# Query Optimization 

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## Query Execution Overview



## Outline

What can we optimize?
Rule-based optimization
Data statistics
Cost models
Cost-based plan selection

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## What Can We Optimize?

Operator graph: what operators do we run, and in what order?

Operator implementation: for operators with several impls (e.g. join), which one to use?

Access paths: how to read each table?
» Index scan, table scan, C-store projections,

## Typical Challenge

There is an exponentially large set of possible query plans
$\begin{gathered}\text { Access paths } \\ \text { for table 1 }\end{gathered} \times \begin{gathered}\text { Access paths } \\ \text { for table 2 }\end{gathered} \times \underset{\text { for join 1 }}{\text { Algorithms }} \times \underset{\text { for join 2 }}{\text { Algorithms }} \times \underset{\ldots}{ }$

Result: we'll need techniques to prune the search space and complexity involved

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## What is a Rule?

Procedure to replace part of the query plan based on a pattern seen in the plan

Example: When I see expr OR TRUE for an expression expr, replace this with TRUE

## Implementing Rules

## Each rule is typically a function that walks through query plan to search for its pattern

```
void replaceOrTrue(Plan plan) {
    for (node in plan.nodes) {
        if (node instanceof Or) {
            if (node.right == Literal(true))
                plan.replace(node, Literal(true));
                break;
            }
            // Similar code if node.left == Literal(true)
        }
    }
}
```


## Implementing Rules

Rules are often grouped into phases
» E.g. simplify Boolean expressions, pushdown selects, choose join algorithms, etc

Each phase runs rules till they no longer apply

```
plan = originalPlan;
while (true) {
    for (rule in rules) {
        rule.apply(plan);
    }
    if (plan was not changed by any rule) break;
}
```


## Result

Simple rules can work together to optimize complex query plans (if designed well):


## Example Extensible Optimizer

For Thursday, you'll read about Spark SQL's Catalyst optimizer
» Written in Scala using its pattern matching features to simplify writing rules
" $>500$ contributors worldwide, >1000 types of expressions, and hundreds of rules

