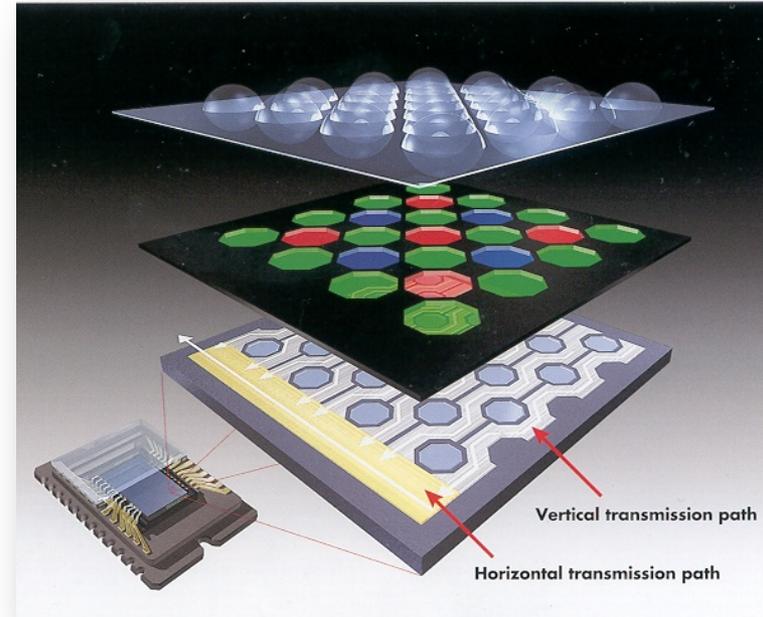


# Image sensors

- Sensor technologies: CMOS and CCD
- CMOS imagers dominate high-volume applications; Fabrication cost, lower power; system integration
- CCD are used in certain scientific applications (astronomy)
- CMOS sensors: viable research platform
  - Enable new experiments
  - New imaging architectures



# Photo detector: basic principles

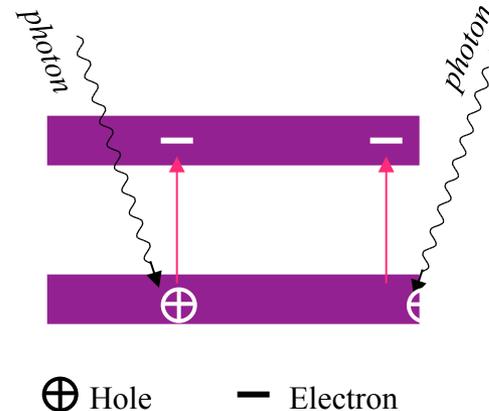
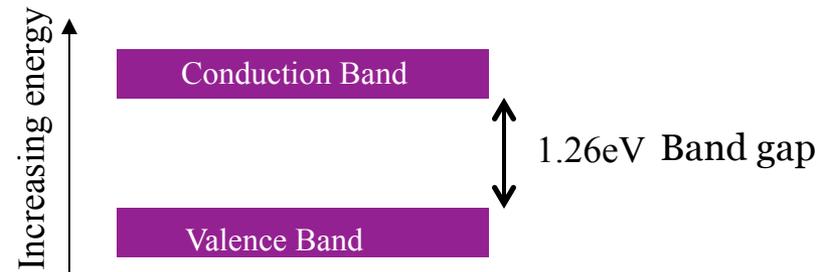
## Photoelectric effect



# The photoelectric effect (CMOS and CCD)

Atoms in a silicon crystal have electrons arranged in discrete bands called the **Valence Band** (lower energy) and the **Conduction Band** (higher energy).

Most electrons occupy the **Valence band**. The absorption of a photon can excite electrons into the **conduction band**. The excitation requires the photon to provide at least 1.26 electron volts.

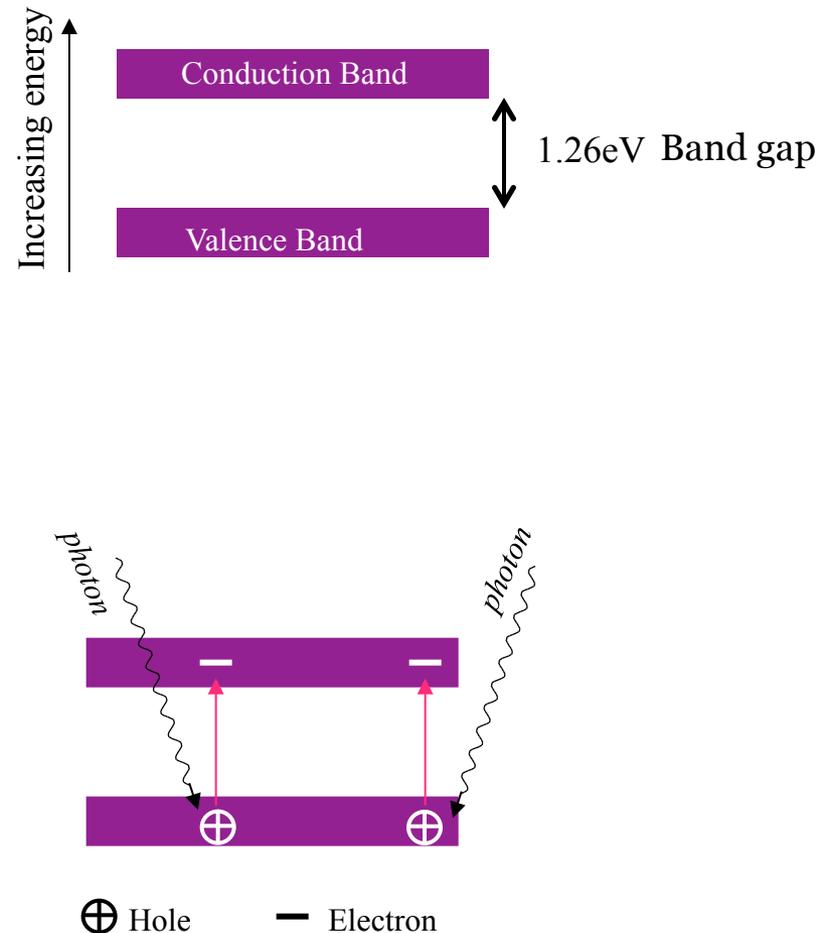


# The photoelectric effect

A 1100nm photon of light has 1.26eV.  
Beyond this wavelength silicon is transparent; hence silicon imagers are insensitive beyond this infra-red band.

In the conduction band electrons move freely about in the lattice of the silicon crystal; this leaves a 'hole' in the valence band which acts like a positively charged carrier. In the absence of an external electric field the hole and electron will recombine and be lost.

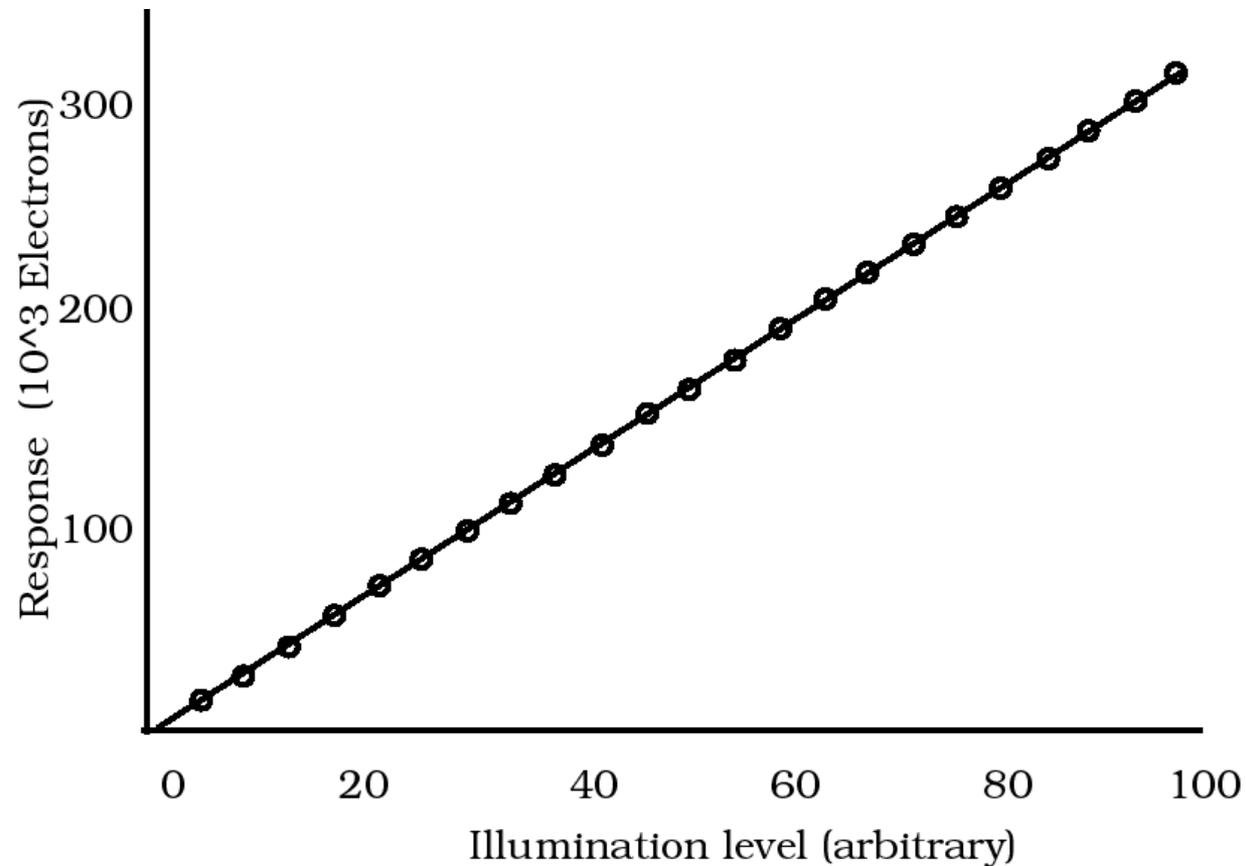
- In a CCD an electric field is introduced to prevent recombination.
- In CMOS electrons are trapped in capacitors.



