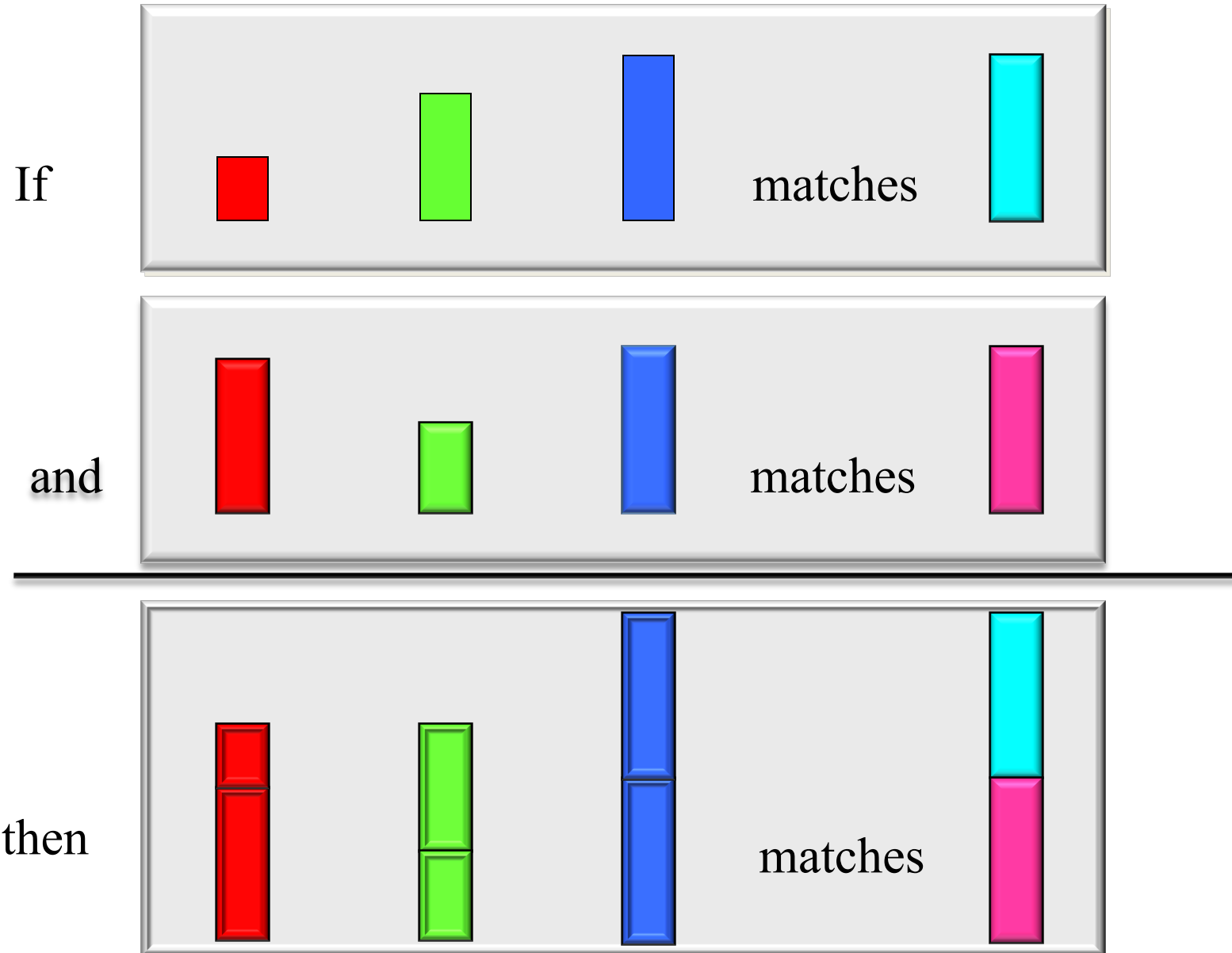


Metamerism is a big effect

These spectral power distributions appear the same color to the eye



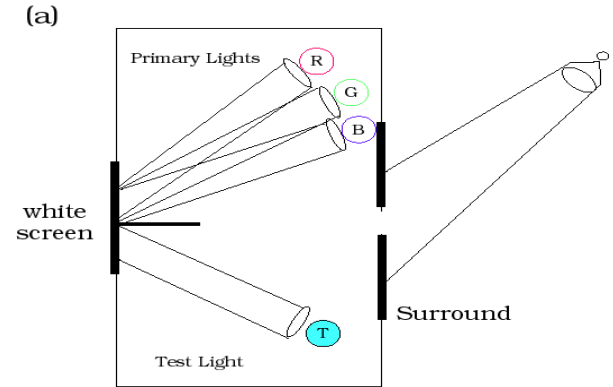
The color matching experiment is linear



Color matching experiment equation



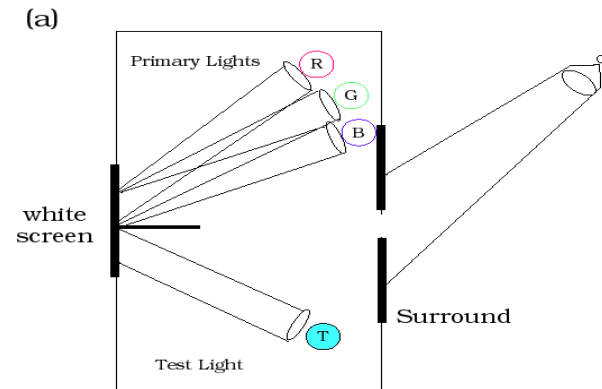
Grassmann



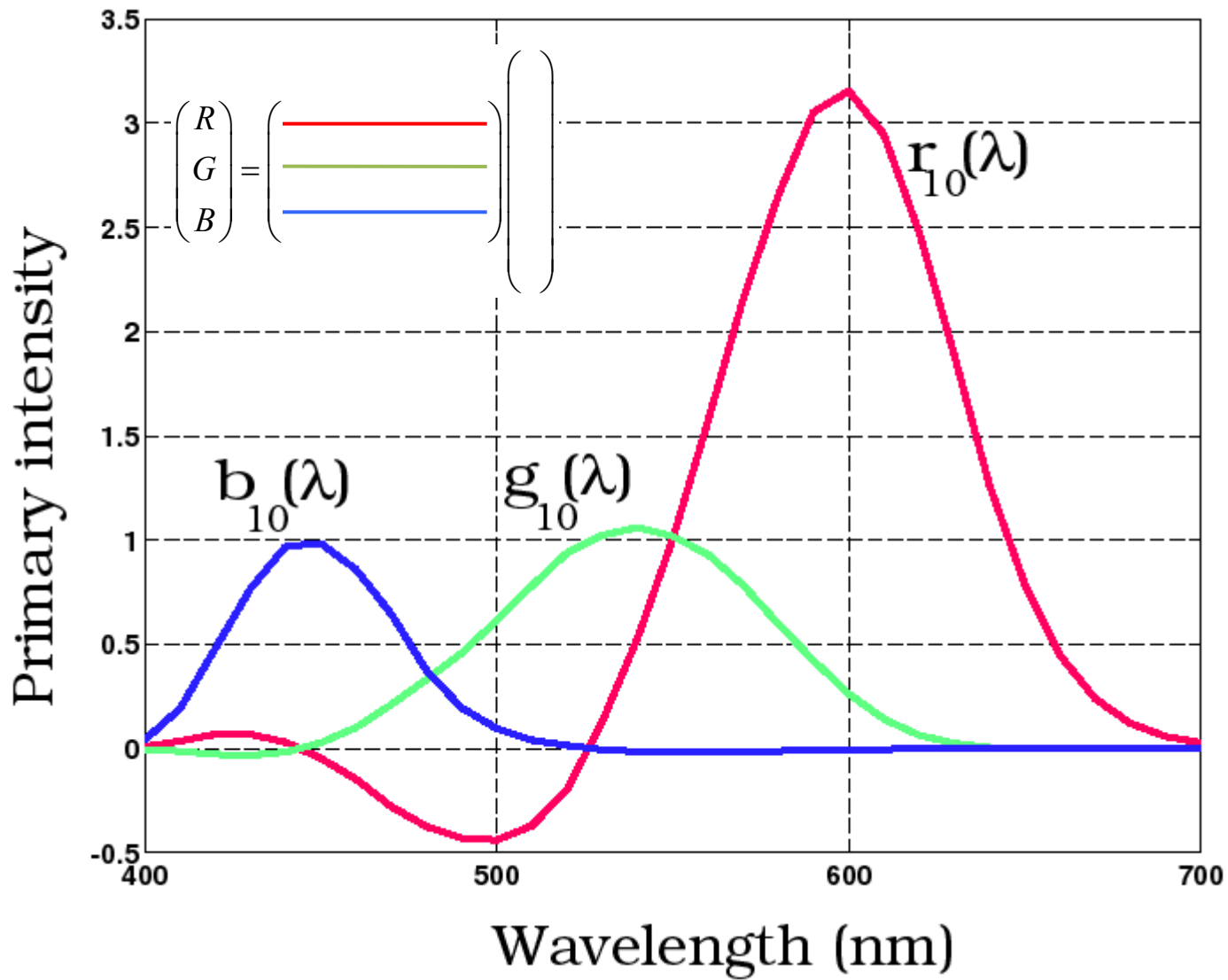
$$\begin{matrix} \text{Response} \\ \begin{pmatrix} R \\ G \\ B \end{pmatrix} \end{matrix} = \begin{matrix} \text{CIE RGB functions} \\ \begin{pmatrix} \text{red line} \\ \text{green line} \\ \text{blue line} \end{pmatrix} \end{matrix} \begin{pmatrix} \text{Test light SPD} \end{pmatrix}$$

Color matching experiment equation

$$\begin{array}{c} \text{Response} \\ \begin{pmatrix} r \\ g \\ b \end{pmatrix} \end{array} = \begin{array}{c} \text{CIE RGB functions} \\ \begin{matrix} 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \end{matrix} \\ \begin{pmatrix} \text{red bar} & r & \text{red bar} \\ \text{green bar} & g & \text{green bar} \\ \text{blue bar} & b & \text{blue bar} \end{pmatrix} \end{array} \begin{pmatrix} 0 \\ 0 \\ 0 \\ \dots \\ 1 \\ \dots \\ 0 \\ 0 \\ 0 \end{pmatrix} \begin{array}{c} \text{Test light} \\ \text{SPD} \end{array}$$



Behavioral color matching functions (CMFs; 10 deg)



Color matching functions

Metamer definition

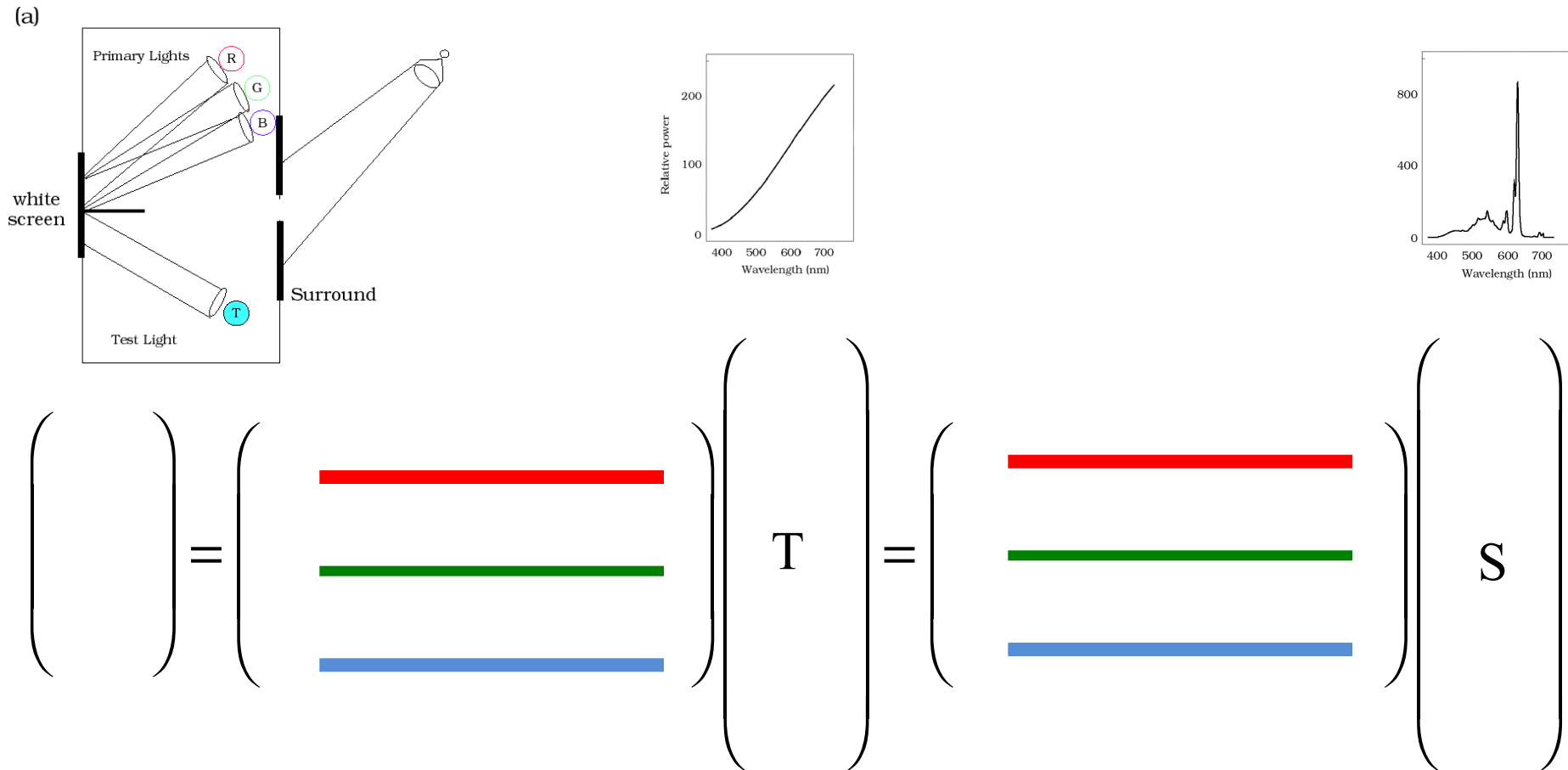
Uniqueness

CIE (1931) XYZ standard



CMFs predict appearance matches

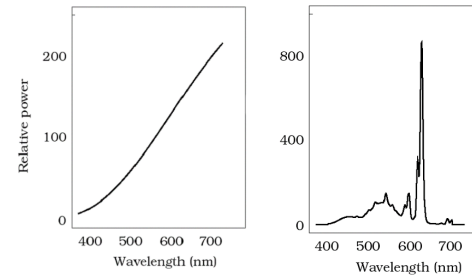
Two SPDs are **metamers** when they differ physically but are matched in the color-matching experiment



Metamer differences: CMF null space

Two SPDs are **metamers** when they differ physically but are matched in the color-matching experiment

Metamer differences always have negative values somewhere in the spectrum; otherwise the difference would produce a signal in the L,M,S cones

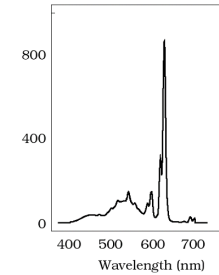
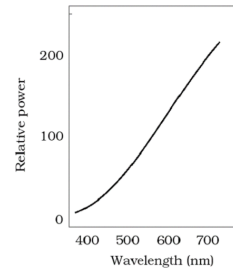


$$0 = \left(\begin{array}{c} \text{red bar} \\ \text{green bar} \\ \text{blue bar} \end{array} \right) \left\{ \left(\begin{array}{c} T \\ \vdots \end{array} \right) - \left(\begin{array}{c} S \\ \vdots \end{array} \right) \right\}$$

(all positive)

CMFs: A uniqueness theorem

Any invertible linear transformation, L , of the CMFs
predicts the same metamers



Invertible 3x3

$$\begin{pmatrix} L \end{pmatrix} \begin{pmatrix} \text{Red bar} \\ \text{Green bar} \\ \text{Blue bar} \end{pmatrix} \begin{pmatrix} T \end{pmatrix} = \begin{pmatrix} L \end{pmatrix} \begin{pmatrix} \text{Red bar} \\ \text{Green bar} \\ \text{Blue bar} \end{pmatrix} \begin{pmatrix} S \end{pmatrix}$$

CMFs: A uniqueness theorem

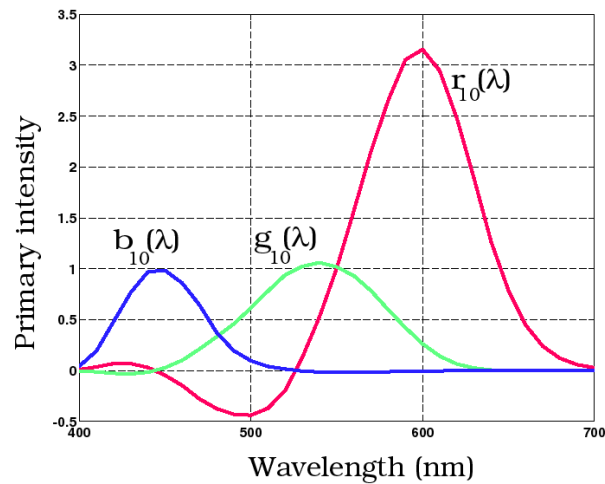
Different choices of primaries produce different CMFs

Related by a linear transformation (see **Foundations of Vision** for proof)