We'll modify Spark SQL in assignment 2

## § master～spark／sql／catalyst／src／main／scala／org／apache／spark／sql／catalyst／optimizer／Optimizer．scala

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```
\begin{tabular}{|c|c|}
\hline 2291 lines（2095 sloc） & 97.7 KB \\
\hline
\end{tabular}
    /*
    * Licensed to the Apache Software Foundation (ASF) under one or more
    * contributor license agreements. See the NOTICE file distributed with
    * this work for additional information regarding copyright ownership.
    * The ASF licenses this file to You under the Apache License, Version 2.0
    * (the "License"); you may not use this file except in compliance with
    * the License. You may obtain a copy of the License at
* http://www.apache.org/licenses/LICENSE-2.0
*
* Unless required by applicable law or agreed to in writing, software
* distributed under the License is distributed on an "AS IS" BASIS,
* WITHOUT WARRANTIES OR CONDITIONS OF ANY KIND, either express or implied.
* See the License for the specific language governing permissions and
* limitations under the License.
*/
package org.apache.spark.sql.catalyst.optimizer
import scala.collection.mutable
import org.apache.spark.sql.catalyst.analysis._
import org.apache.spark.sql.catalyst.catalog.{InMemoryCatalog, SessionCatalog}
4 \text { import org.apache.spark.sql.catalyst.expressions._}
import org.apache.spark.sql.catalyst.expressions.aggregate.
26 import org.apache.spark.sql.catalyst.plans._
import org.apache.spark.sql.catalyst.plans.logical.{RepartitionOperation, _}
2 8 ~ i m p o r t ~ o r g . a p a c h e . s p a r k . s q l . c a t a l y s t . r u l e s . - ~
import org.apache.spark.sql.catalyst.trees.AlwaysProcess
30 import org.apache.spark.sql.catalyst.trees.TreePattern._
31 import org.apache.spark.sql.connector.catalog.CatalogManager
32 import org.apache.spark.sql.errors.QueryCompilationErrors
import org.apache.spark.sql.internal.SQLConf
34 import org.apache.spark.sql.types._
35 import org.apache.spark.sql.util.SchemaUtils._
36 import org.apache.spark.util.Utils
```

* Defines the default rule batches in the Optimizer.
* 
* Implementations of this class should override this method, and [[nonExcludableRules]] if
* necessary, instead of [[batches]]. The rule batches that eventually run in the Optimizer,
* i.e., returned by [[batches]], will be (defaultBatches - (excludedRules - nonExcludableRules)).
*/
def defaultBatches: Seq[Batch] = \{
val operatorOptimizationRuleSet $=$ Seq(
// Operator push down
PushProjectionThroughUnion,
ReorderJoin,
EliminateOuterJoin,
PushDownPredicates,
PushDownLeftSemiAntiJoin,
PushLeftSemiLeftAntiThroughJoin,
LimitPushDown,
LimitPushDownThroughWindow,
ColumnPruning,
GenerateOptimization,
// Operator combine
CollapseRepartition,
CollapseProject,
OptimizeWindowFunctions,
CollapseWindow,
CombineFilters,
EliminateLimits,
CombineUnions,
// Constant folding and strength reduction
OptimizeRepartition,
TransposeWindow,
NullPropagation,
NullDownPropagation,
ConstantPropagation,
FoldablePropagation,
OptimizeIn,
ConstantFolding,
EliminateAggregateFilter,
ReorderAssociativeOperator,