# CCD and CMOS transfer functions

Both are Si absorptions

Photons to electrons mapping is linear



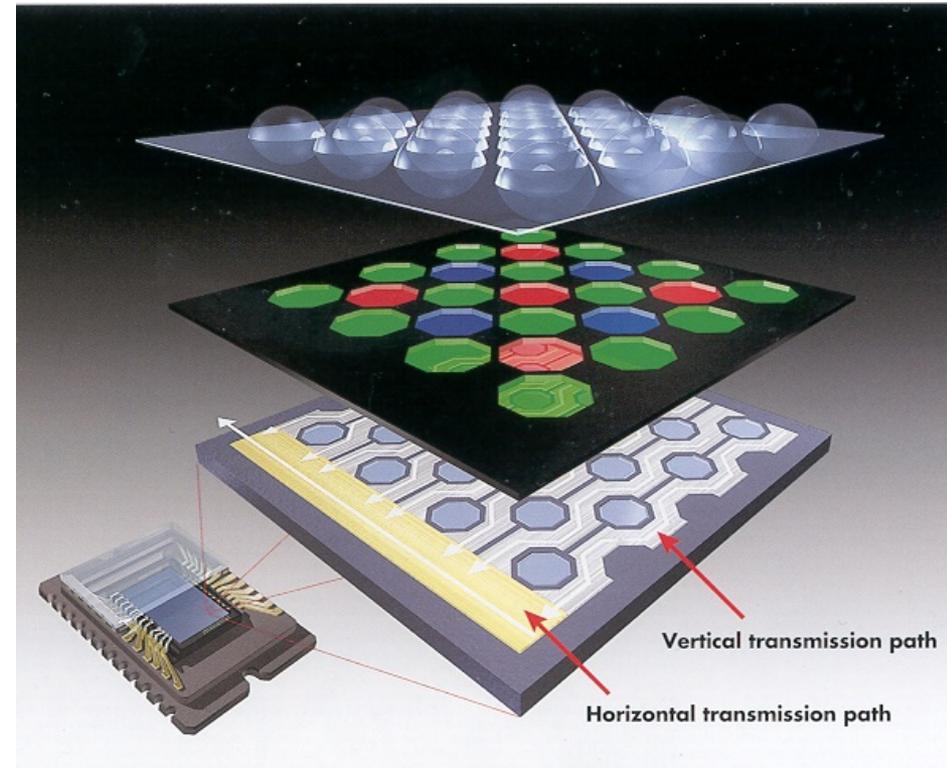
*(Epperson, P.M. et al. Electro-optical characterization of the Tektronix TK5 ..., Opt Eng., 25, 1987)*