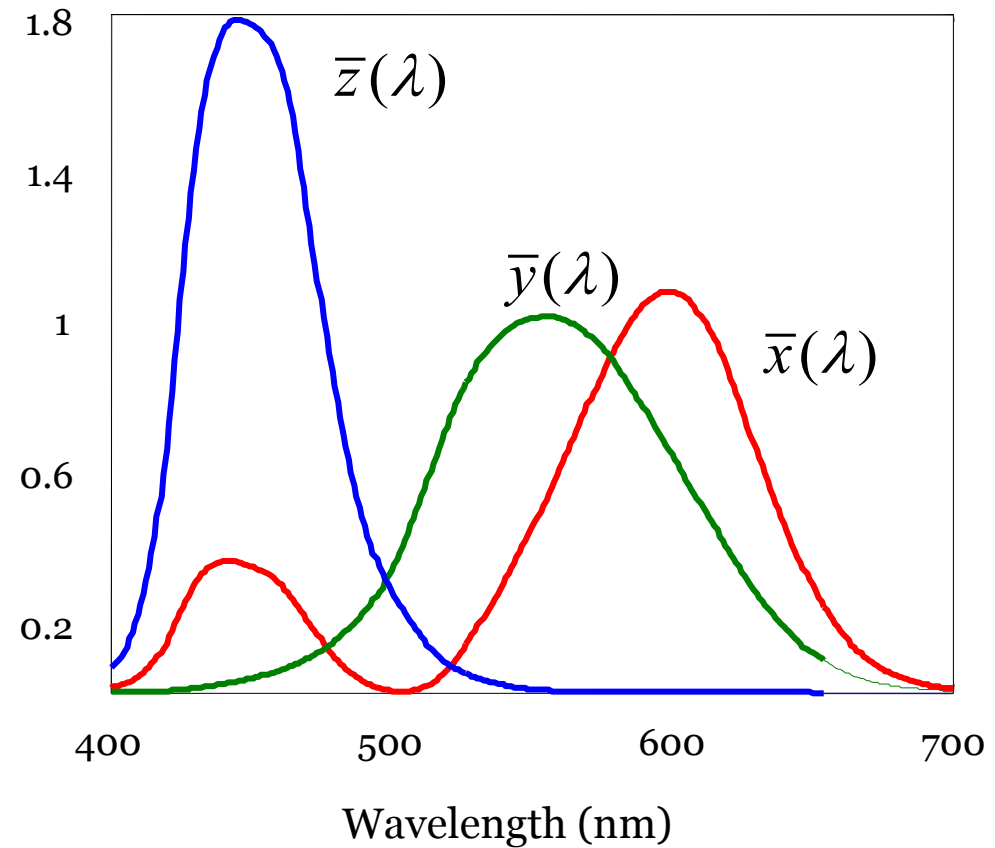
The diagram illustrates the relationship between two Color Matching Functions (CMFs) via a linear transformation. On the left, a bracket groups the terms L and a 3x3 matrix of colored bars (red, green, blue). An arrow labeled "Invertible 3x3" points to this matrix. This is followed by a vertical vector T . An equals sign follows. On the right, the same L is multiplied by a 3x3 matrix of colored bars (red, green, blue), which is then multiplied by a vertical vector S . A bracket under the left side is labeled "New CMF".

$$\underbrace{\left(L \begin{pmatrix} \text{red bar} \\ \text{green bar} \\ \text{blue bar} \end{pmatrix} \right)}_{\text{New CMF}} T = L \begin{pmatrix} \text{red bar} \\ \text{green bar} \\ \text{blue bar} \end{pmatrix} S$$

The CIE (1931) XYZ standard CMFs



CIE (1931) 10 deg XYZ functions



The CIE (1931) XYZ standard CMFs

You must specify radiance
using **energy**, not photons

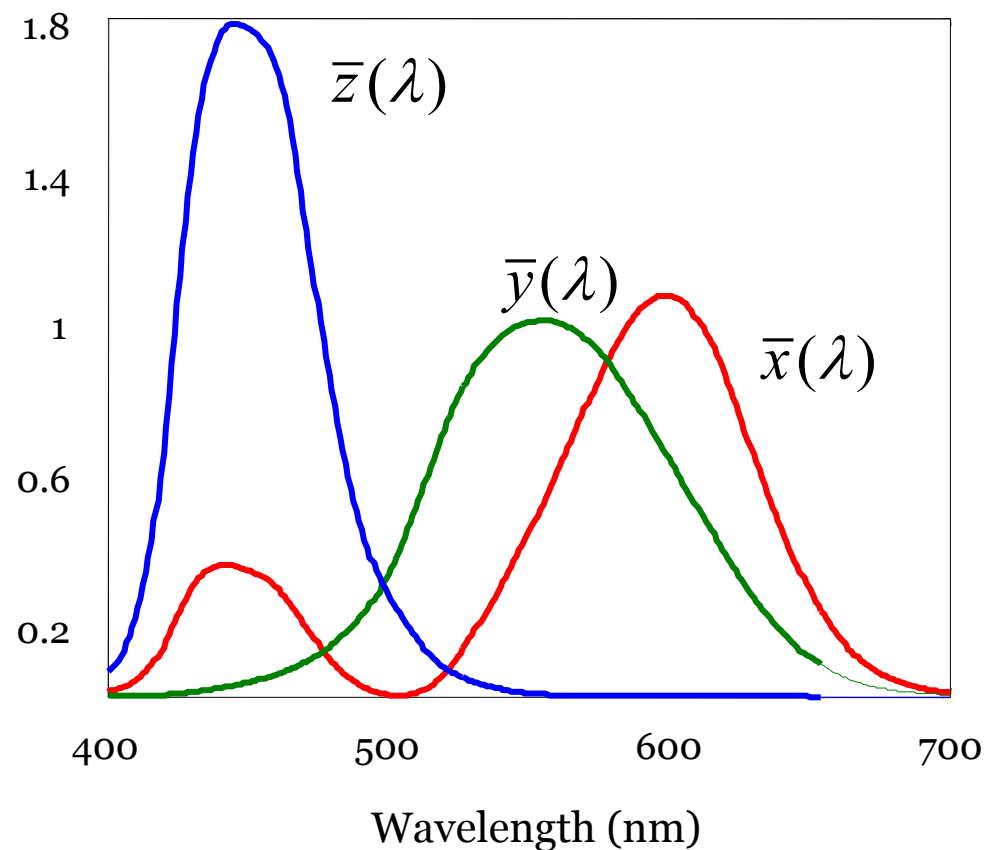
Radiance

$$X = \sum_{\lambda} \bar{x}(\lambda) t(\lambda) d\lambda$$

$$Y = \sum_{\lambda} \bar{y}(\lambda) t(\lambda) d\lambda$$

$$Z = \sum_{\lambda} \bar{z}(\lambda) t(\lambda) d\lambda$$

CIE (1931) 10 deg XYZ functions



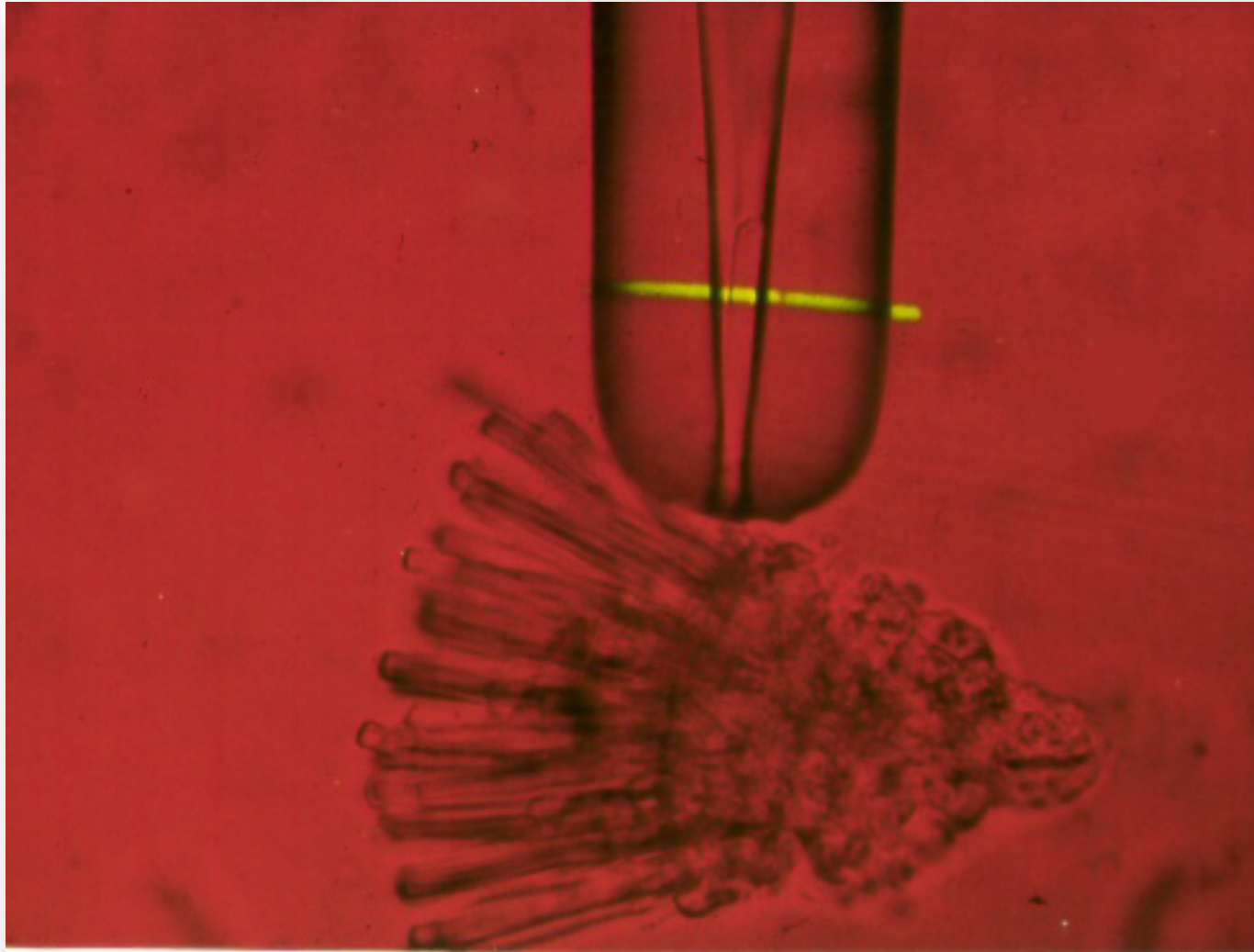
Physiology and color-matching

- Relating cone responses to color matches
- Static nonlinearities



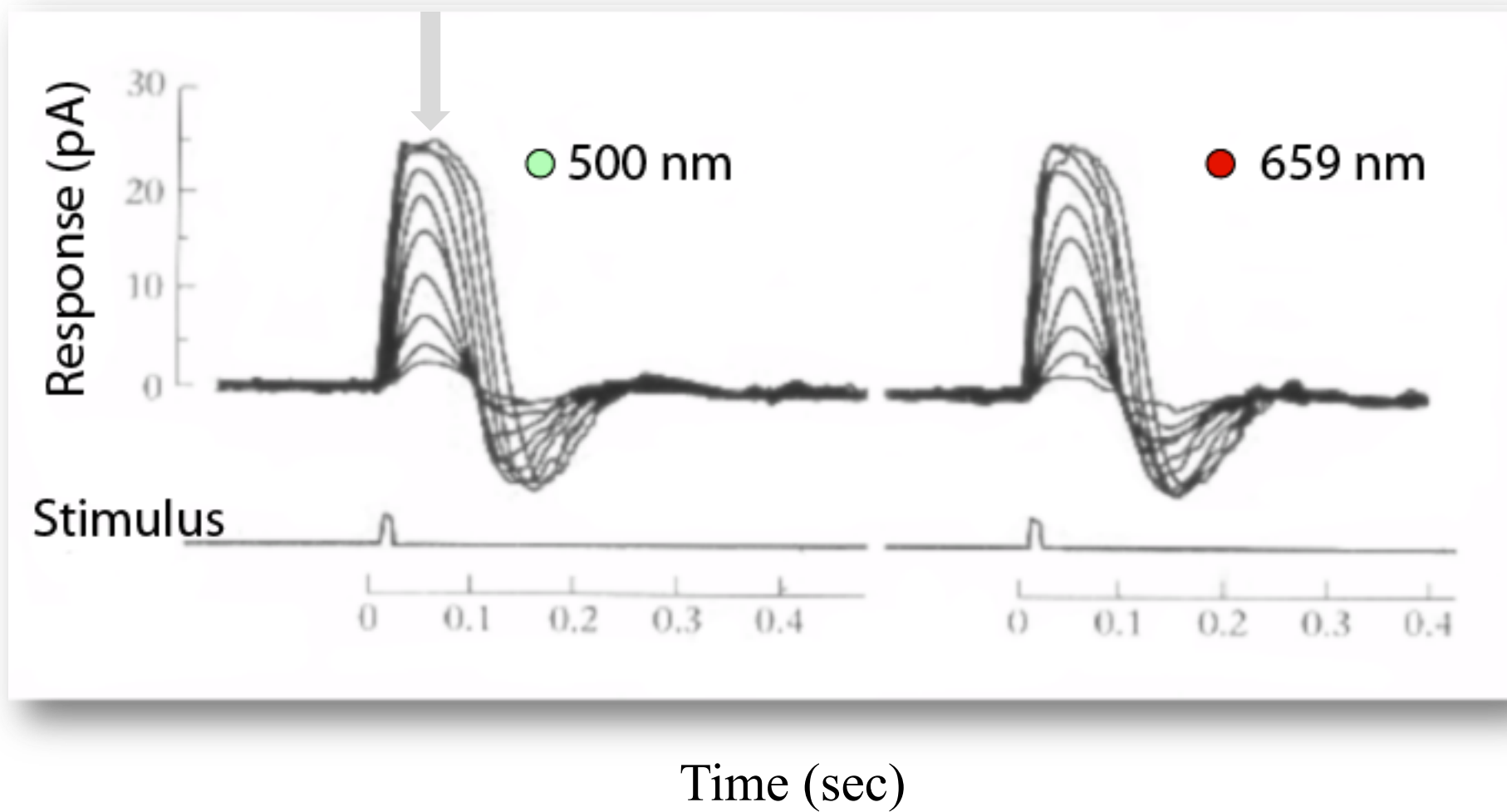
Single cone photocurrent measurements

(Schnapf, Baylor et al., 1986)



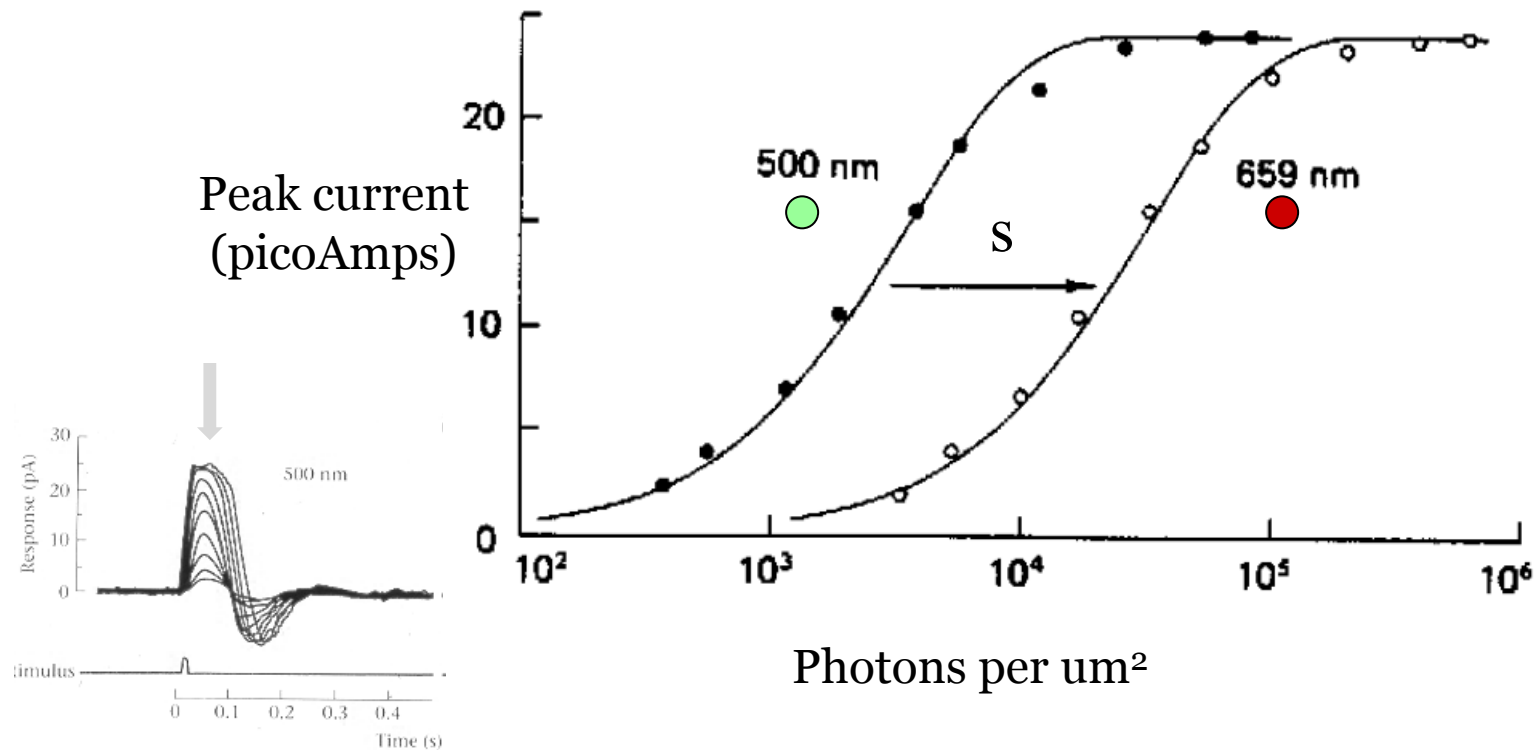
Principle of univariance (Rushton)