LikeSimplification,
NotPropagation,
BooleanSimplification,
SimplifyConditionals,
PushFoldableIntoBranches,
RemoveDispensableExpressions,
SimplifyBinaryComparison,
ReplaceNullWithFalseInPredicate,
SimplifyConditionalsInPredicate,
PruneFilters,
SimplifyCasts,
SimplifyCaseConversionExpressions,
RewriteCorrelatedScalarSubquery,
RewriteLateralSubquery,


## Common Rule-Based Optimizations

Simplifying expressions in select, project, etc
» Boolean algebra, numeric expressions, string expressions, etc
» Many redundancies because queries are optimized for readability or produced by code

Simplifying relational operator graphs
" Select, project, join, etc
These relational optimizations have the most impact

## Common Rule-Based Optimizations

Selecting access paths and operator _Also very implementations in simple cases
» Index column predicate $\Rightarrow$ use index
» Small table $\Rightarrow$ use hash join against it
» Aggregation on field with few values $\Rightarrow$ use in-memory hash table

Rules also often used to do type checking and analysis (easy to write recursively)

## Common Relational Rules

Push selects as far down the plan as possible
Recall:
$\sigma_{p}(R \bowtie S)=\sigma_{p}(R) \bowtie S \quad$ if $p$ only references $R$
$\sigma_{q}(R \bowtie S)=R \bowtie \sigma_{q}(S) \quad$ if $q$ only references $S$

$$
\sigma_{p \wedge q}(R \bowtie S)=\sigma_{p}(R) \bowtie \sigma_{q}(S) \quad \text { if } p \text { on } R, q \text { on } S
$$

Idea: reduce \# of records early to minimize work in later ops; enable index access paths

## Common Relational Rules

Push projects as far down as possible
Recall:

$$
\begin{array}{ll}
\Pi_{x}\left(\sigma_{p}(R)\right)=\Pi_{x}\left(\sigma_{p}\left(\Pi_{x \cup z}(R)\right)\right) & z=\text { the fields in } p \\
\Pi_{x \cup y}(R \bowtie S)=\Pi_{x \cup y}\left(\left(\Pi_{x \cup z}(R)\right) \bowtie\left(\Pi_{y \cup z}(S)\right)\right)
\end{array}
$$

$\mathrm{x}=$ fields in $\mathrm{R}, \mathrm{y}=$ in $\mathrm{S}, \mathrm{z}=$ in both

Idea: don't process fields you'll just throw away

## Project Rules Can Backfire!

Example: $\quad R$ has fields $A, B, C, D, E$ $p: A=3 \wedge B=" c a t "$ x: $\{E\}$

$$
\Pi_{x}\left(\sigma_{p}(\mathrm{R})\right) \quad \text { vs } \quad \Pi_{\mathrm{x}}\left(\sigma_{\mathrm{p}}\left(\Pi_{\{\mathrm{A}, \mathrm{~B}, \mathrm{E}\}}(\mathrm{R})\right)\right)
$$

## What if R has Indexes?



## Bottom Line

Many valid transformations will not always improve performance

Need more info to make good decisions
» Data statistics: properties about our input or intermediate data to be used in planning
" Cost models: how much time will an operator take given certain input data statistics?

## Outline

What can we optimize?
Rule-based optimization
Data statistics

## Cost models

Cost-based plan selection

## What Are Data Statistics?

Information about the tuples in a relation that can be used to estimate size \& cost
» Example: \# of tuples, average size of tuples, \# distinct values for each attribute, \% of null values for each attribute