# Sensors

- Front-illuminated

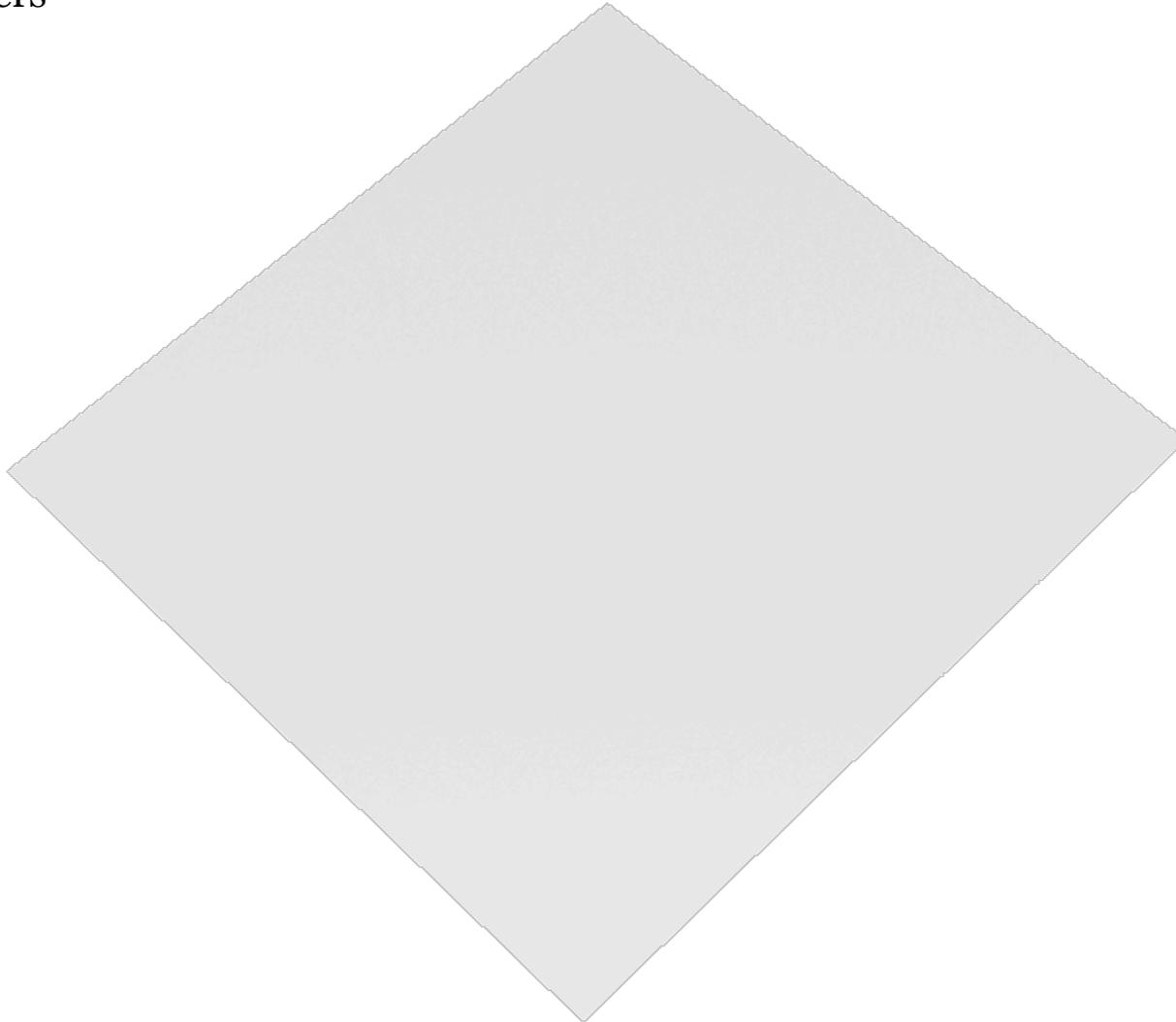


# Front-illuminated imagers



# Front illuminated CMOS

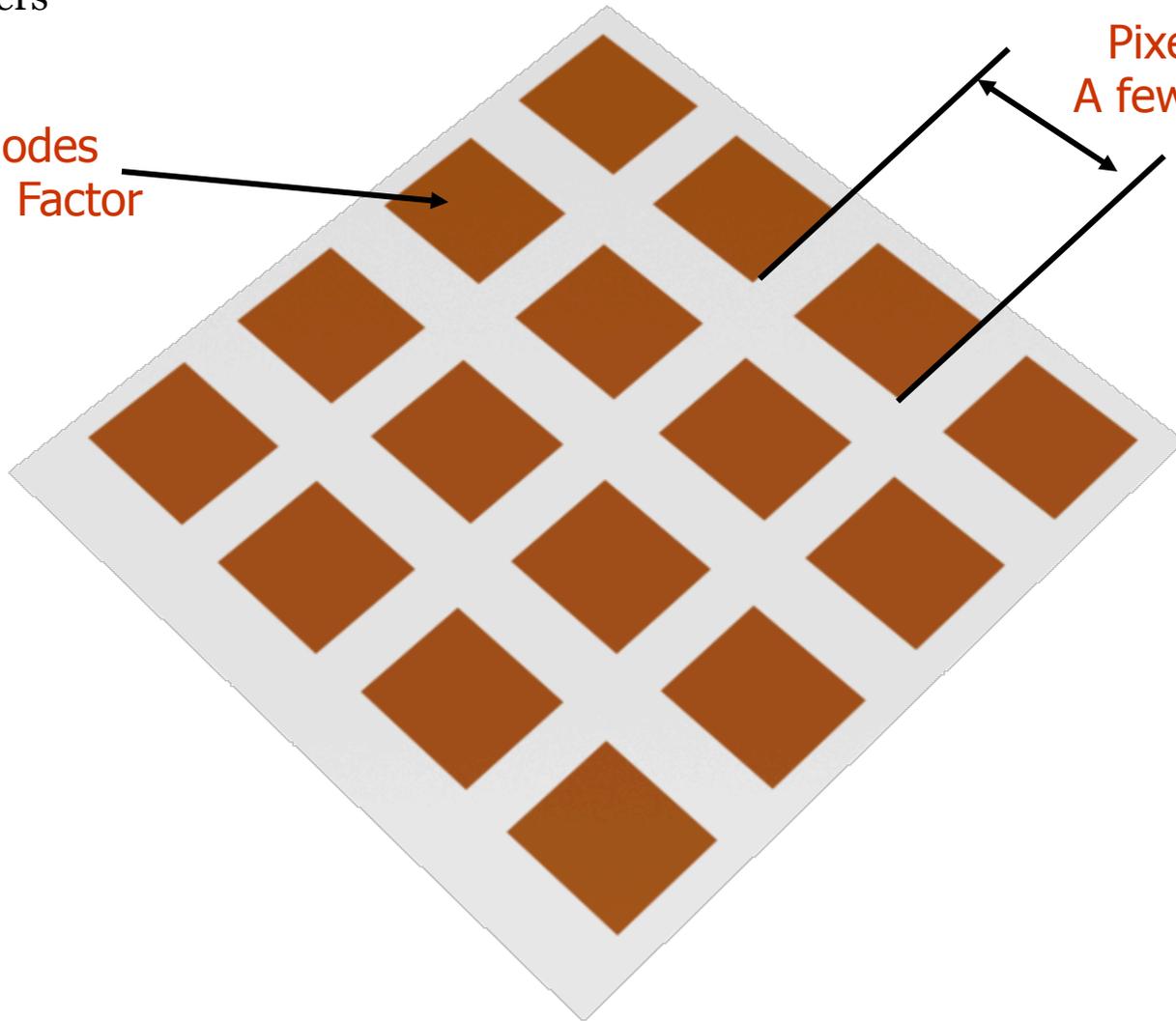
Building up the  
CMOS imager layers