Cone photocurrent using stimuli with different wavelengths



Spectral sensitivity of nonlinear systems

$$N(I_{500}) = N(sI_{659})$$

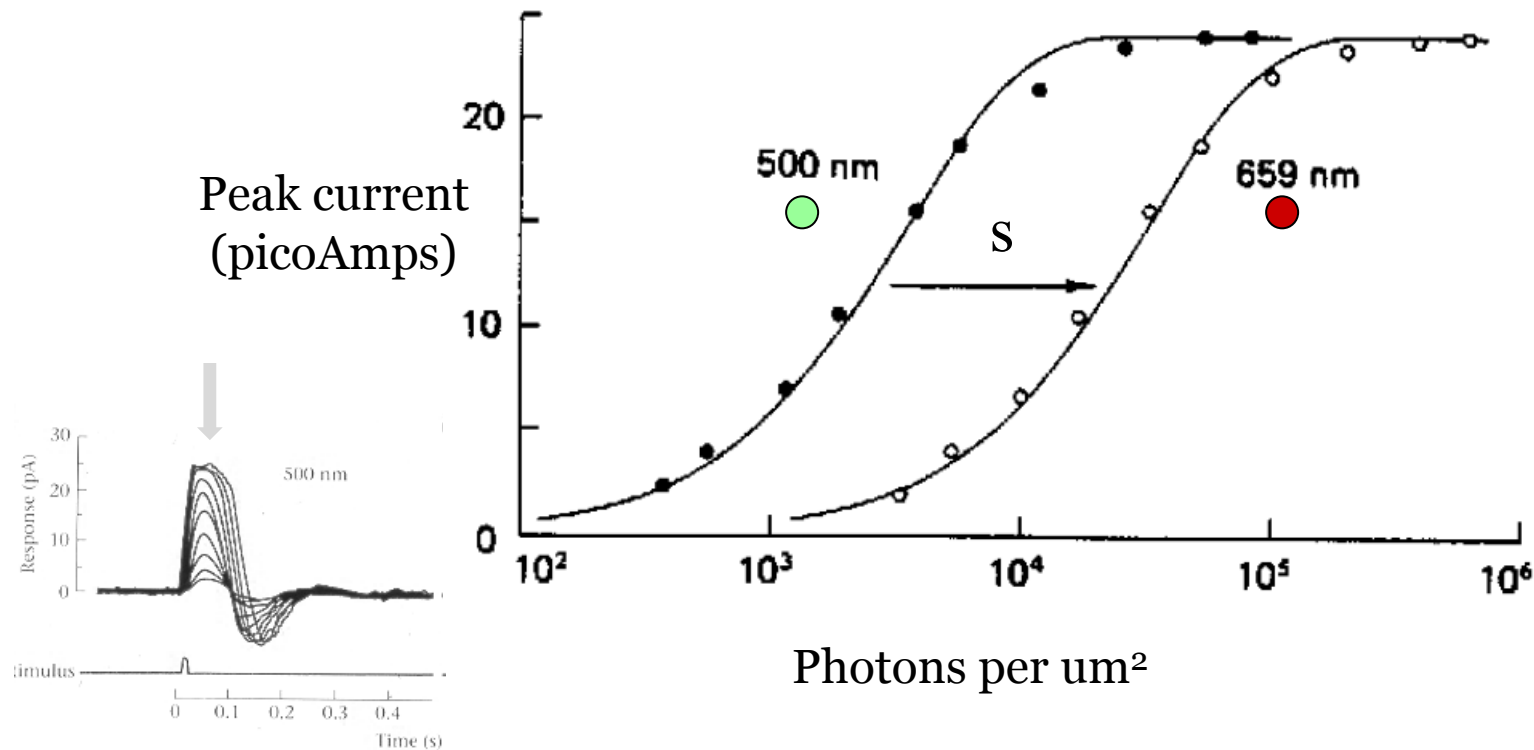


Spectral sensitivity of nonlinear systems

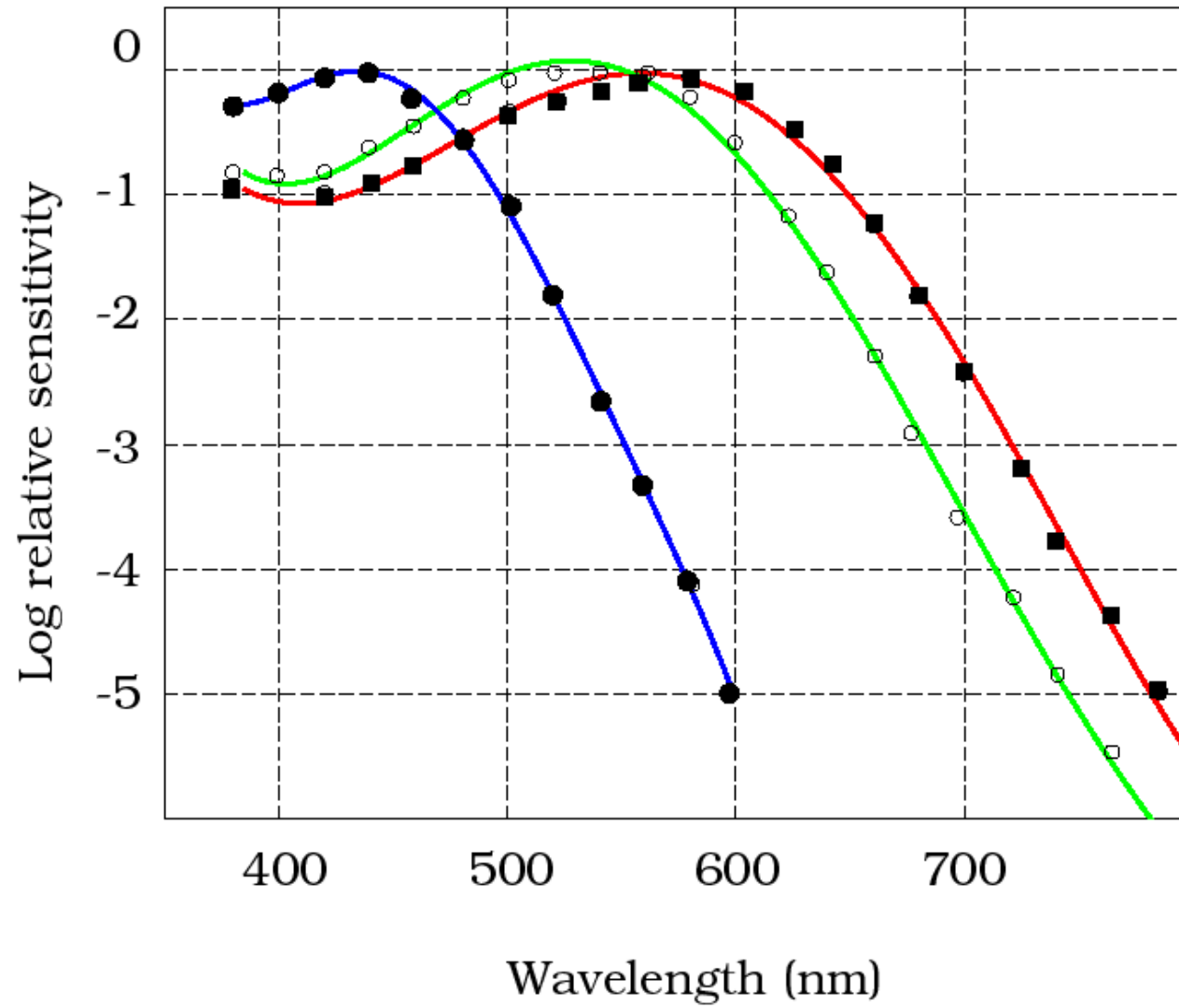
Static nonlinearity:

$$N(I_{500}) = N(sI_{659})$$

$$N(I_{500} + sI_{659}) = N(2I_{500})$$

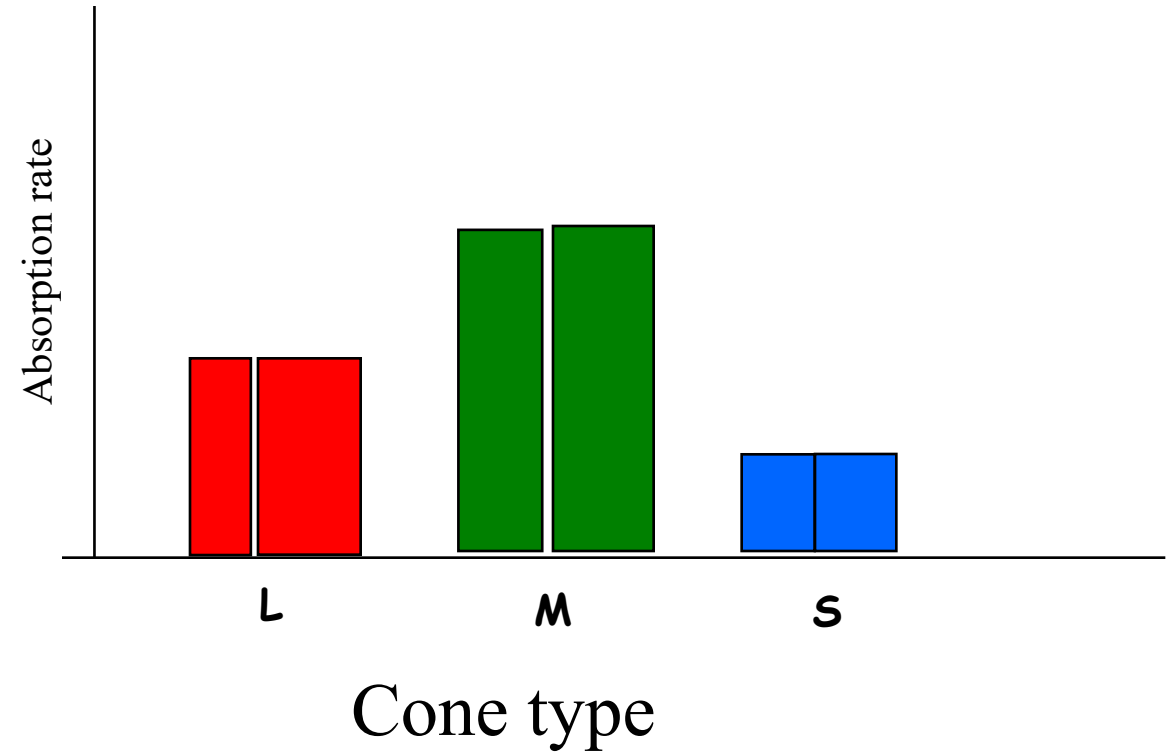
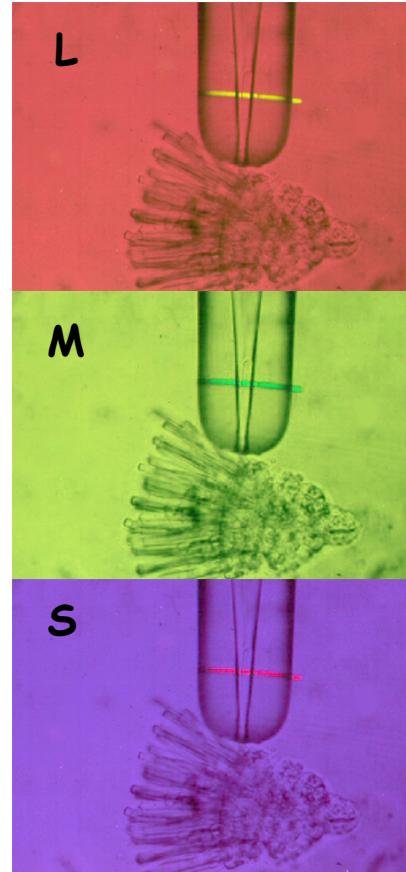
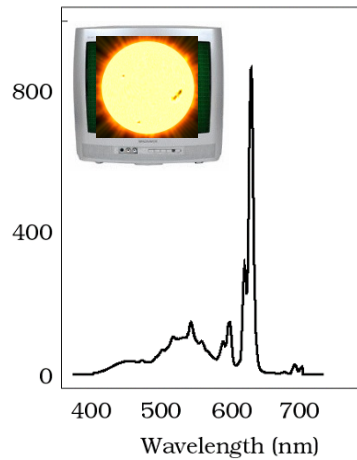
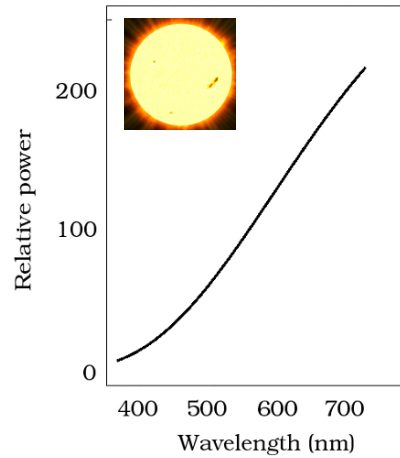


There are three cone wavelength responsivity functions



Stimuli causing equal cone absorptions match perceptually

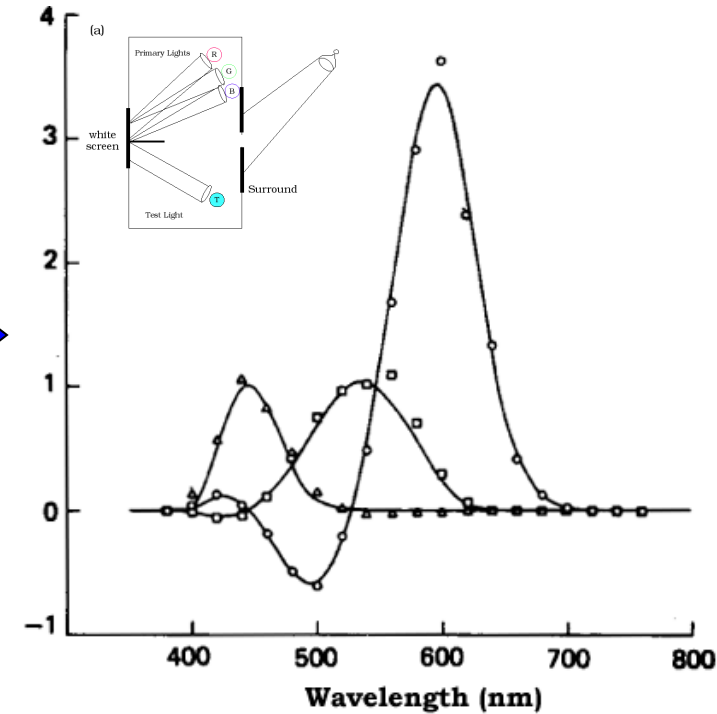
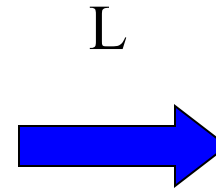
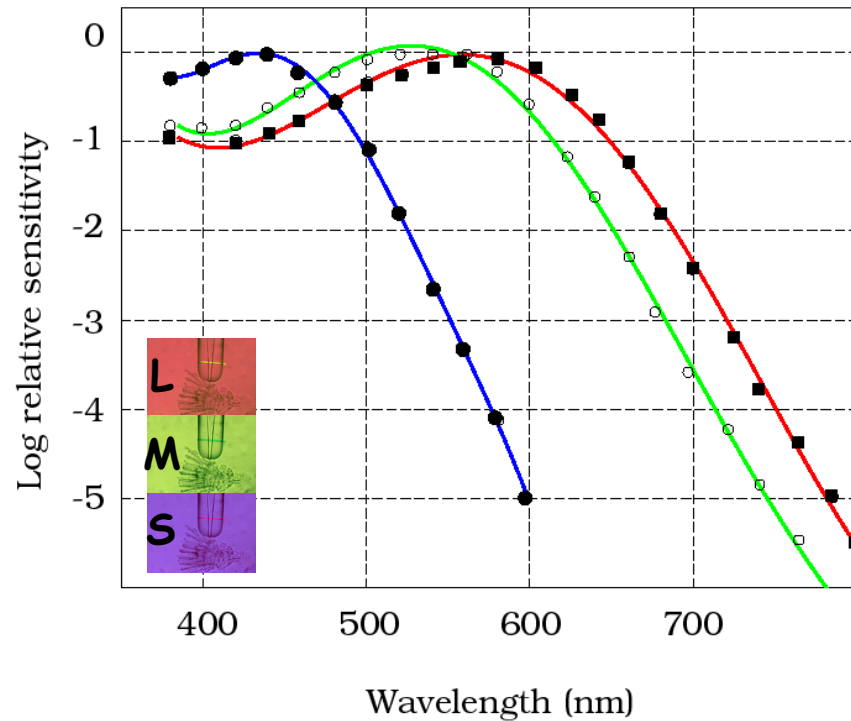
What about the rods?