Typically maintained by the storage engine as tuples are added \& removed in a relation
» File formats like Parquet can also have them

## Some Statistics We'll Use

For a relation R ,
$\mathbf{T}(\mathbf{R})=$ \# of tuples in $R$
$\mathbf{S}(\mathbf{R})=$ average size of R's tuples in bytes
$\mathbf{B}(\mathbf{R})=$ \# of blocks to hold all of R's tuples
$\mathbf{V}(\mathbf{R}, \mathbf{A})=$ \# distinct values of attribute A in R

## Example

$R:$| A | B | C | D |
| :---: | :---: | :---: | :---: |
| cat | 1 | 10 | a |
| cat | 1 | 20 | b |
| dog | 1 | 30 | a |
| dog | 1 | 40 | c |
| bat | 1 | 50 | d |

A: 20 byte string
B: 4 byte integer
C: 8 byte date
D: 5 byte string

## Example

R: | A | B | C | D |
| :---: | :---: | :---: | :---: |
| cat | 1 | 10 | a |
| cat | 1 | 20 | b |
| dog | 1 | 30 | a |
| dog | 1 | 40 | c |
| bat | 1 | 50 | d |

$$
\begin{array}{ll}
T(R)=5 & S(R)=37 \\
V(R, A)=3 & V(R, C)=5 \\
V(R, B)=1 & V(R, D)=4
\end{array}
$$

## Challenge: Intermediate Tables

Keeping stats for tables on disk is easy, but what about intermediate tables that appear during a query plan?

## Examples:

$\sigma_{p}(R) \leftarrow \begin{aligned} & \text { We already have } T(R), S(R), V(R, a) \text {, etc, } \\ & \text { but how to get these for tuples that pass } p \text { ? }\end{aligned}$
$R \bowtie S \leftarrow$ How many and what types of tuple pass the join condition?

Should we do $(R \bowtie S) \bowtie T$ or $R \bowtie(S \bowtie T)$ or $(R \bowtie T) \bowtie S$ ?

## Stat Estimation Methods

Algorithms to estimate subplan stats
An ideal algorithm would have:

1) Accurate estimates of stats
2) Low cost
3) Consistent estimates (e.g. different plans for a subtree give same estimated stats)

Can't always get all this!

## Size Estimates for $\mathbf{W}=\mathbf{R}_{\mathbf{1}} \times \mathbf{R}_{\mathbf{2}}$

## $\mathrm{S}(\mathrm{W})=$

$T(W)=$

## Size Estimates for $\mathbf{W}=\mathbf{R}_{\mathbf{1}} \times \mathbf{R}_{\mathbf{2}}$

$$
S(W)=S\left(R_{1}\right)+S\left(R_{2}\right)
$$

$$
T(W)=T\left(R_{1}\right) \times T\left(R_{2}\right)
$$

## Size Estimate for $\mathbf{W}=\sigma_{A=a}(R)$

## $\mathrm{S}(\mathrm{W})=$

$T(W)=$

## Size Estimate for $\mathbf{W}=\sigma_{A=a}(R)$

## $S(W)=S(R) \longleftarrow$ Not true if some variable-length fields

 are correlated with value of $A$$T(W)=$

## Example

| R | A | B | C | D | $V(R, A)=3$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | cat | 1 | 10 | a | $V(R, B)=1$ |
|  | cat | 1 | 20 | b |  |
|  | dog | 1 | 30 | a |  |
|  | dog | 1 | 40 | c | R,D)=4 |
|  | bat | 1 | 50 | d |  |

$\mathrm{W}=\sigma_{\mathrm{Z}=\mathrm{val}}(\mathrm{R}) \quad \mathrm{T}(\mathrm{W})=$

## Example


$\mathrm{W}=\sigma_{\mathrm{Z}=\mathrm{val}}(\mathrm{R}) \quad \mathrm{T}(\mathrm{W})=$

## Example

| R | A | B | C | D | $V(R, A)=3$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | cat | 1 | 10 | a | $V(R, B)=1$ |
|  | cat | 1 | 20 | b | $V(\mathrm{R}, \mathrm{C})=5$ |
|  | dog | 1 | 30 | a |  |
|  | dog | 1 | 40 | c |  |
|  | bat | 1 | 50 | d |  |

$W=\sigma_{Z=\text { val }}(R) \quad T(W)=\frac{T(R)}{V(R, Z)}$