# Building up the CMOS imager layers

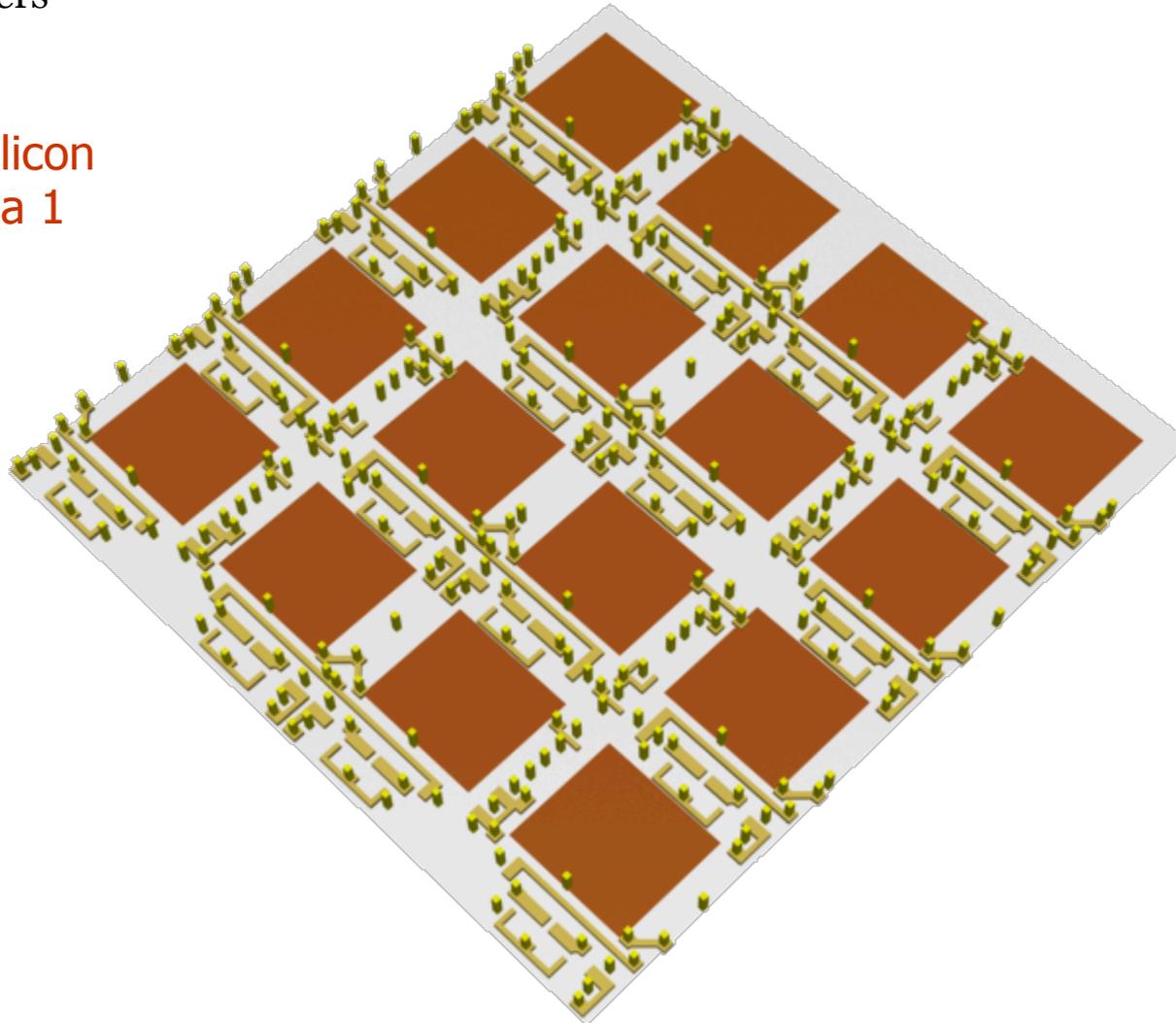
Photodiodes  
~50% Fill Factor

Pixel pitch:  
A few microns

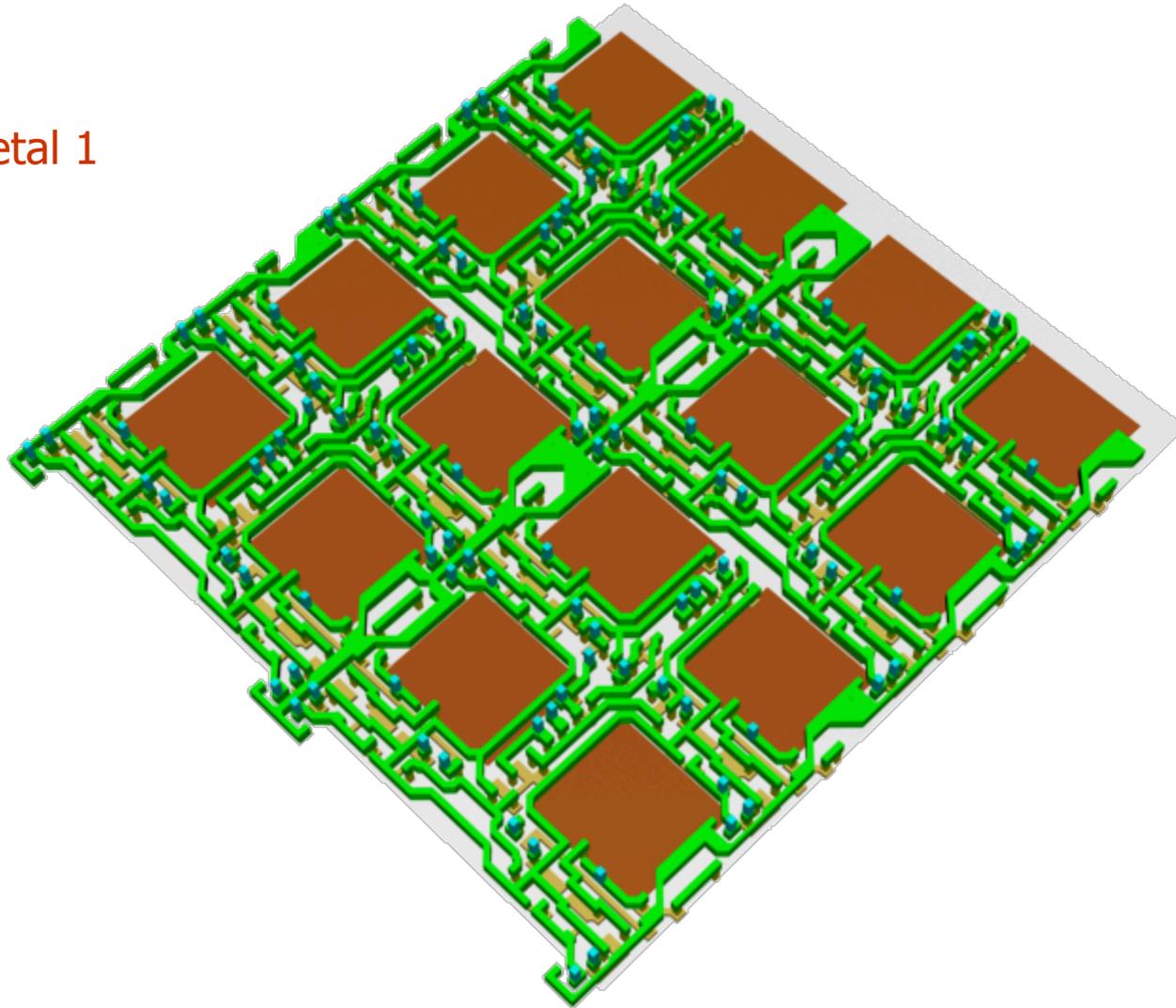


# Building up the CMOS imager layers

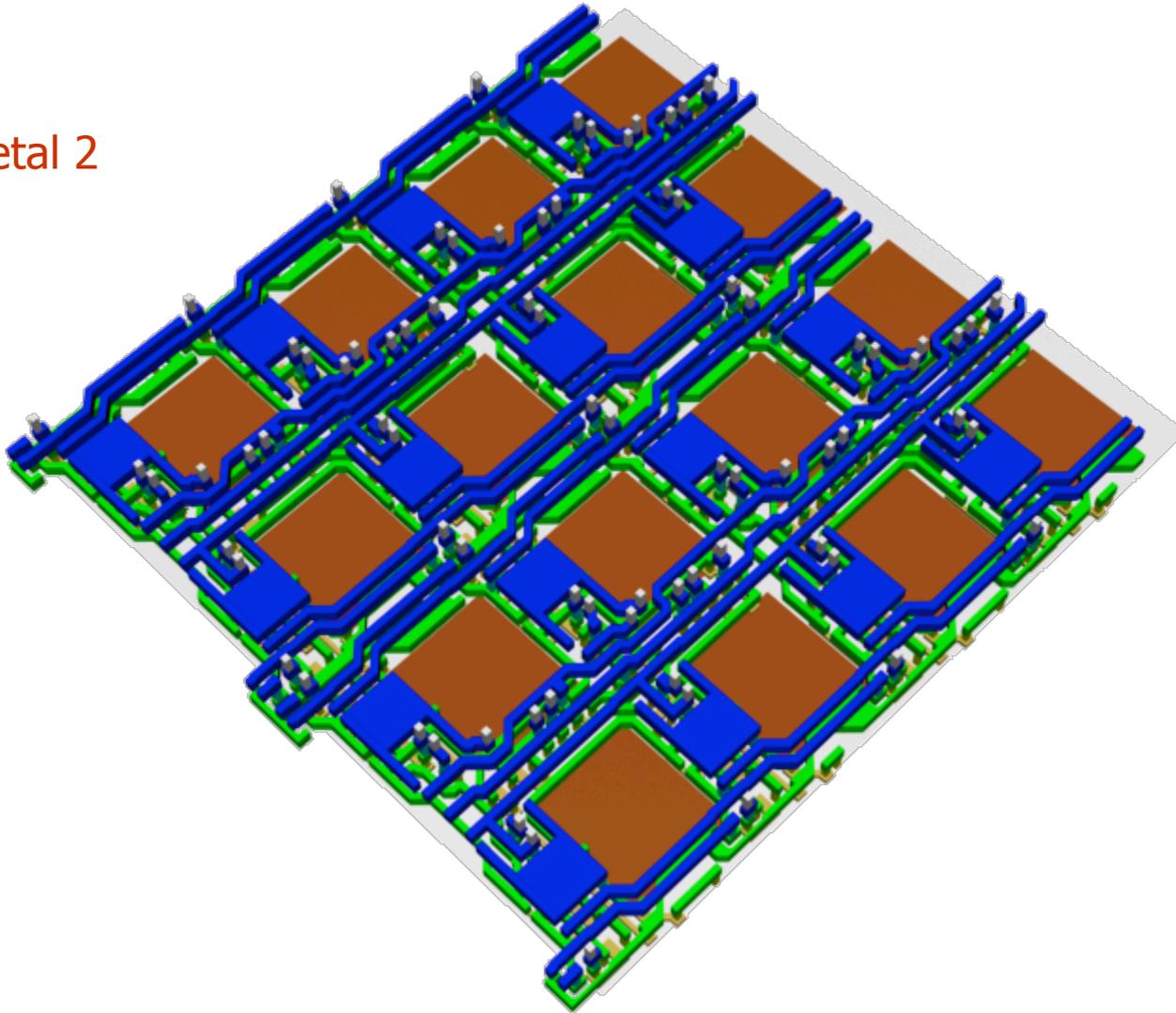
Polysilicon  