The cone responsivities predict the CMFs

Recall the point about all CMFs being unique up to a linear transformation

The relationship between the cones and the XYZ functions is a linear transform



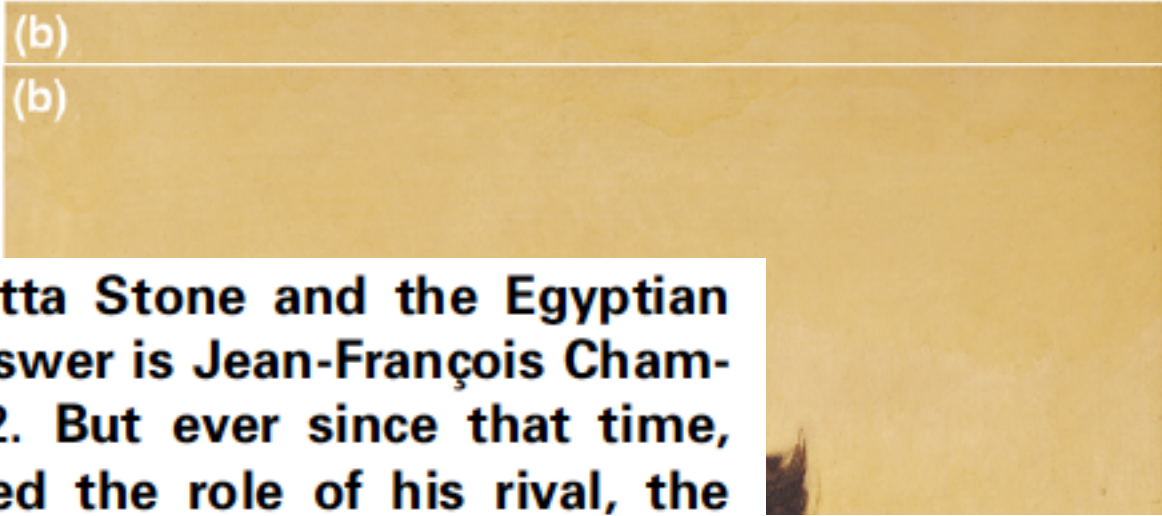
Historical notes





(a)

(a)



(b)

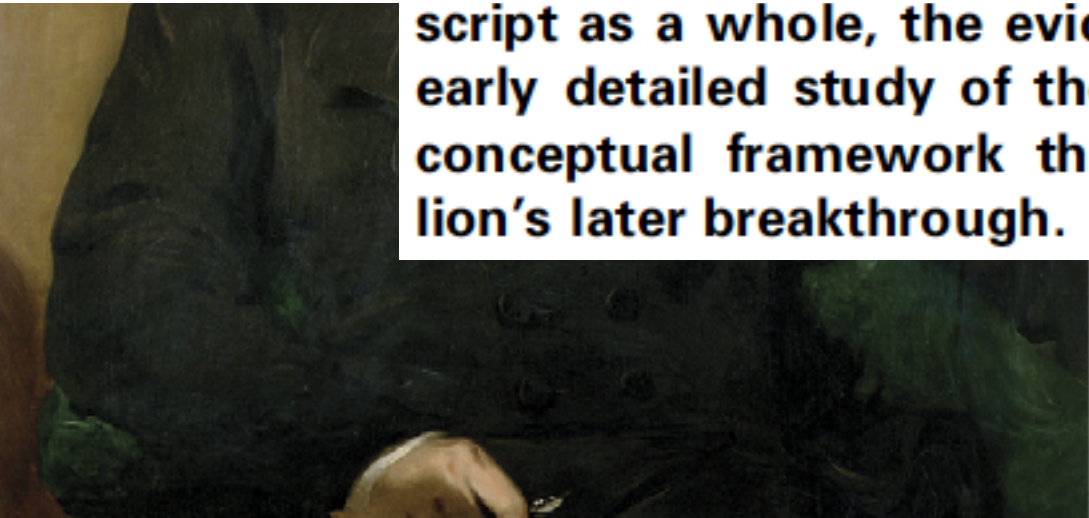
(b)

Who deciphered the Rosetta Stone and the Egyptian hieroglyphs? The usual answer is Jean-François Champollion, beginning in 1822. But ever since that time, Egyptologists have debated the role of his rival, the

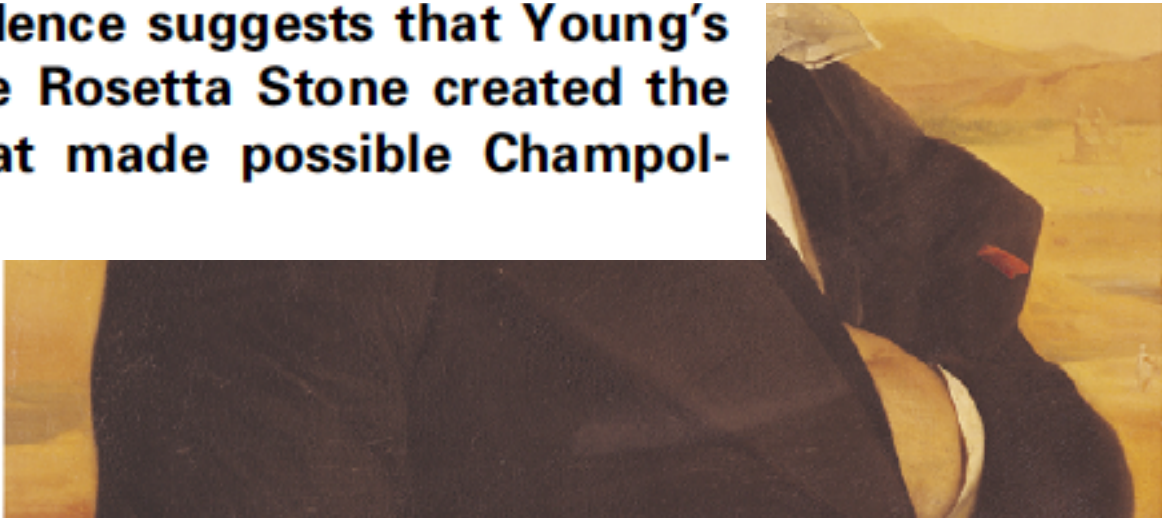
Thomas Young and the Rosetta Stone

Andrew Robinson

13 Lonsdale Square, London N1 1EN, United Kingdom



script as a whole, the evidence suggests that Young's early detailed study of the Rosetta Stone created the conceptual framework that made possible Champollion's later breakthrough.





Thomas Young (1802)
On the theory of lights
and colours.
Philosophical
Transactions of the
Royal Society 92, 12-
48.

“....this paper contains nothing which deserves the name, either of experiment or of discovery, and as it is, in fact, destitute of every species of merit....”

“We now dismiss, for the present, the feeble lucubrations of this author, in which we have searched without success for some traces of learning, acuteness, and ingenuity, that might compensate his evident deficiency in the powers of solid thinking, calm and patient investigation....”

Henry Brougham in Edinburgh Review, an ardent admirer of Newton, criticizing Thomas Young's Bakerian Lectures.

Original color-matching technology

(Clerk Maxwell, Image from John Mollon, Cambridge)

Color-mixing was done by spinning a top rapidly, rather than by mixing lights.

In the course of his 1855 paper on the perception of colour, Maxwell proposed that if three black-and-white photographs of a scene were taken through red, green and blue filters, and transparent prints of the images were projected onto a screen using three projectors equipped with similar filters, when superimposed on the screen the result would be perceived by the human eye as a complete reproduction of all the colours in the scene. (From Wikipedia)

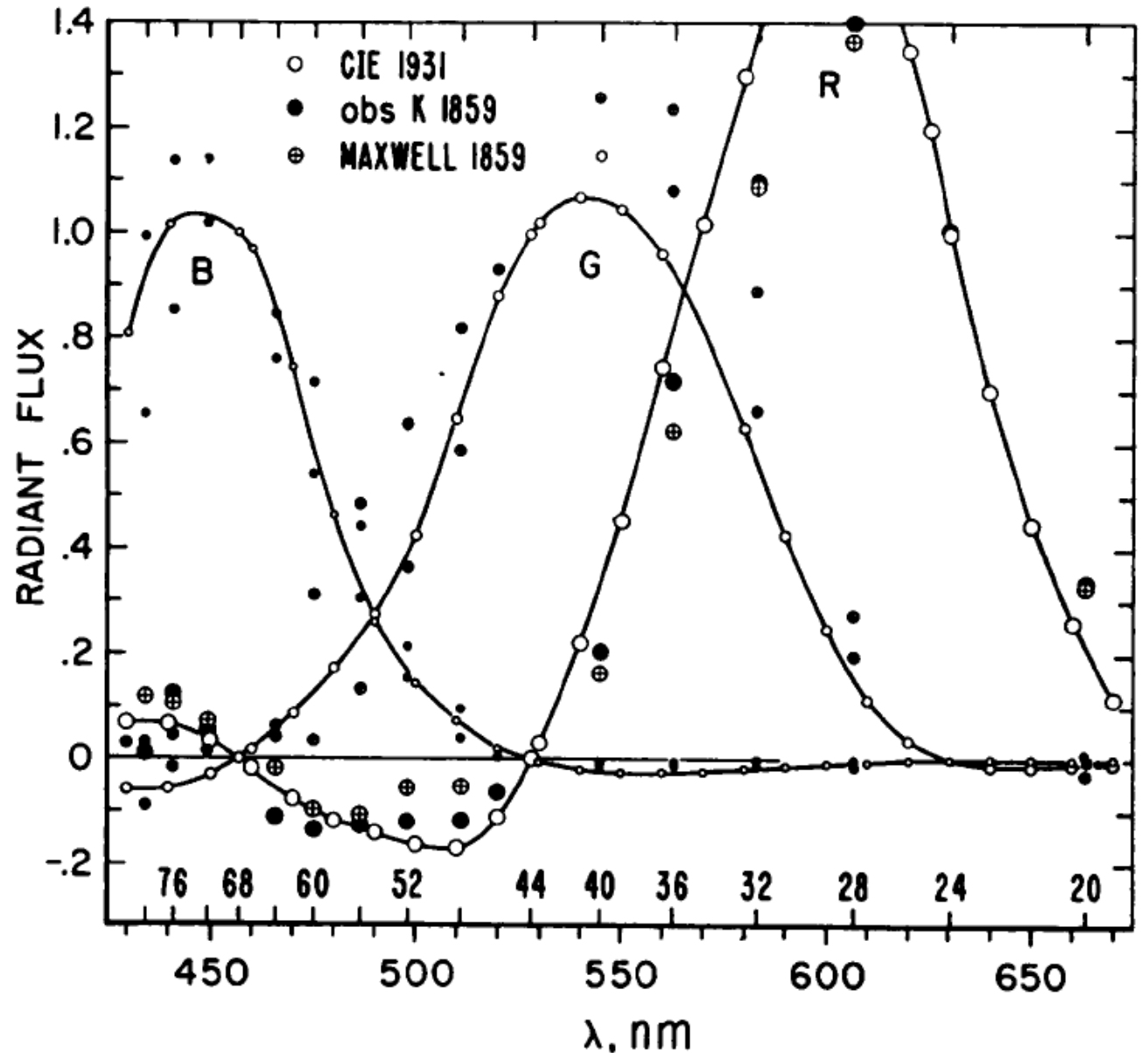


Figure 1.19 The color-mixing top of James Clerk Maxwell. The instrument survived in the collection of the Cavendish Laboratory, Cambridge. This photograph was taken in 1982. (Copyright: Department of Experimental Psychology, Cambridge University, reproduced with permission.)

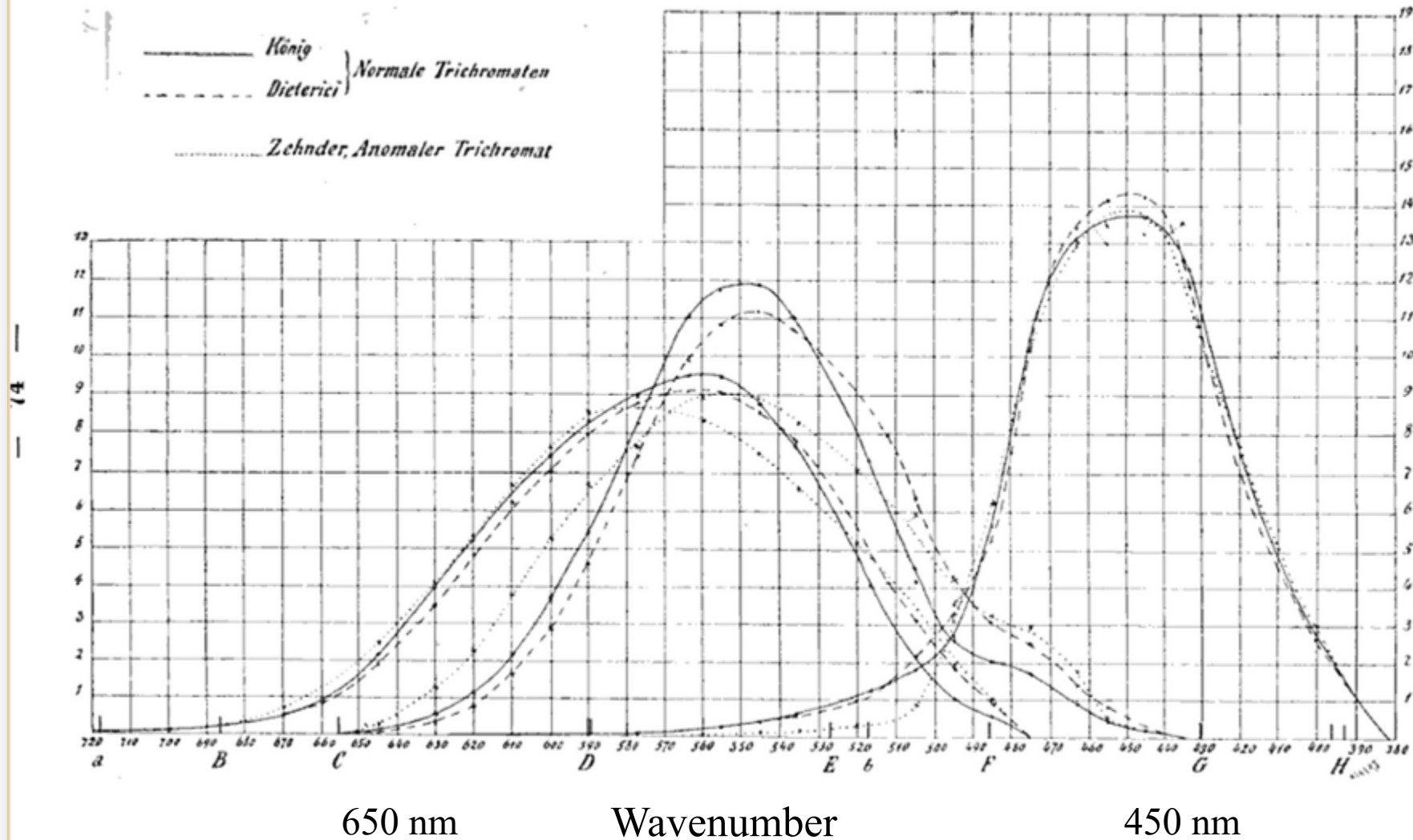
JC Maxwell was the first to measure the color-matching functions

Observer K – JCM's spouse
Maxwell
Comparison with 1931

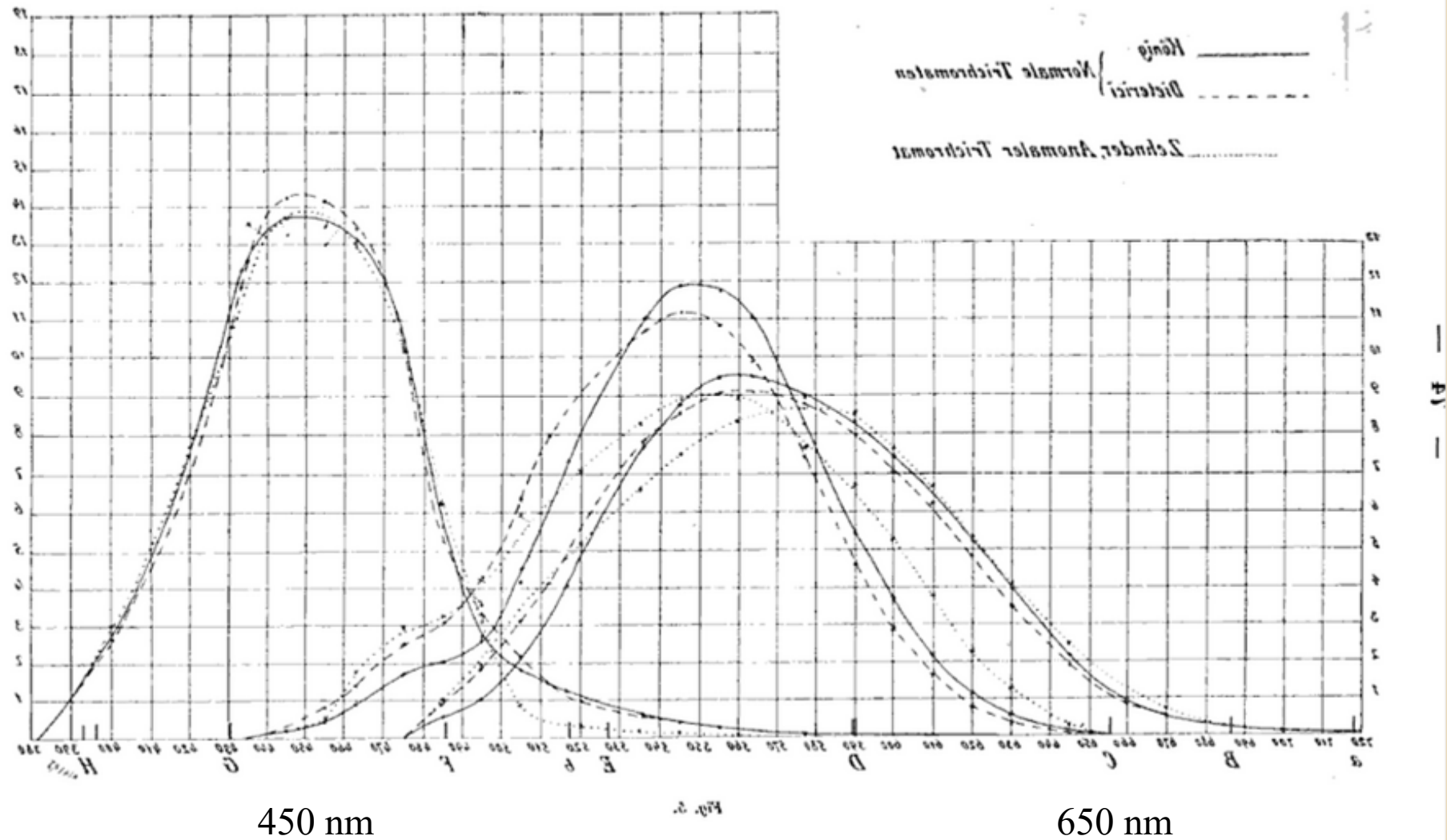
(From Judd, PNAS)