## Assumption:

Values in select expression $\mathrm{Z}=$ val are uniformly distributed over all $V(R, Z)$ values

## Alternate Assumption:

Values in select expression $\mathrm{Z}=\mathrm{val}$ are uniformly distributed over a domain with
$\operatorname{DOM}(R, Z)$ values

## Example

Alternate assumption

R | A | B | C | D |
| :---: | :---: | :---: | :---: |
| cat | 1 | 10 | a |
| cat | 1 | 20 | b |
| dog | 1 | 30 | a |
| dog | 1 | 40 | c |
| bat | 1 | 50 | d |

$V(R, A)=3, \operatorname{DOM}(R, A)=10$
$V(R, B)=1, D O M(R, B)=10$
$V(R, C)=5, \operatorname{DOM}(R, C)=10$
$V(R, D)=4, \operatorname{DOM}(R, D)=10$
$\mathrm{W}=\sigma_{\mathrm{Z}=\mathrm{val}}(\mathrm{R}) \quad \mathrm{T}(\mathrm{W})=$

## Example

## Alternate assumption

| R | A | B | C | D | $V(R, A)=3, \operatorname{DOM}(\mathrm{R}, \mathrm{A})=10$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | cat | 1 | 10 | a | $V(R, B)=1, \operatorname{DOM}(\mathrm{R}, \mathrm{B})=10$ |
|  | cat | 1 | 20 | b | $V(\mathrm{R}, \mathrm{C})=5, \mathrm{DOM}(\mathrm{R}, \mathrm{C})=10$ |
|  | dog | 1 | 30 | a | $V(R, D)=4, \operatorname{DOM}(\mathrm{R}, \mathrm{D})=10$ |
| (dog 1 |  |  |  |  |  |
| 50 d what is probability this |  |  |  |  |  |
|  | ( pal |  |  |  |  |

## Example

Alternate assumption

$R \quad$| A | B | C | D |
| :---: | :---: | :---: | :---: |
| cat | 1 | 10 | a |
| cat | 1 | 20 | b |
| dog | 1 | 30 | a |
| dog | 1 | 40 | c |
| bat | 1 | 50 | d |

$V(R, A)=3, D O M(R, A)=10$
$V(R, B)=1, D O M(R, B)=10$
$V(R, C)=5, \operatorname{DOM}(R, C)=10$
$\mathrm{V}(\mathrm{R}, \mathrm{D})=4, \mathrm{DOM}(\mathrm{R}, \mathrm{D})=10$
$\mathrm{W}=\sigma_{\mathrm{Z}=\mathrm{val}}(\mathrm{R})$

$$
T(W)=\frac{T(R)}{\operatorname{DOM}(R, Z)}
$$

## Selection Cardinality

SC(R, A) = average \# records that satisfy equality condition on R.A
$S C(R, A)=\left\{\begin{array}{l}\frac{T(R)}{V(R, A)} \\ \frac{T(R)}{D O M(R, A)}\end{array}\right.$

## What About $W=\sigma_{z \geq \text { val }}(R) ?$

## $\mathrm{T}(\mathrm{W})=$ ?

## What About $W=\sigma_{z \geq \text { val }}(R)$ ?

$\mathrm{T}(\mathrm{W})=$ ?
Solution 1: $\mathrm{T}(\mathrm{W})=\mathrm{T}(\mathrm{R}) / 2$

## What About $W=\sigma_{z \geq \text { val }}(R)$ ?

$\mathrm{T}(\mathrm{W})=$ ?
Solution 1: $\mathrm{T}(\mathrm{W})=\mathrm{T}(\mathrm{R}) / 2$
Solution 2: $\mathrm{T}(\mathrm{W})=\mathrm{T}(\mathrm{R}) / 3$

## Solution 3: Estimate Fraction of Values in Range

Example: R

$\operatorname{Min}=1 \quad V(R, Z)=10$ $\downarrow \quad W=\sigma_{z \geq 15}(R)$
$\operatorname{Max}=20$
$f=\frac{20-15+1}{20-1+1}=\frac{6}{20}$
(fraction of range)
$T(W)=f \times T(R)$

# Solution 3: Estimate Fraction of Values in Range 

Equivalently, if we know values in column:
$f=$ fraction of distinct values $\geq$ val
$T(W)=f \times T(R)$

# What About More Complex Expressions? 

E.g. estimate selectivity for

SELECT * FROM R
WHERE user_defined_func(a) > 10


1926
1927
function_selectivity(PlannerInfo *root,
Oid funcid,
List *args,
Oid inputcollid,
bool is_join,
int varRelid,
JoinType jointype,
SpecialJoinInfo *sjinfo)

RegProcedure prosupport = get_func_support(funcid);