& Via 1



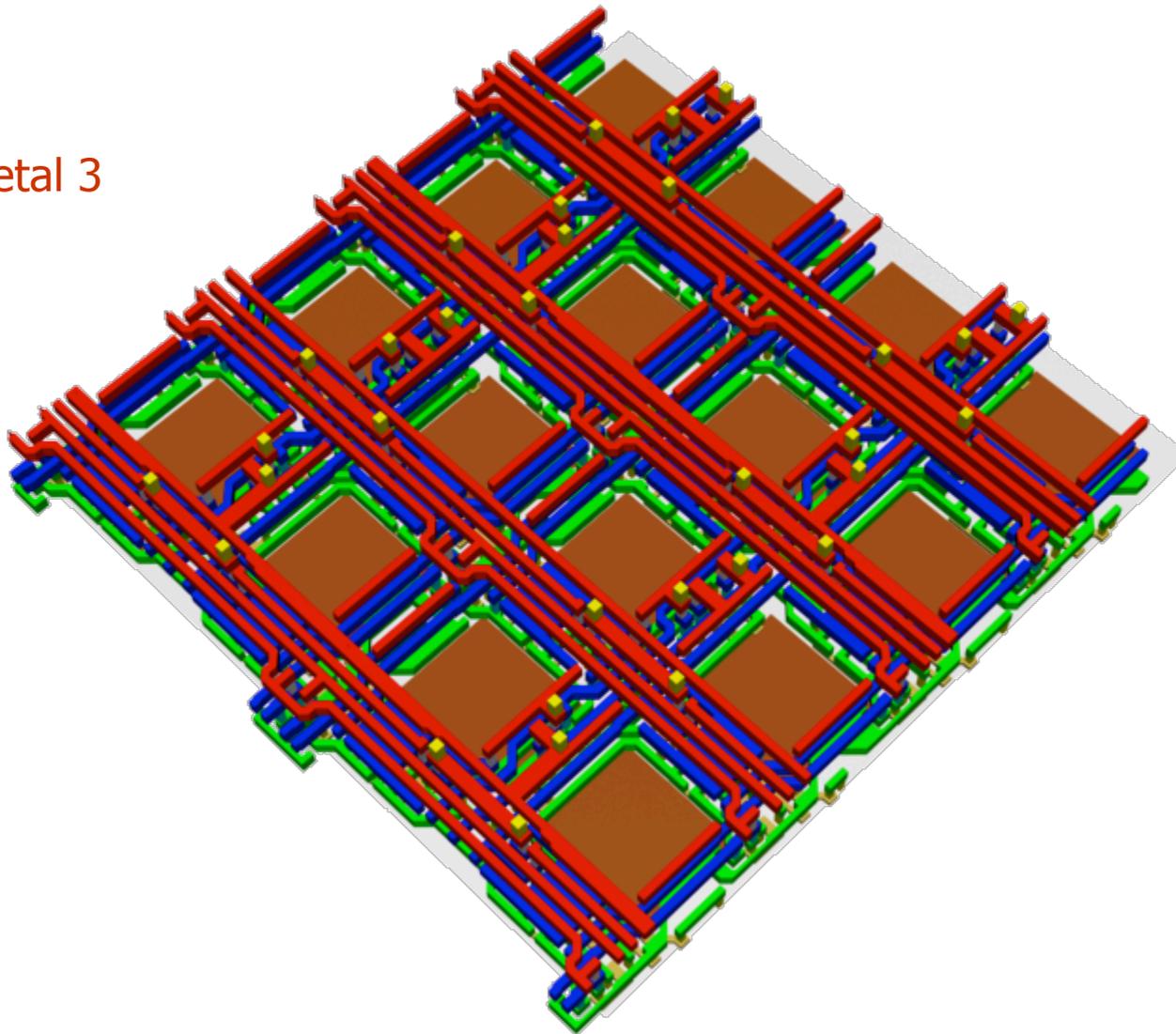
Metal 1



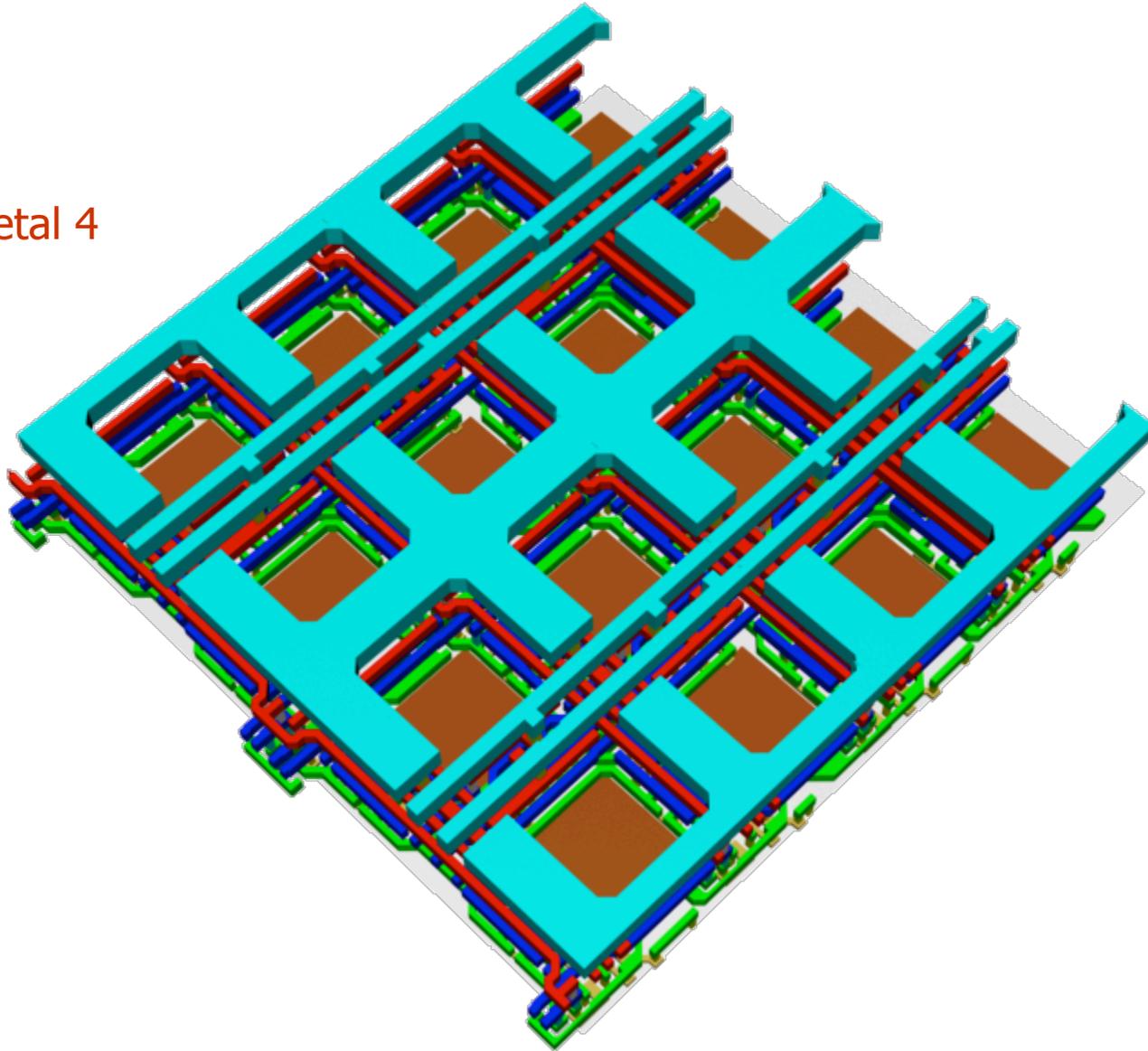
Metal 2



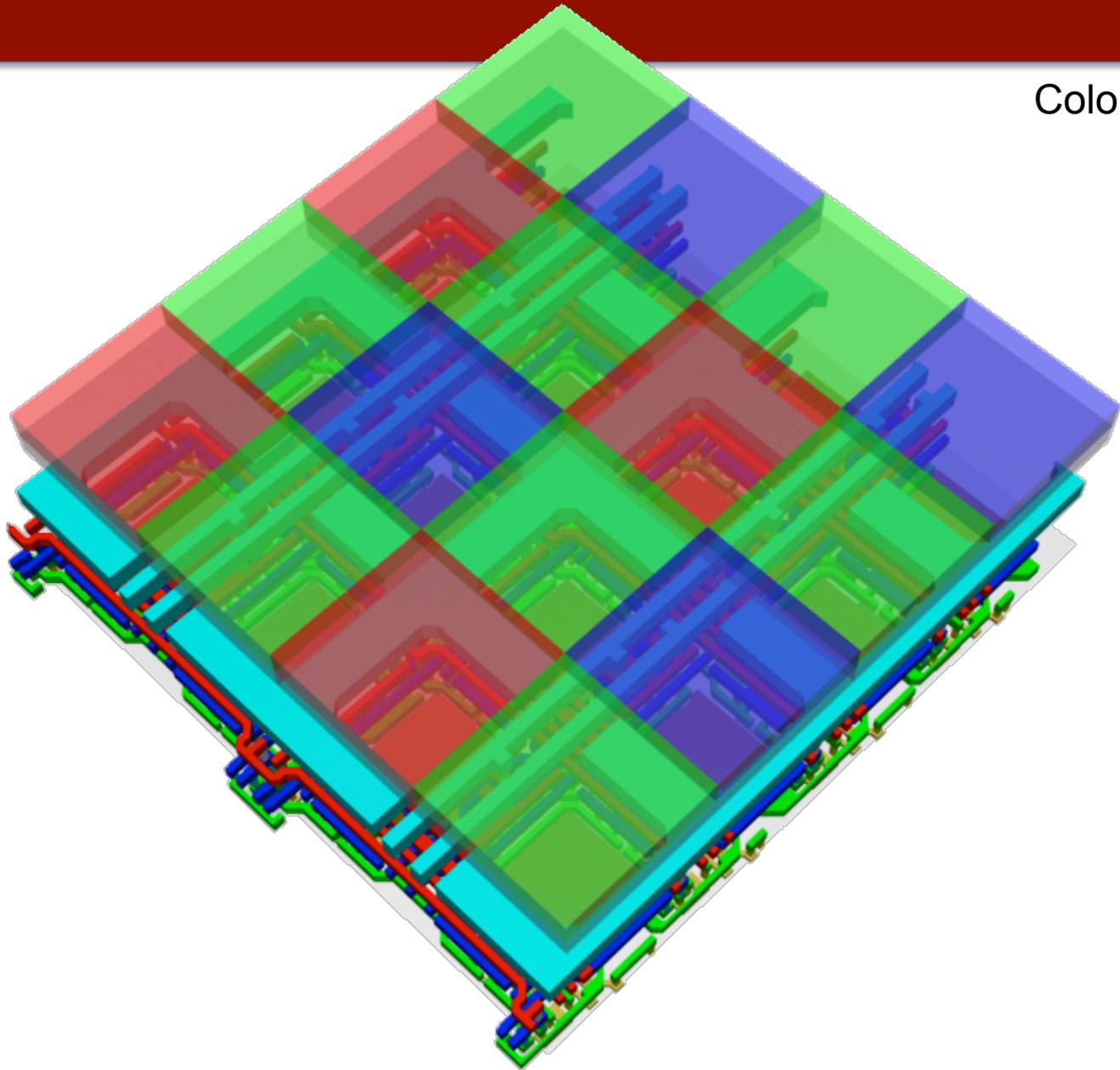
Metal 3



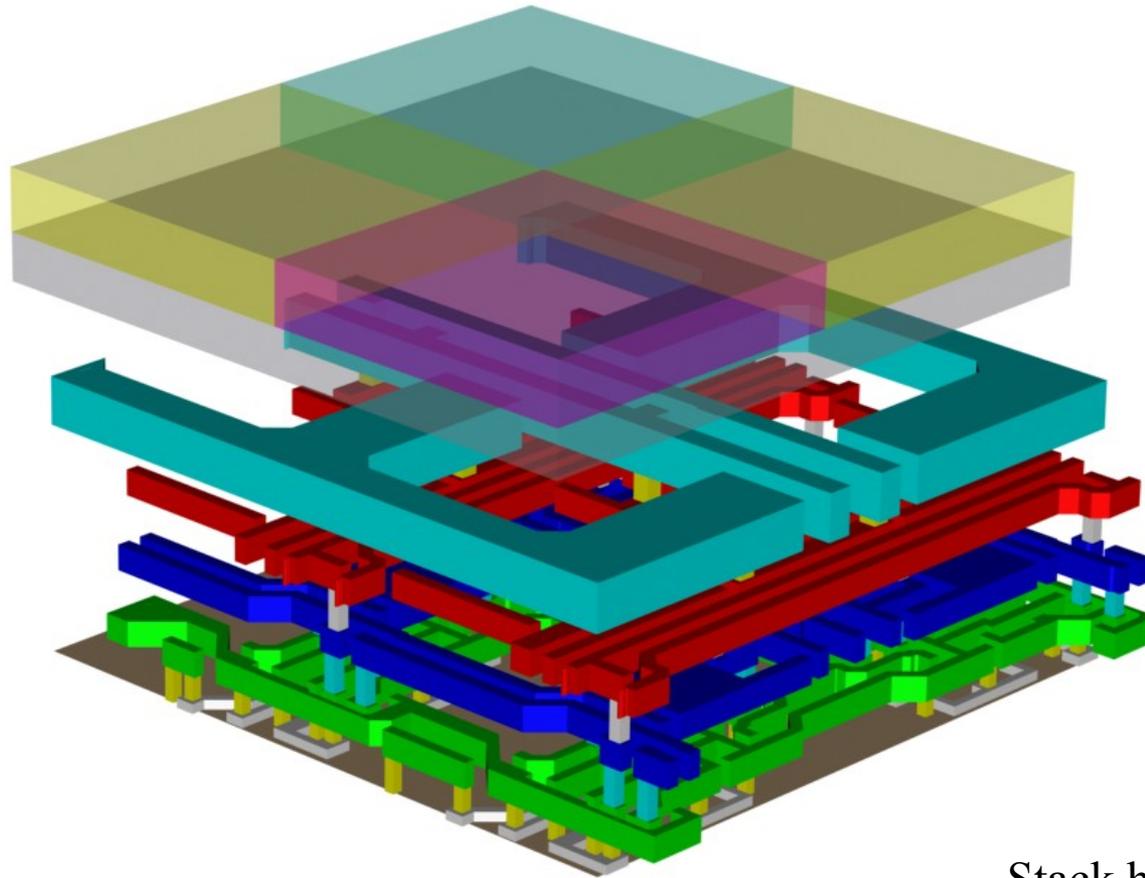
Metal 4



Color filter array