Koenig and Dieterici (1892) – Estimated cone absorptions

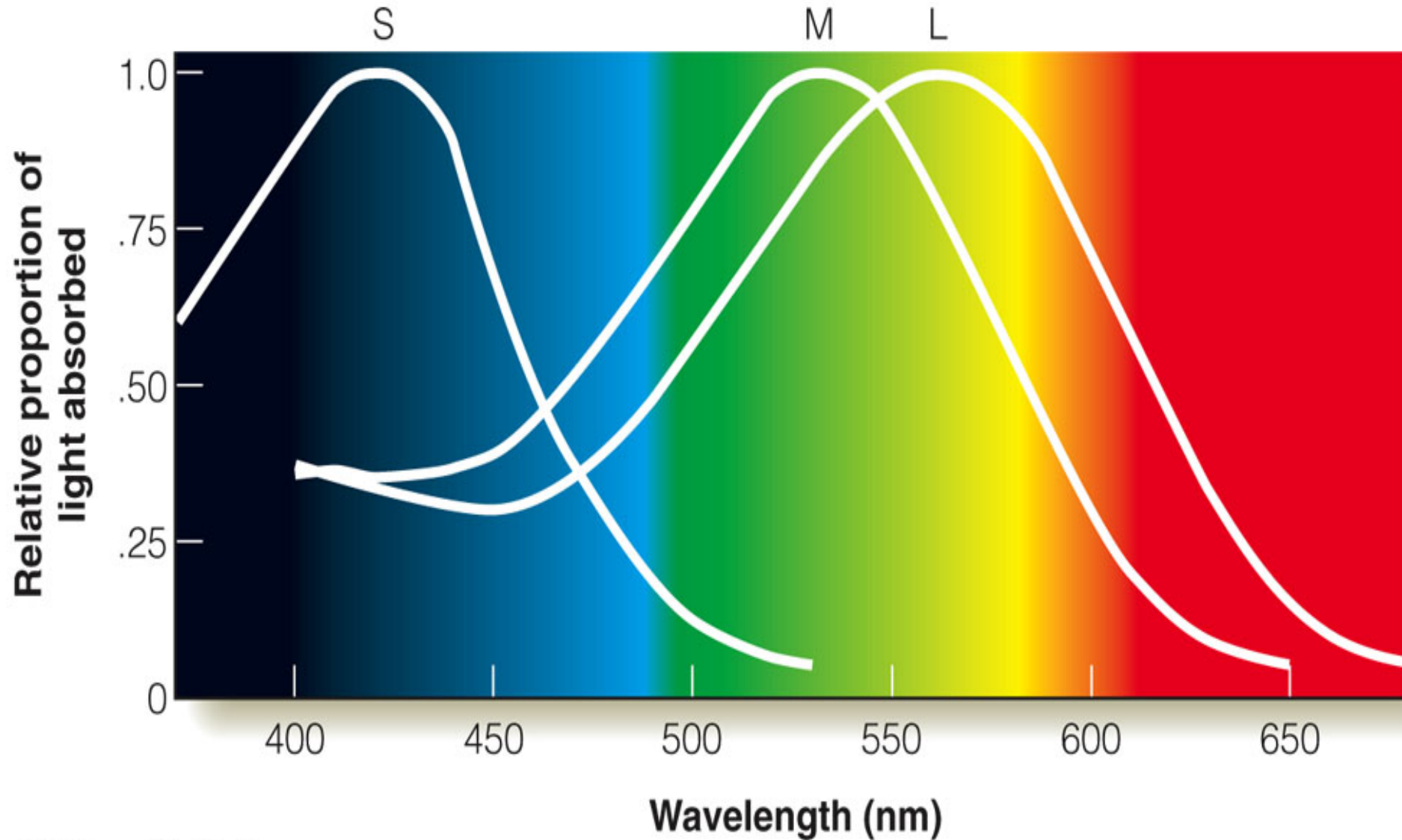


Koenig and Dieterici (1892) – Estimated cone absorptions



The cone response functions predict color matching

Modern
estimates

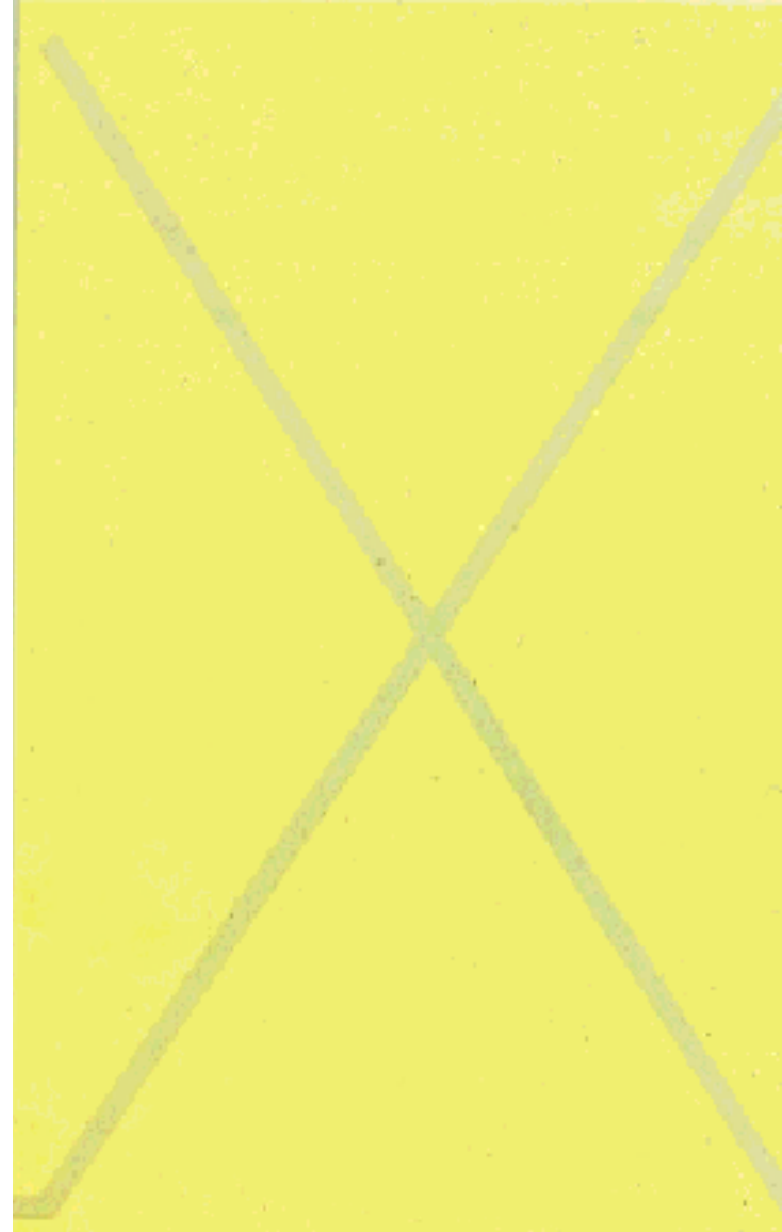
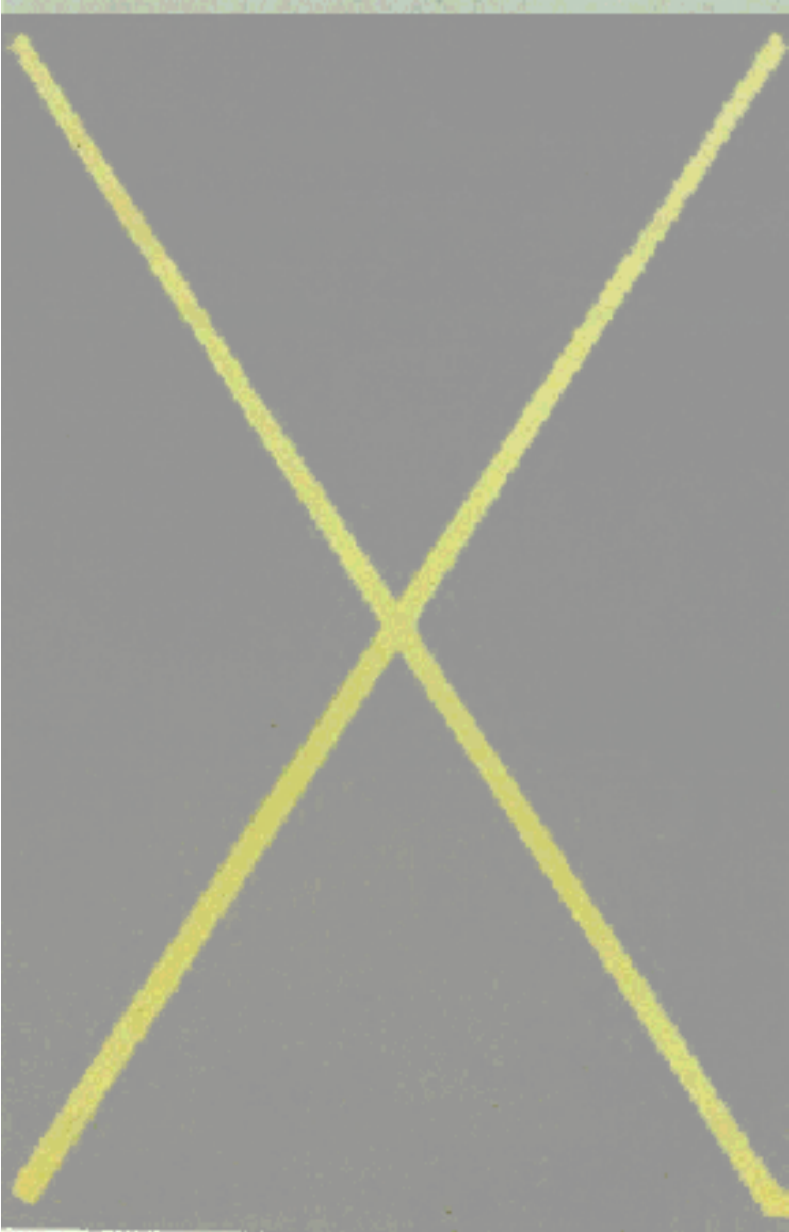


Color appearance: More than matching

Context
History

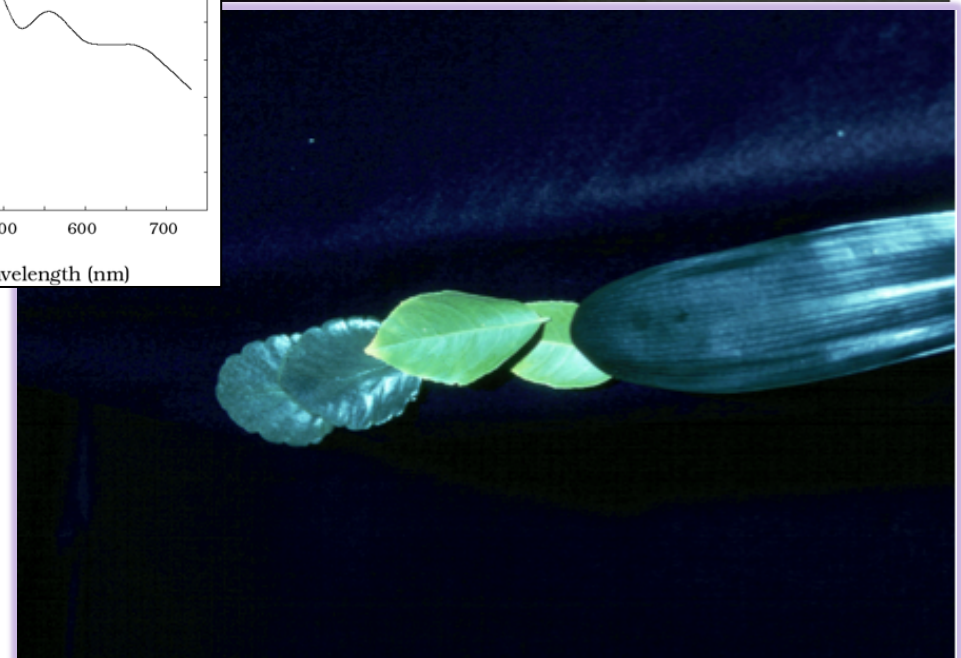
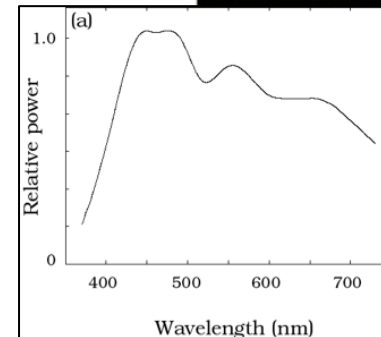
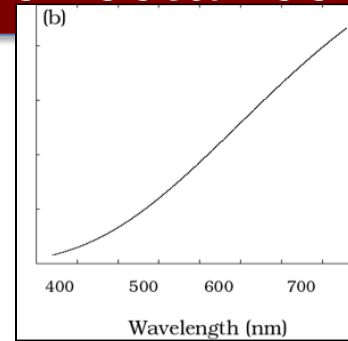


Matching does not predict appearance



Scene radiance depends on reflectance and illumination

- People want to recognize the object – hence estimate reflectance
- The visual system interprets color in a way that accounts for the spectral properties of the illuminant



Color appearance and context



. . . passing then into another place illuminated by sunlight, if one looks through the door of the room, the objects that are lit by candlelight will appear tinted reddish-yellow in comparison with those lit by the sun and seen concurrently. One cannot appreciate this when he is in the candle-lit chamber.

(De La Hire, 1694/1730)

Even simple
judgments – such
as lightness -
depend on
interpreting the
nature of the
lighting

(Anderson and Winawer,
Nature, 2005)





johnsadowski.com





johnsadowski.com

END

Artistic rendering – which one do you like better?

Notice that the hole and 2nd prism is missing!

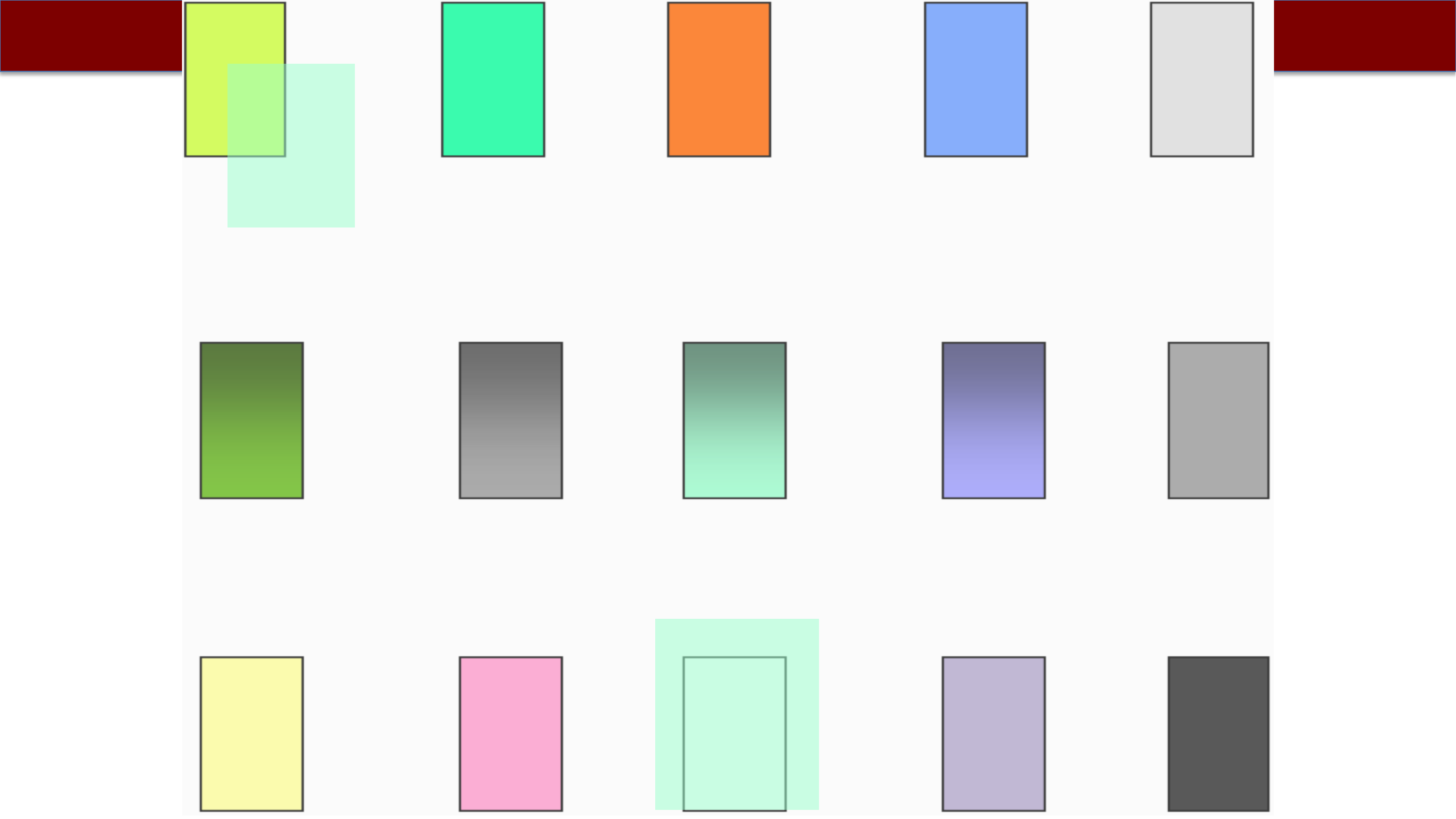
And what is that dude doing there in the background?