SupportRequestSelectivity req;
SupportRequestSelectivity *sresult;
/*

* If no support function is provided, use our historical default
* estimate, 0.3333333 . This seems a pretty unprincipled choice, but
* Postgres has been using that estimate for function calls since 1992.
* The hoariness of this behavior suggests that we should not be in too
* much hurry to use another value.
*/
if (!prosupport)
return (Selectivity) 0.3333333;
req.type $=$ T_SupportRequestSelectivity;
req. root $=$ root;
req.funcid $=$ funcid;
req.args = args;
req.inputcollid $=$ inputcollid;
req.is_join = is_join;
req.varRelid = varRelid;
req.jointype $=$ jointype;
req.sjinfo $=$ sjinfo;
req. selectivity $=-1 ; \quad / *$ to catch failure to set the value $* /$
sresult $=($ SupportRequestSelectivity $*)$
DatumGetPointer(OidFunctionCall1(prosupport,
PointerGetDatum(\&req)));
/* If support function fails, use default */
if (sresult != \&req)
return (Selectivity) 0.3333333;
if (req.selectivity < 0.0 || req. selectivity > 1.0)
elog(ERROR, "invalid function selectivity: \%f", req.selectivity);
return (Selectivity) req.selectivity;


## Size Estimate for $\mathbf{W}=\mathbf{R}_{1} \bowtie \mathbf{R}_{2}$

Let $X=$ attributes of $R_{1}$
$Y=$ attributes of $R_{2}$

Case 1: $\mathrm{X} \cap \mathrm{Y}=\emptyset:$
Same as $\mathrm{R}_{1} \times \mathrm{R}_{2}$

## Case 2: $\mathbf{W}=\mathbf{R}_{1} \bowtie \mathbf{R}_{2}, \mathbf{X} \cap \mathbf{Y}=\mathbf{A}$

| $\mathrm{R}_{1}$ | A | B | C | $\mathrm{R}_{2}$ | A | D |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |

## Case 2: $\mathbf{W}=\mathbf{R}_{1} \bowtie R_{\mathbf{2}}, \mathrm{X} \cap \mathrm{Y}=\mathrm{A}$



Assumption ("containment of value sets"):
$V\left(R_{1}, A\right) \leq V\left(R_{2}, A\right) \Rightarrow$ Every $A$ value in $R_{1}$ is in $R_{2}$ $V\left(R_{2}, A\right) \leq V\left(R_{1}, A\right) \Rightarrow$ Every $A$ value in $R_{2}$ is in $R_{1}$

## Computing T(W) when $\mathrm{V}\left(\mathrm{R}_{1}, \mathrm{~A}\right) \leq \mathrm{V}\left(\mathrm{R}_{2}, \mathrm{~A}\right)$



1 tuple matches with $\quad T\left(R_{2}\right)$ tuples...
$\mathrm{V}\left(\mathrm{R}_{2}, \mathrm{~A}\right)$
$\begin{array}{cc}\text { so } \\ \text { cs } 245\end{array} \quad T(W)=\frac{T\left(R_{1}\right) \times T\left(R_{2}\right)}{V\left(R_{2}, A\right)}$

$$
\begin{aligned}
& V\left(R_{1}, A\right) \leq V\left(R_{2}, A\right) \Rightarrow T(W)=\frac{T\left(R_{1}\right) \times T\left(R_{2}\right)}{V\left(R_{2}, A\right)} \\
& V\left(R_{2}, A\right) \leq V\left(R_{1}, A\right) \Rightarrow T(W)=\frac{T\left(R_{1}\right) \times T\left(R_{2}\right)}{V\left(R_{1}, A\right)}
\end{aligned}
$$

## In General for $\mathbf{W}=\mathbf{R}_{\mathbf{1}} \bowtie \mathbf{R}_{\mathbf{2}}$

$$
T(W)=\frac{T\left(R_{1}\right) \times T\left(R_{2}\right)}{\max \left(V\left(R_{1}, A\right), V\left(R_{2}, A\right)\right)}
$$

Where $A$ is the common attribute set

## Case 2 with Alternate Assumption

Values uniformly distributed over domain


This tuple matches $T\left(R_{2}\right) / \operatorname{DOM}\left(R_{2}, A\right)$, so

$$