# The pixel stack



CMY Color Filter  
Anti-Reflection Coating

Metal 4

Metal 3

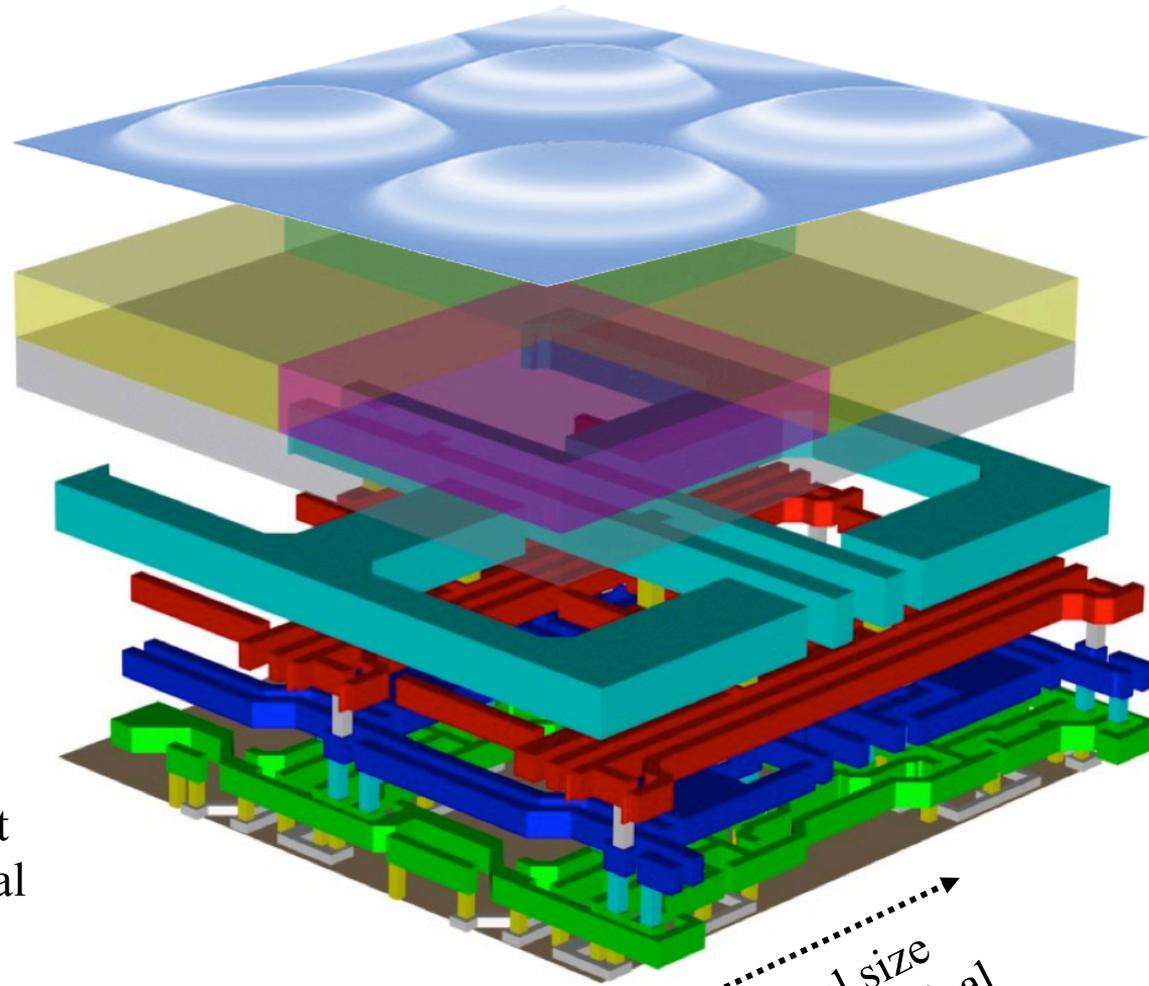
Metal 2

Metal 1

Substrate

Stack height  $\sim 4\mu\text{m}$  is typical  
Pixel size  $\sim 2\mu\text{m}$  is typical