And where is the lens?

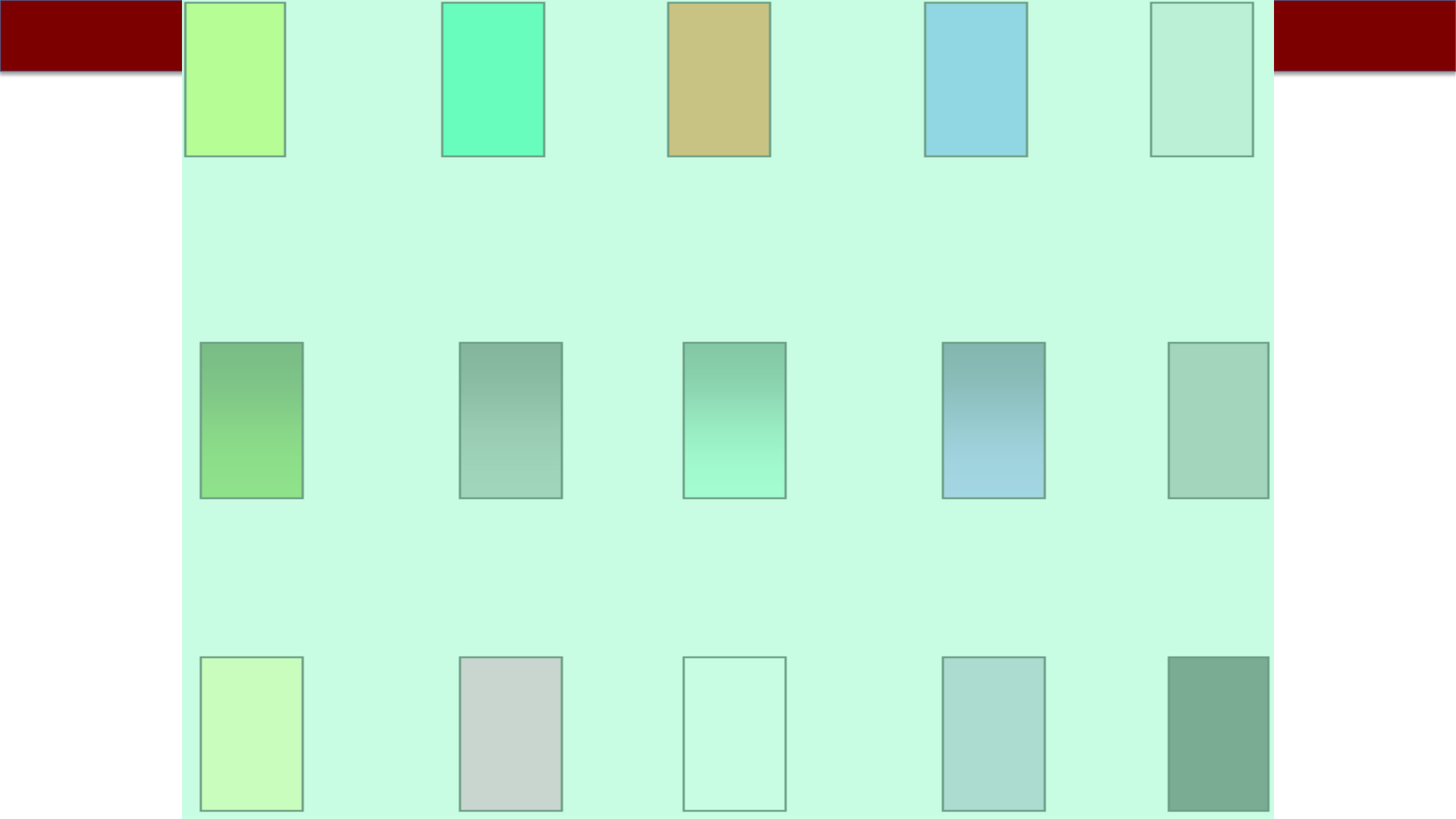


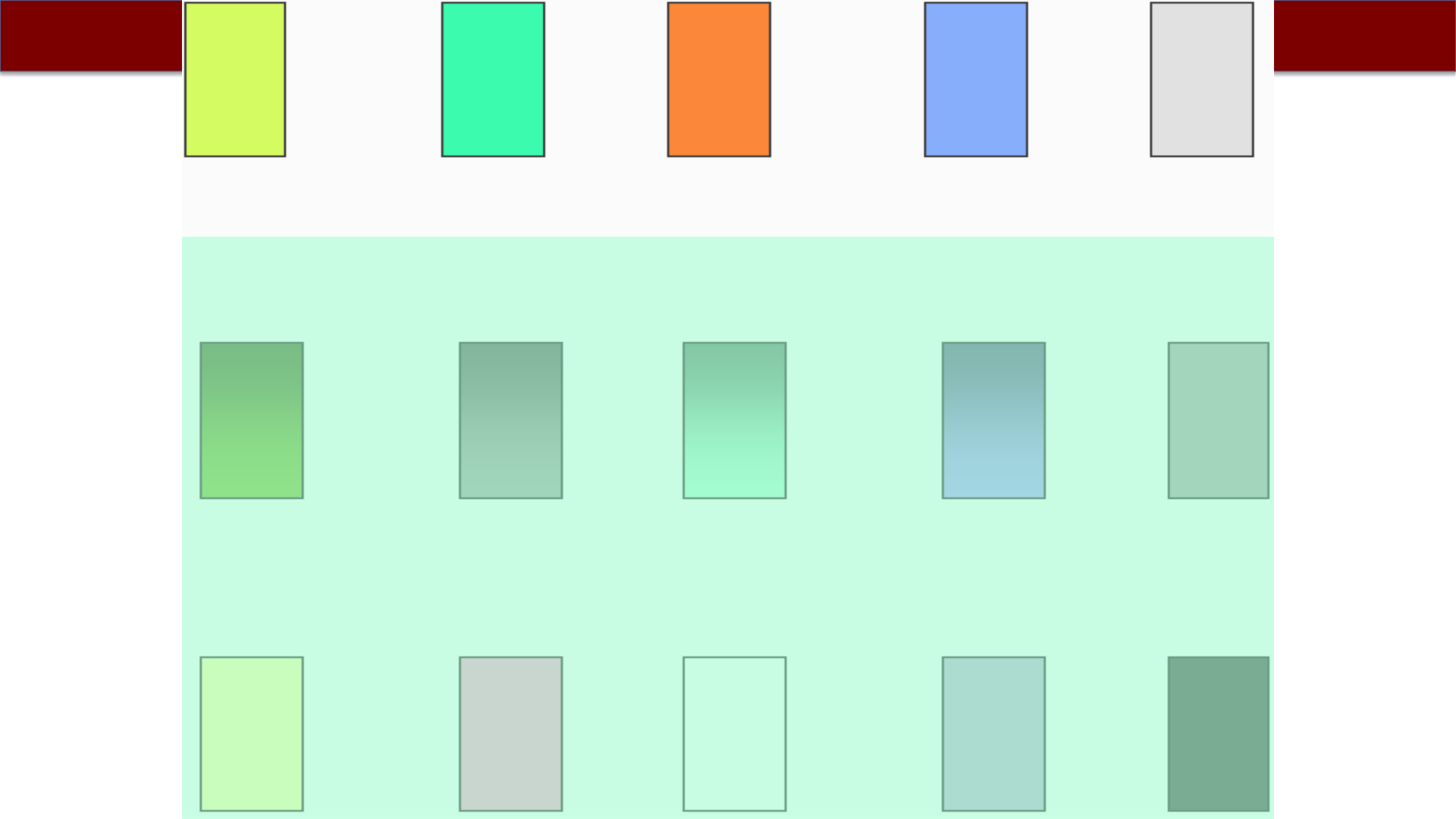
The fundamental components of light

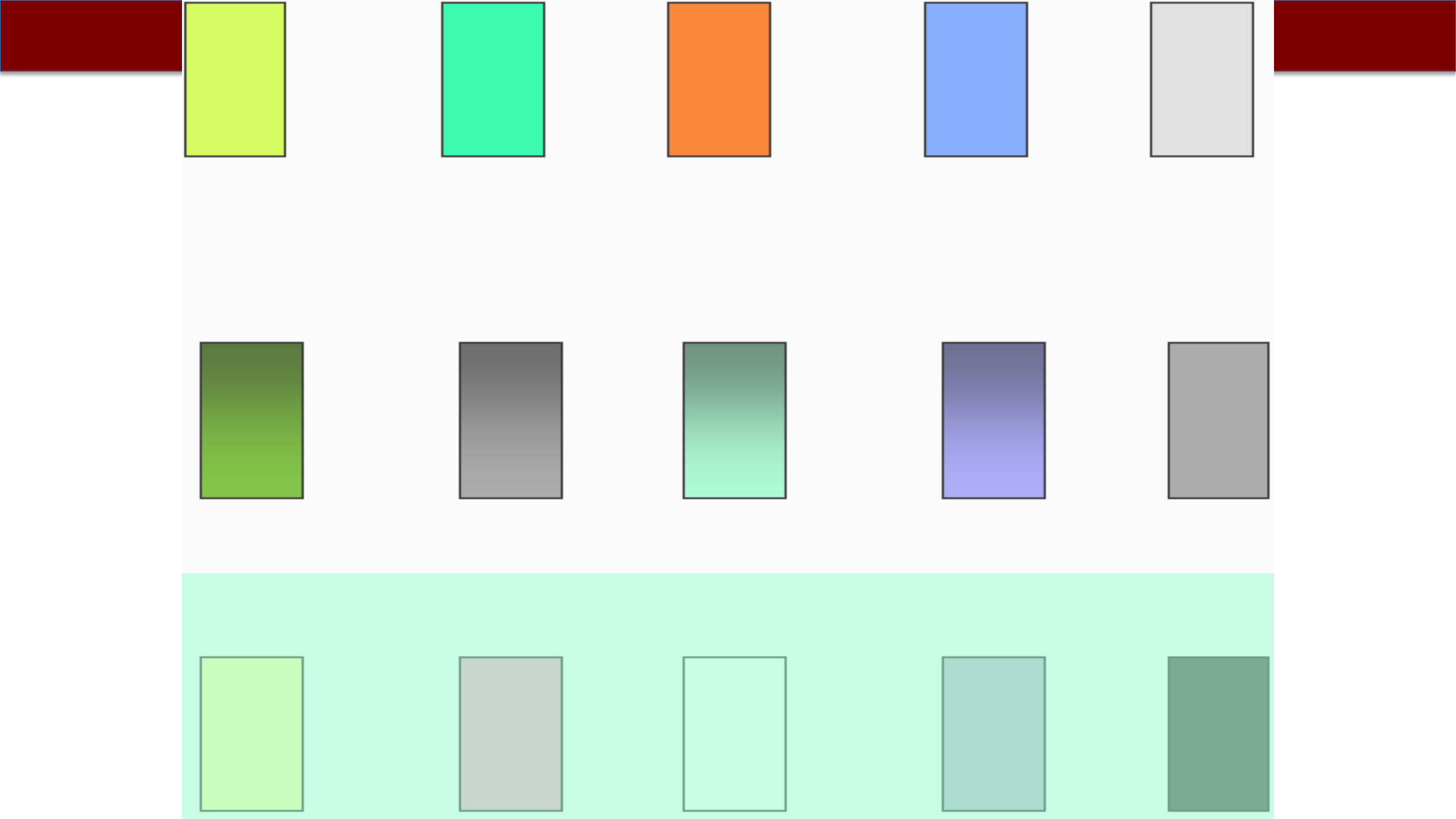


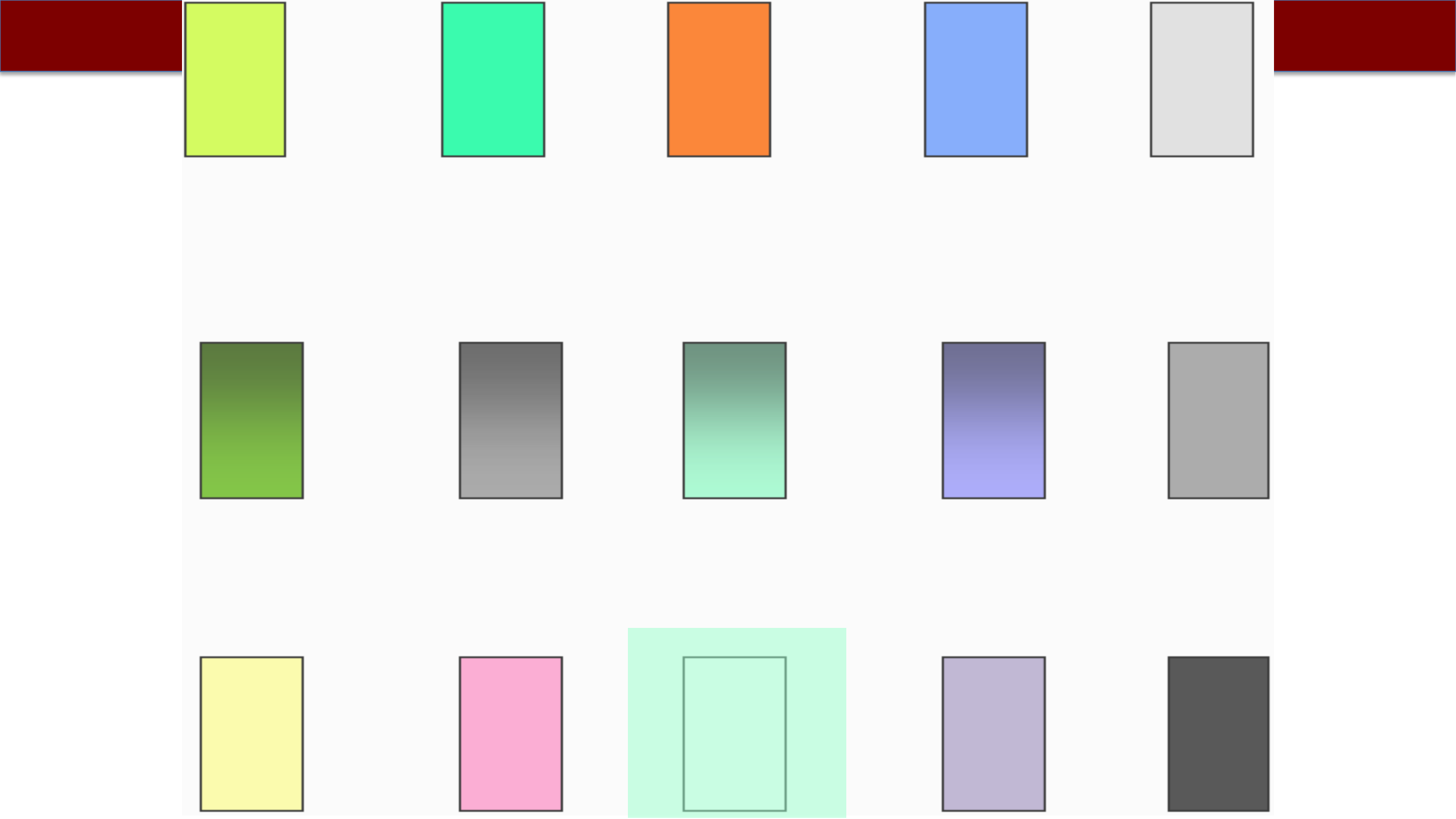


*Color Appearance is
Calculated Across Space*

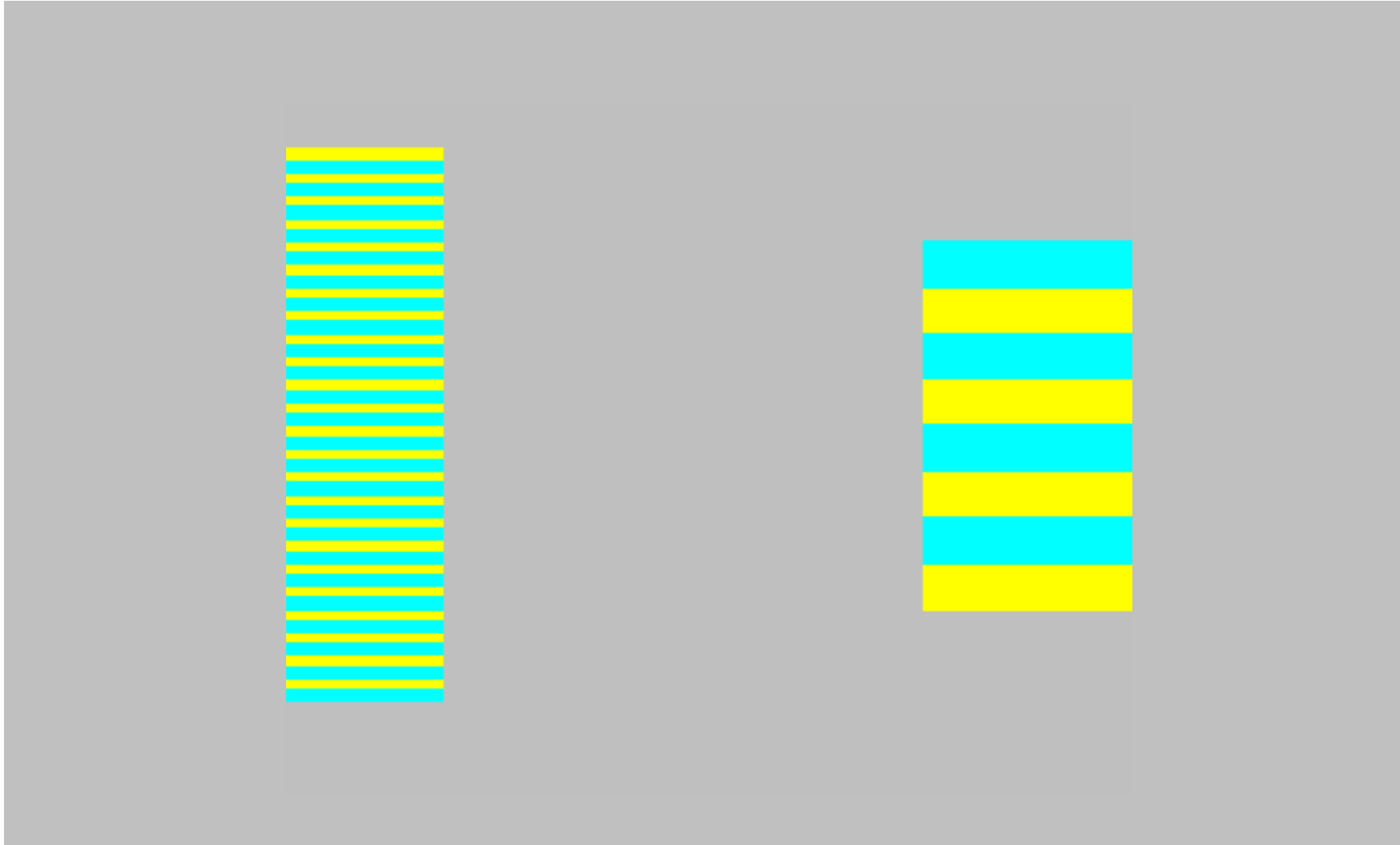








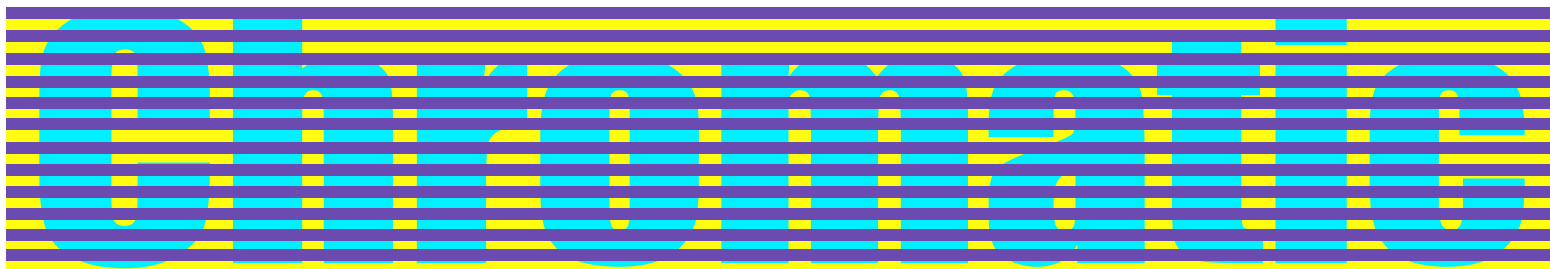
Chromatic Aberration Influences Appearance



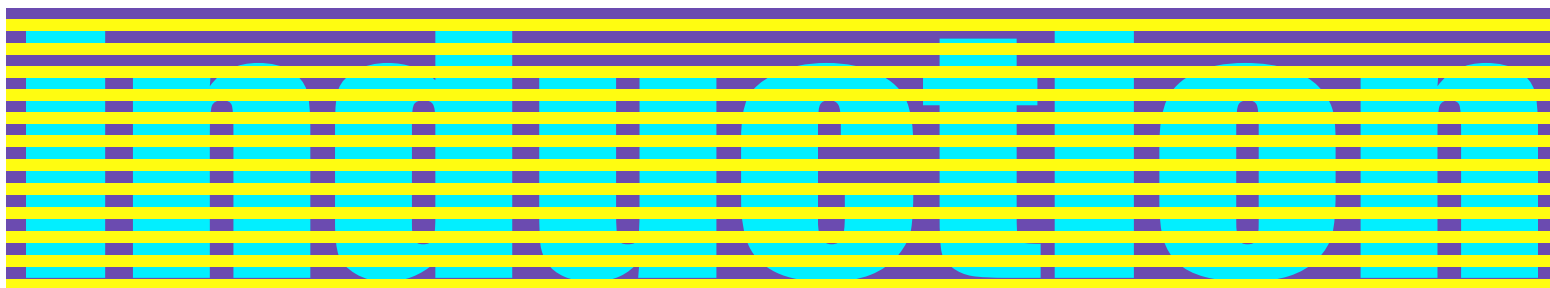
From Foundations of Vision