T(W)=\frac{T\left(R_{1}\right) T\left(R_{2}\right)}{\operatorname{DOM}\left(R_{2}, A\right)}=\frac{T\left(R_{1}\right) T\left(R_{2}\right)}{\operatorname{DOM}\left(R_{1}, A\right)}
$$

## Tuple Size after Join

## In all cases:

$$
S(W)=S\left(R_{1}\right)+S\left(R_{2}\right)-S(A)
$$

## Using Similar Ideas, Can Estimate Sizes of:

$\Pi_{A, B}(R)$
$\sigma_{A=a \wedge B=b}(R)$
$R \bowtie S$ with common attributes $A, B, C$
Set union, intersection, difference, ...

## For Complex Expressions, Need Intermediate T, S, V Results

$$
\text { E.g. } W=\sigma_{A=a}\left(R_{1}\right) \bowtie R_{2}
$$

Treat as relation U

$$
T(U)=T\left(R_{1}\right) / V\left(R_{1}, A\right) \quad S(U)=S\left(R_{1}\right)
$$

Also need V(U, *) !!

## To Estimate V

## E.g., $U=\sigma_{A=a}\left(R_{1}\right)$

Say $R_{1}$ has attributes $A, B, C, D$

$$
\begin{aligned}
& V(U, A)= \\
& V(U, B)= \\
& V(U, C)= \\
& V(U, D)=
\end{aligned}
$$

## Example



$$
\begin{aligned}
& V\left(R_{1}, A\right)=3 \\
& V\left(R_{1}, B\right)=1 \\
& V\left(R_{1}, C\right)=5 \\
& V\left(R_{1}, D\right)=3 \\
& U=\sigma_{A=a}\left(R_{1}\right)
\end{aligned}
$$

## Example

$$
\begin{aligned}
& V\left(R_{1}, A\right)=3 \\
& V\left(R_{1}, B\right)=1 \\
& V\left(R_{1}, C\right)=5 \\
& V\left(R_{1}, D\right)=3 \\
& U=\sigma_{A=a}\left(R_{1}\right) \\
& V(U, A)=1 \quad V(U, B)=1 \quad V(U, C)=\frac{T(R 1)}{V(R 1, A)}
\end{aligned}
$$

$\mathrm{V}(\mathrm{U}, \mathrm{D})=$ somewhere in between..

## Possible Guess in $U=\sigma_{A \geq a}(R)$

$V(U, A)=V(R, A) / 2$
$V(U, B)=V(R, B)$

## For Joins: $\mathbf{U}=\mathbf{R}_{\mathbf{1}}(\mathrm{A}, \mathrm{B}) \bowtie \mathbf{R}_{\mathbf{2}}(\mathrm{A}, \mathrm{C})$

We'll use the following estimates:
$\mathrm{V}(\mathrm{U}, \mathrm{A})=\min \left(\mathrm{V}\left(\mathrm{R}_{1}, A\right), \mathrm{V}\left(\mathrm{R}_{2}, A\right)\right)$
$\mathrm{V}(\mathrm{U}, \mathrm{B})=\mathrm{V}\left(\mathrm{R}_{1}, \mathrm{~B}\right)$
$V(U, C)=V\left(R_{2}, C\right)$

Called "preservation of value sets"

## Example:

$$
Z=R_{1}(A, B) \bowtie R_{2}(B, C) \bowtie R_{3}(C, D)
$$

$\mathrm{R}_{1}$
$T\left(R_{1}\right)=1000 \quad V\left(R_{1}, A\right)=50 \quad V\left(R_{1}, B\right)=100$
$\mathrm{R}_{2}$
$T\left(R_{2}\right)=2000 V\left(R_{2}, B\right)=200 V\left(R_{2}, C\right)=300$
$\mathrm{R}_{3}$
$T\left(R_{3}\right)=3000 \quad V\left(R_{3}, C\right)=90 \quad V\left(R_{3}, D\right)=500$

## Partial Result: U = $\mathbf{R}_{1} \bowtie \mathbf{R}_{\mathbf{2}}$

$$
\begin{aligned}
& T(U)=\frac{1000 \times 2000}{200} \\
& V(U, A)=50 \\
& V(U, B)=100 \\
& V(U, C)=300
\end{aligned}
$$

## End Result: Z = U $\bowtie \mathbf{R}_{3}$

$$
\begin{aligned}
\mathrm{T}(\mathrm{Z})=\frac{1000 \times 2000 \times 3000}{200 \times 300} \quad & V(Z, A)=50 \\
& V(Z, B)=100 \\
& V(Z, C)=90 \\
& V(Z, D)=500
\end{aligned}
$$

## Another Statistic: Histograms



$$
\begin{aligned}
& \sigma_{A \geq a}(R)=? \\
& \sigma_{A=a}(R)=?
\end{aligned}
$$

## Requires some care to set bucket boundaries

## Outline

What can we optimize?
Rule-based optimization
Data statistics

## Cost models

Cost-based plan selection