# The microlens array



Microlens array

CMY Color Filter

Anti-Reflection Coating

Metal 4

Metal 3

Metal 2

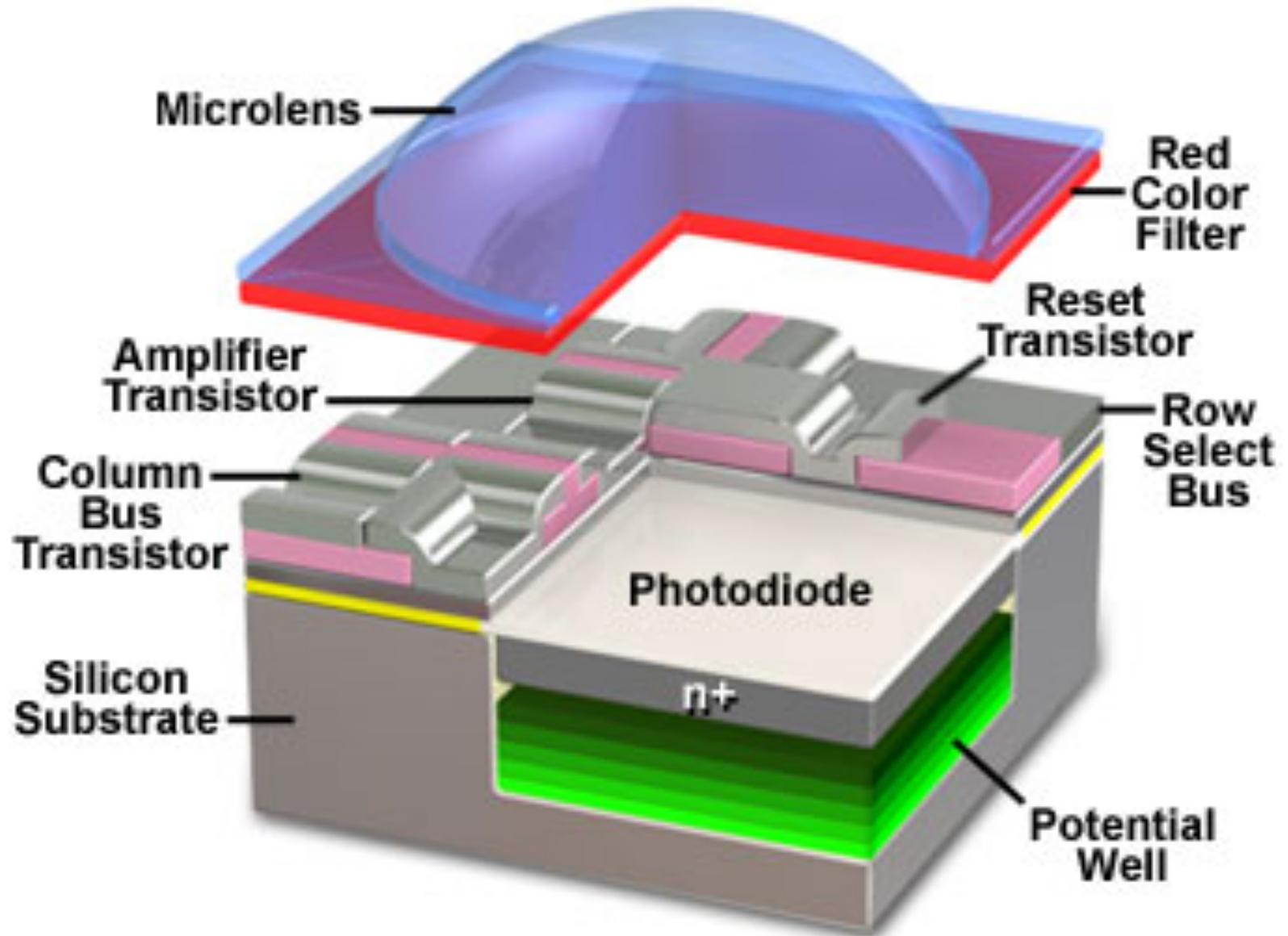
Metal 1

Substrate

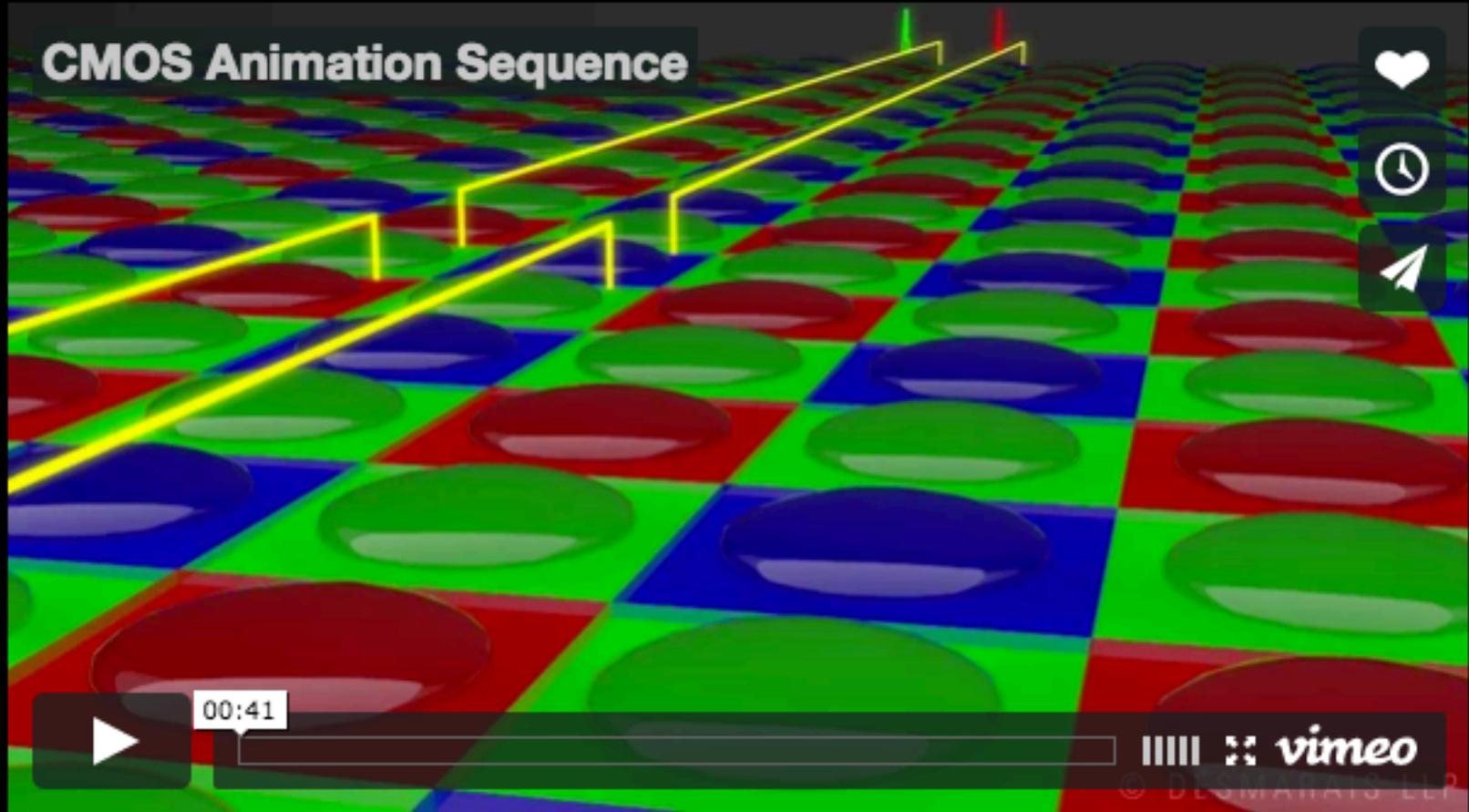
Stack height  
4 $\mu$ m is typical

Pixel size  
2 $\mu$ m is typical

# Anatomy of the Active Pixel Sensor Photodiode



# CMOS graphics description



# Back-illuminated sensors

- Back-illuminated
- Optical cross-talk
- Light sensitivity



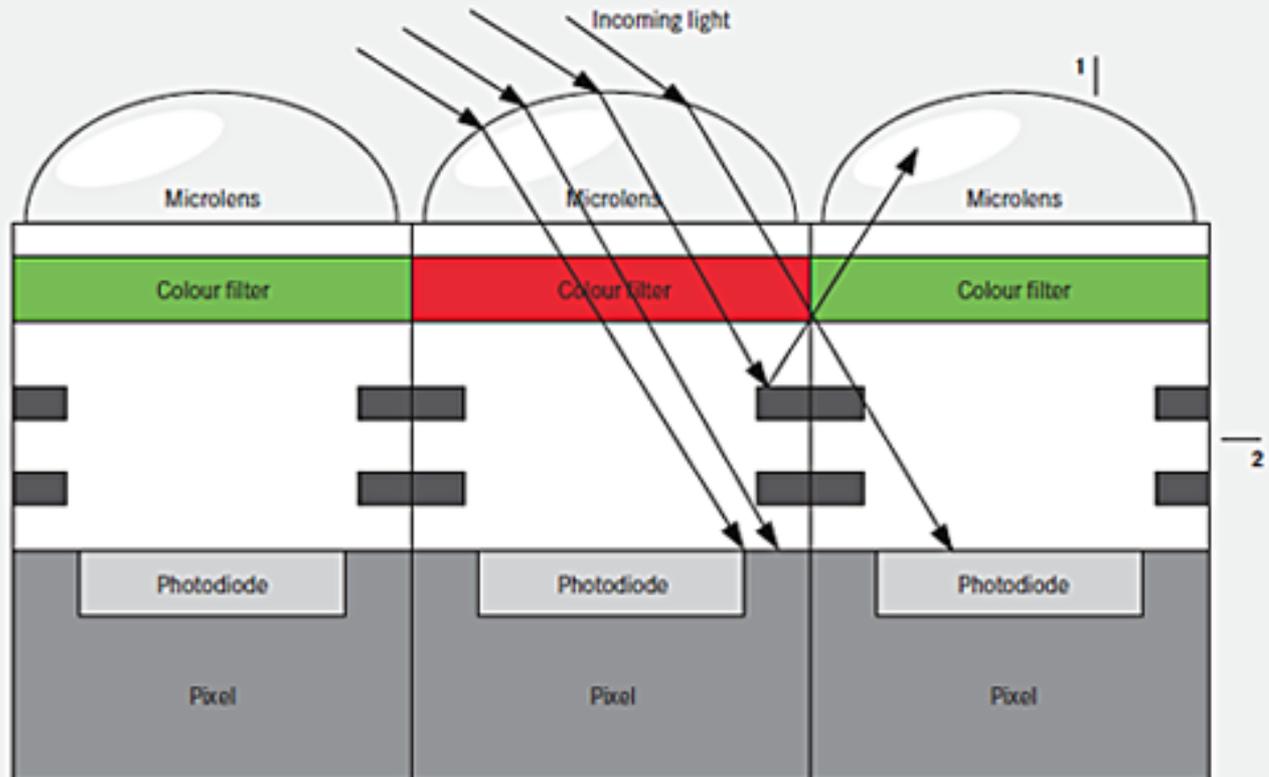
# A problem with front-illuminated

## Optical cross-talk

**Sensor architecture of a standard CMOS sensor**  
(schematic diagram)

1 Microlens design with normal radius

2 Relatively large distance between color filter and photodiode

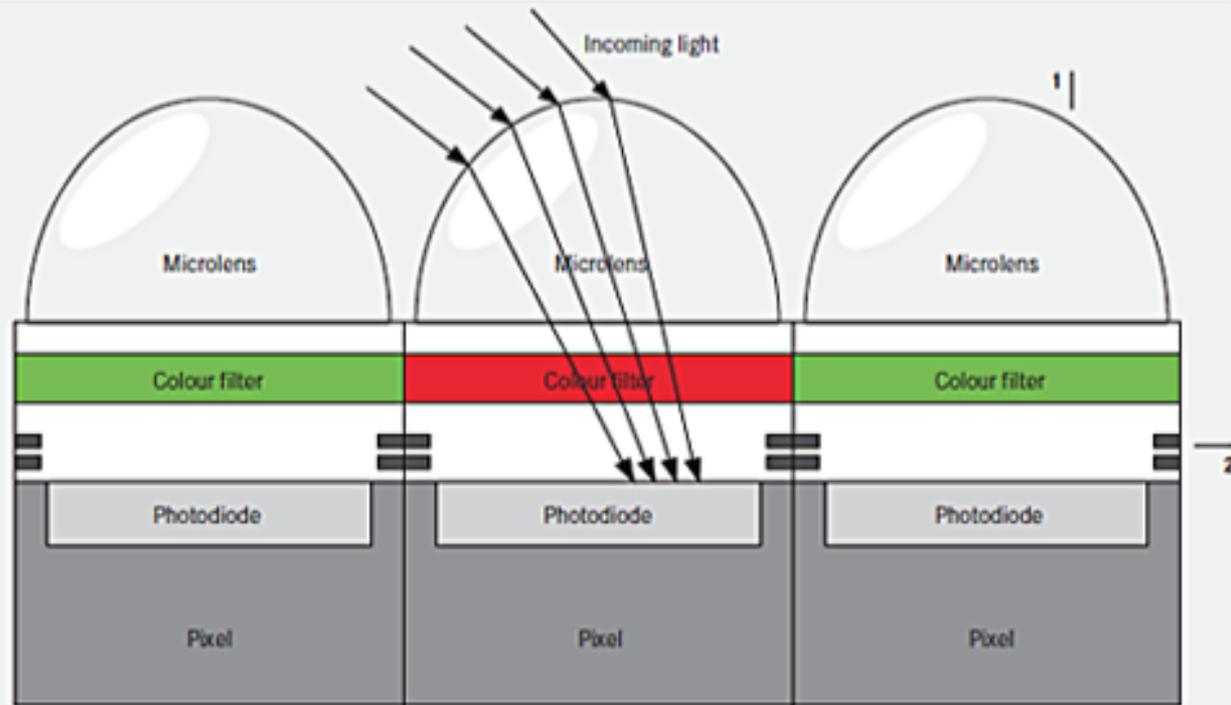


With some CMOS sensors, rays of incoming light at large angles of incidence can fail to reach the photodiode of the corresponding pixel and reach only the adjacent pixel. Or they are