Text is the same in 3 slides

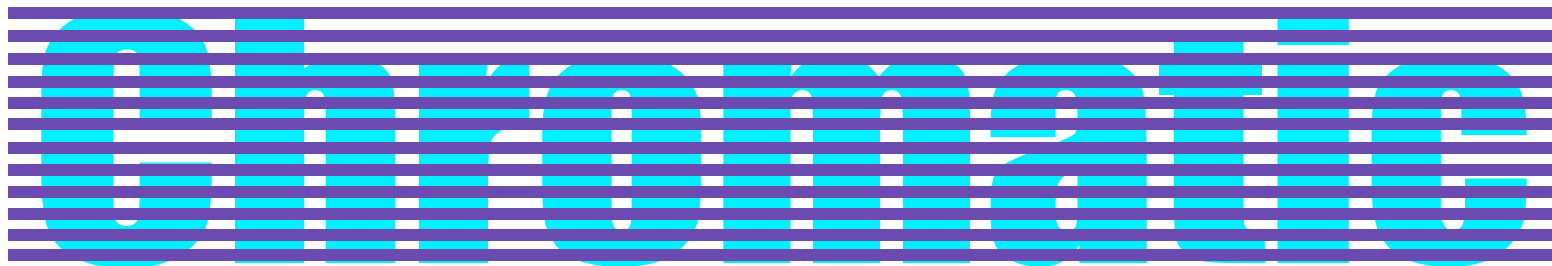
Chromatic induction



Purple in front, Yellow in back



Yellow in front, Purple in back

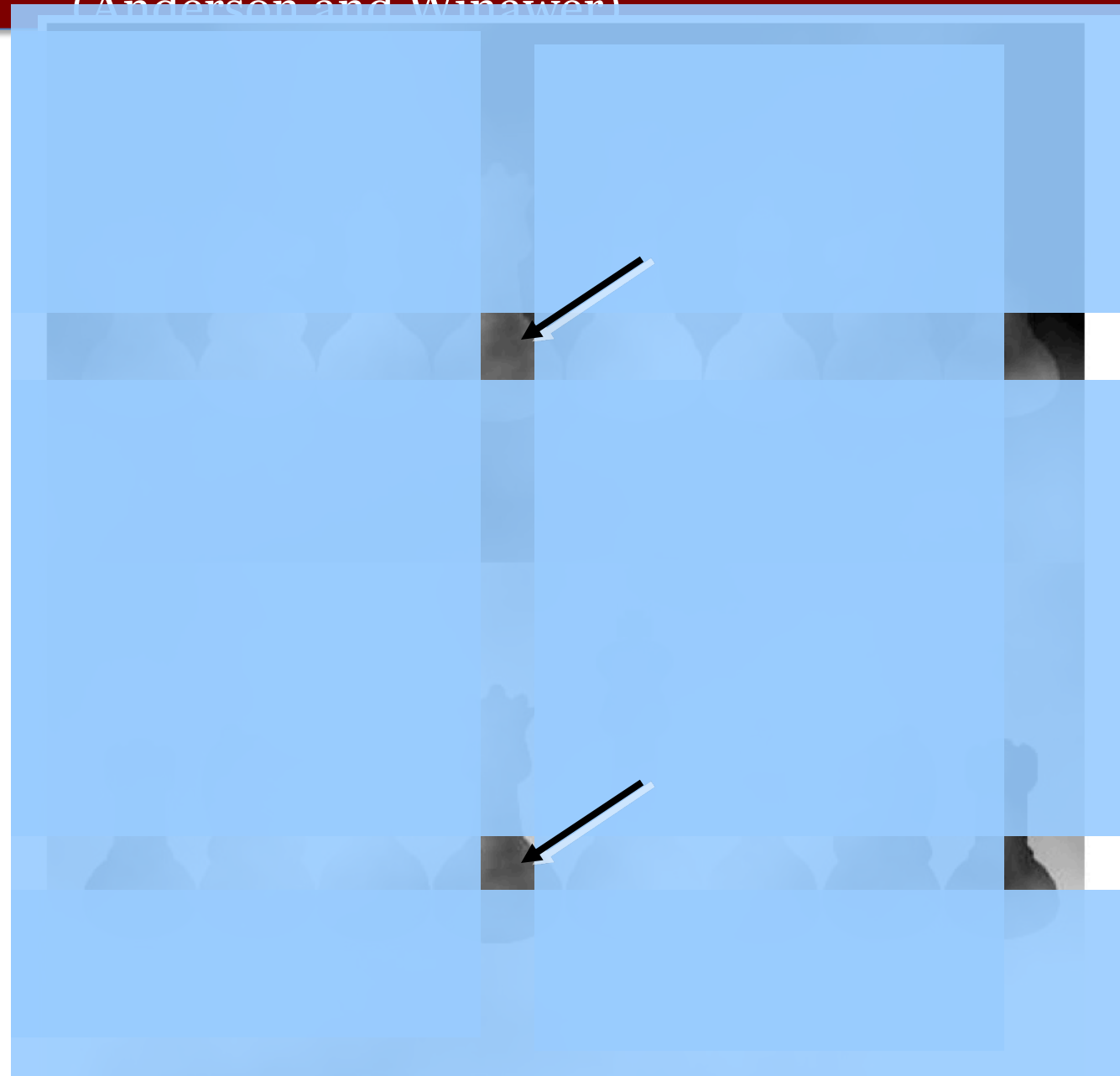


Purple in front, White in back



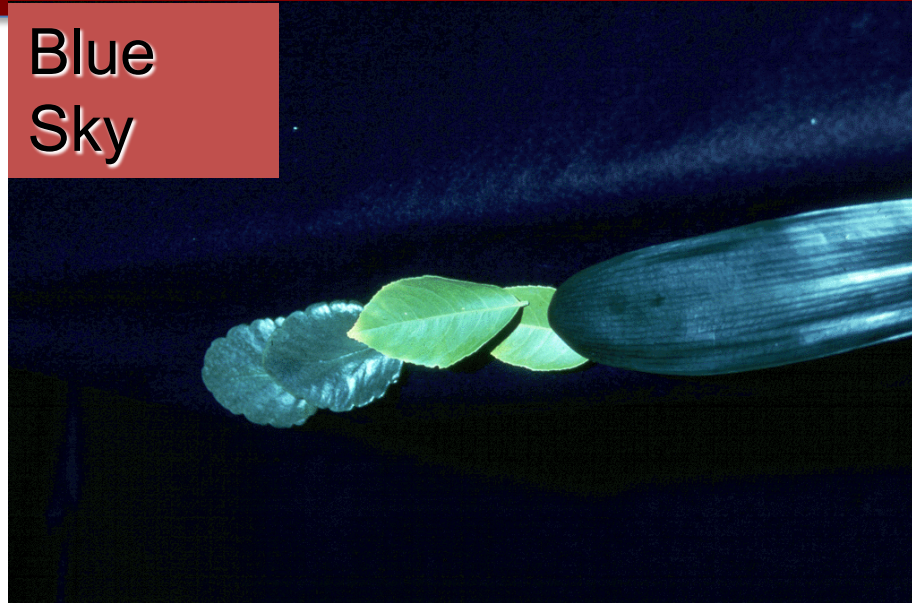
Yellow in front, White in back

Lightness Perception (Anderson and Winawer)

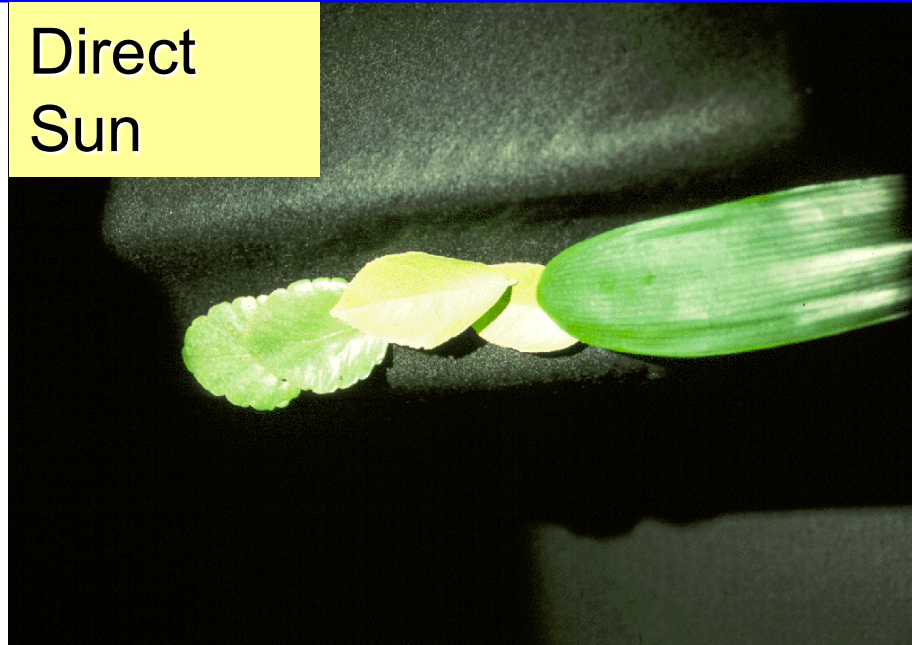


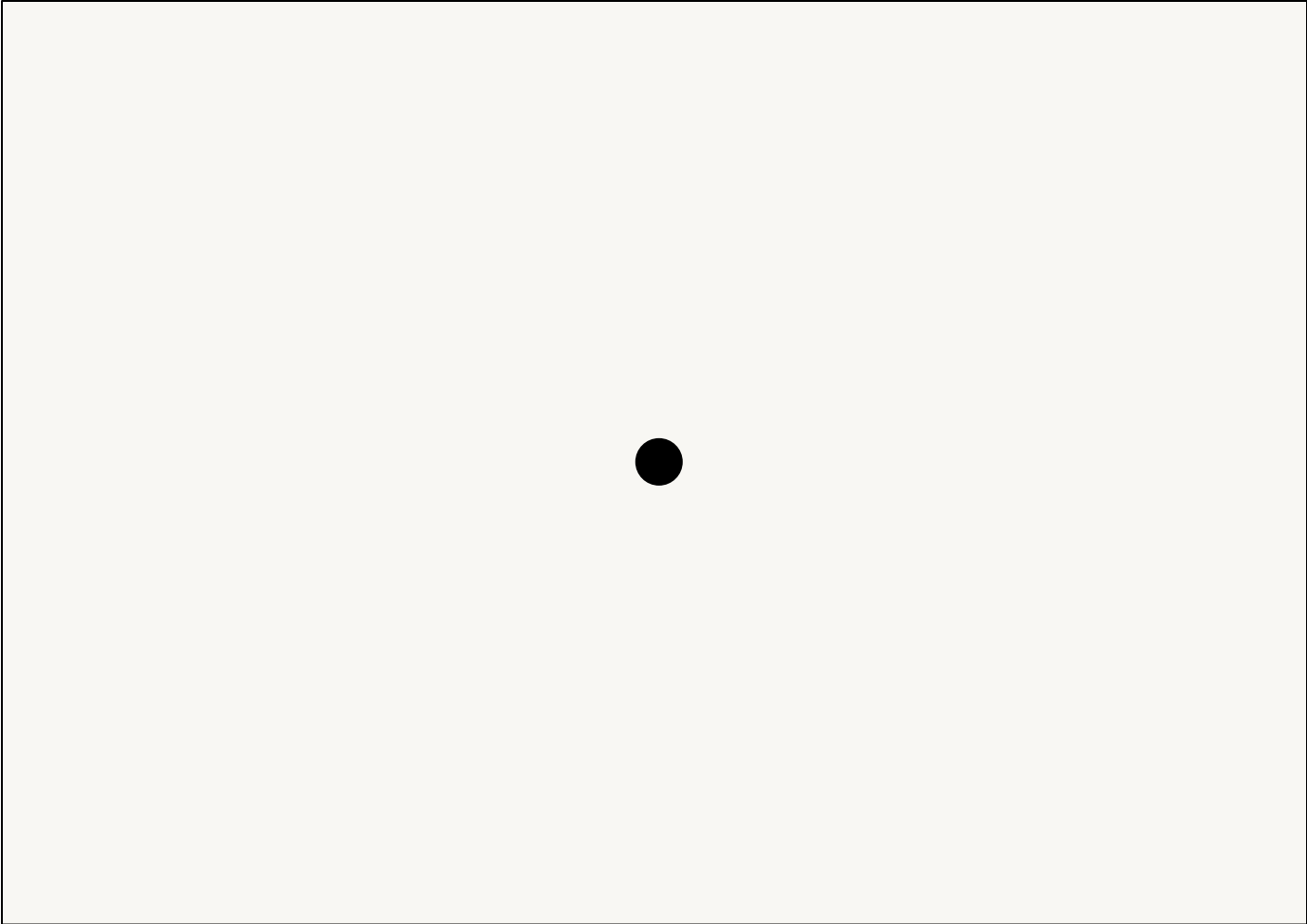
*The chess pieces
are the same shade;
really.*

Blue
Sky



Direct
Sun

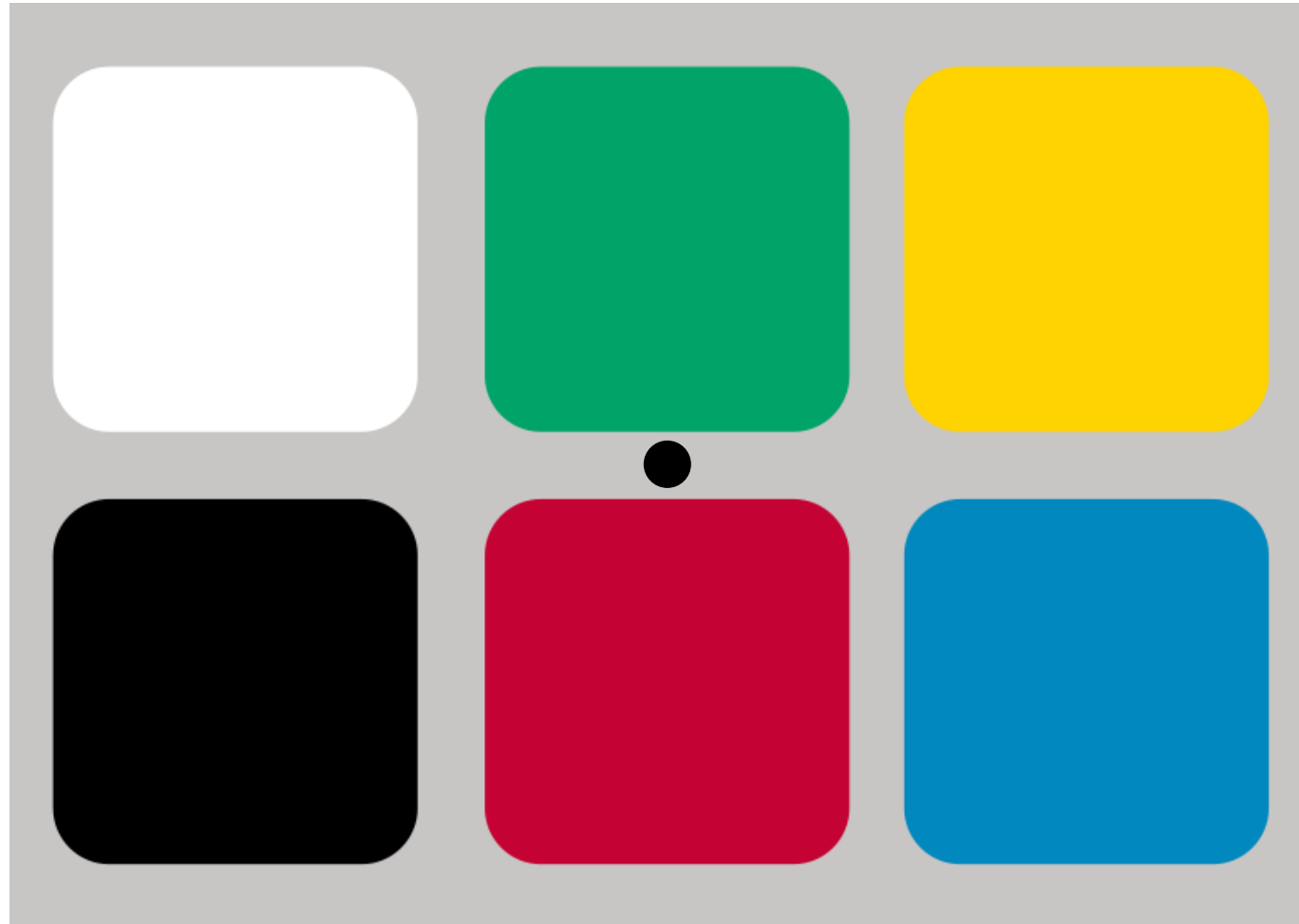




White
Green
Yellow

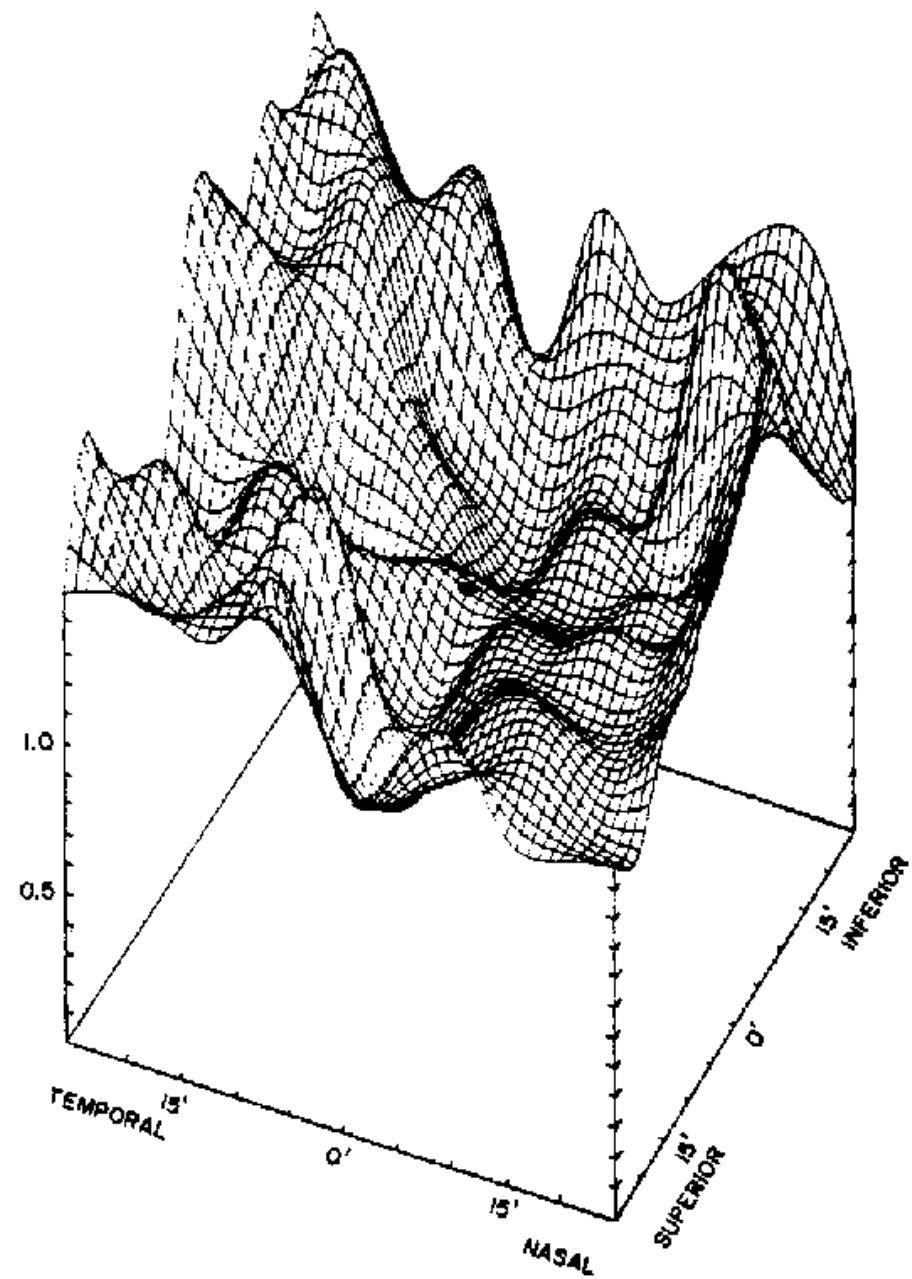
Black
Red
Blue

Opponent-Colors – Afterimage demo



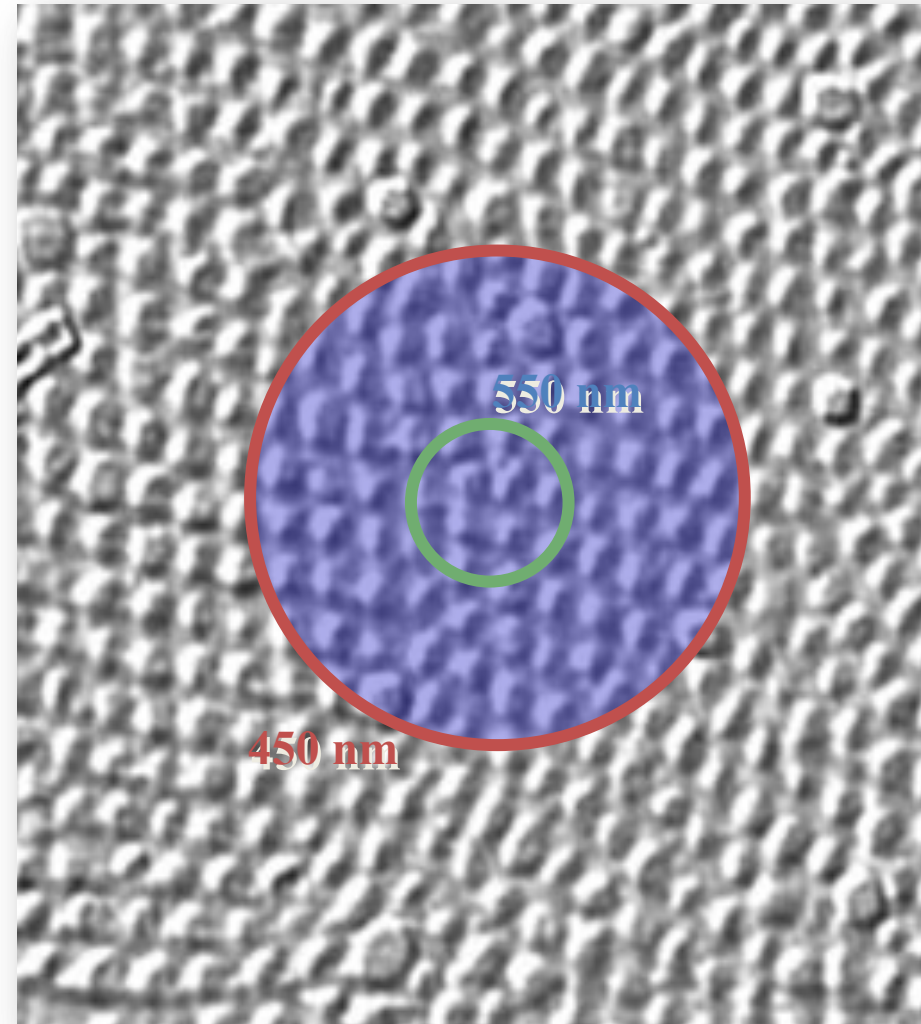
White
Green
Yellow

Black
Red
Blue



Optical point spread in the human fovea

for a 3mm pupil at 550nm and 450nm
(cone mosaic is shown in the background)

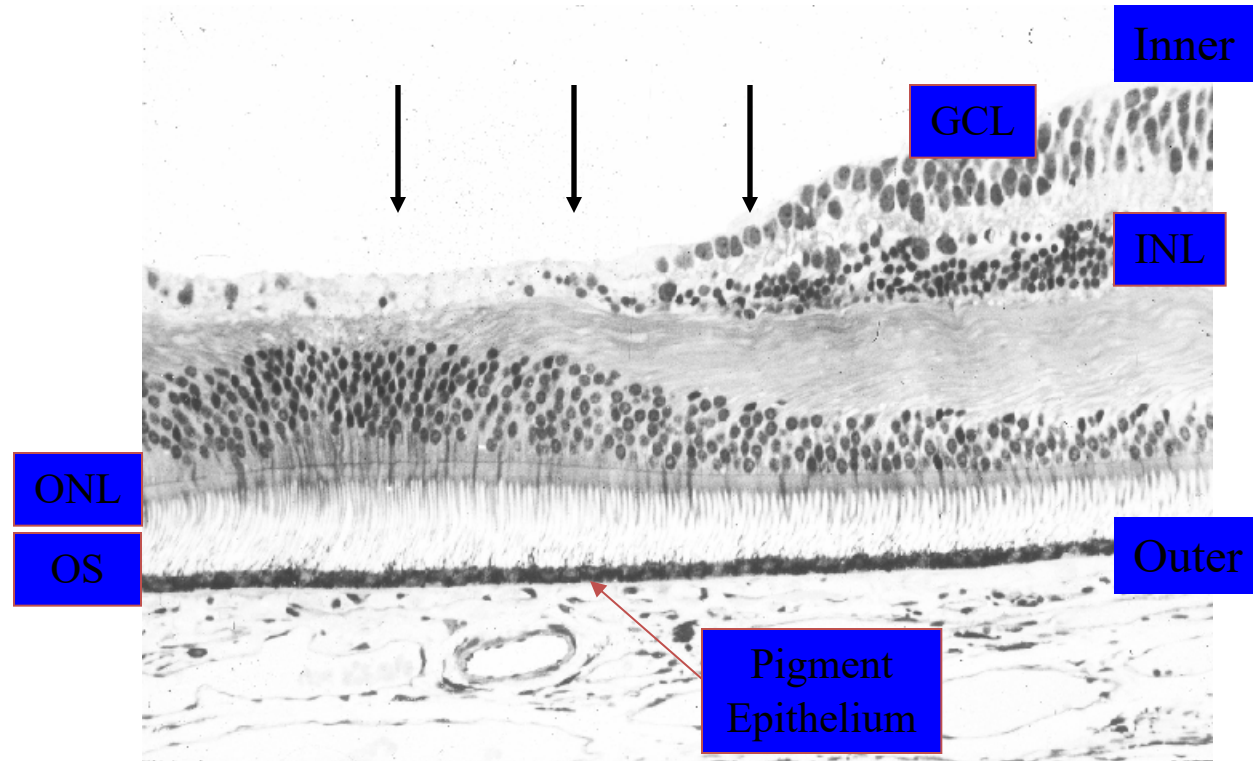


5 μm

Short-wavelength
(450nm) light creates
a very blurry image

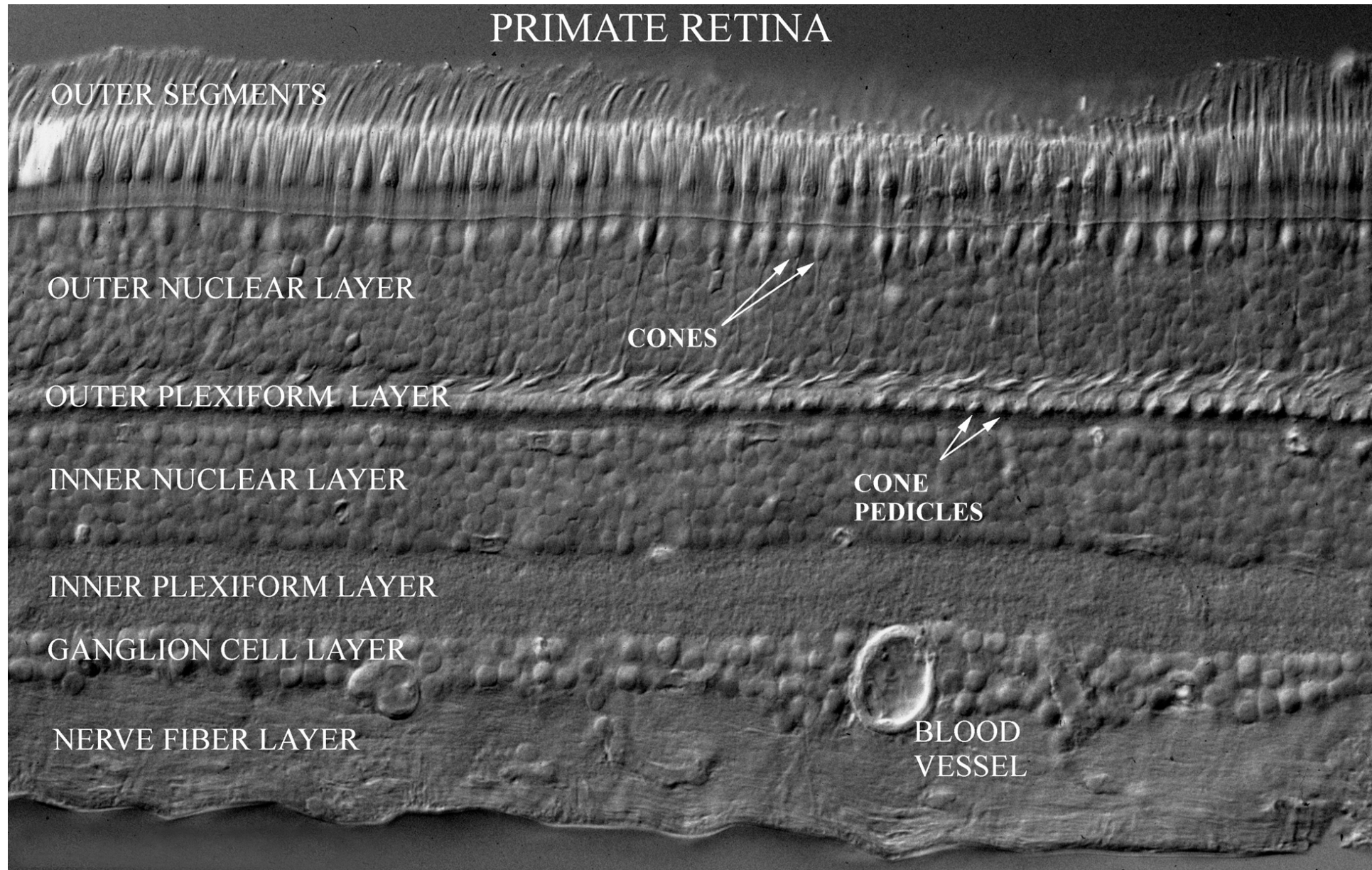
The Retina

- 5 x 5 cm, 0.4 mm thick
 - 5×10^6 cones
 - 10^8 rods
- Foveal cone width: 1 μ m
- Contacts per cone: 250
 - 10^6 optic nerve fibers



Curcio
Rodiek

Peripheral retina



Color vision is interesting

[Blue Man Group](#)

Oct. 2016: 2,614,430 views



http://www.youtube.com/watch?v=W-yLfm5HsHc&feature=youtube_gdata_player