shadowed or reflected on the way to the pixel with the effect that the overall amount of light received by the pixels is less than the amount arriving through the microlenses.

# Reducing path length to correct for optical cross-talk

## Sensor architecture of the Leica Max 24 MP sensor (schematic diagram)

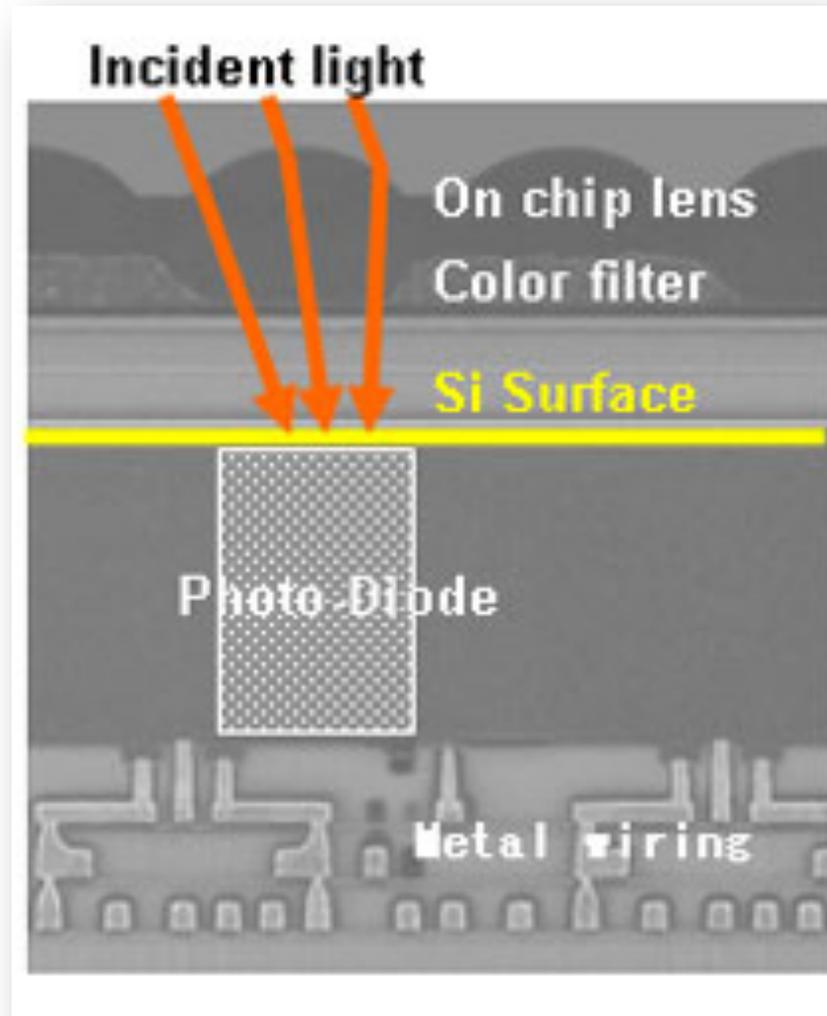
- 1 Microlens design with varying radius
- 2 Relatively short distance between color filter and photodiode



In the case of the Leica Max 24 MP sensor, and in contrast to standard CMOS sensors, even light rays with large angles of incidence, e.g. from wide-angle lenses or large apertures, are captured precisely by the photodiodes of the sensor. This is enabled by the special microlens design and the smaller distance between the colour filter and photodiode, which allows more light to enter the system, and ensures that it falls more directly on the respective photodiodes.

# Back-illuminated (BI) CMOS sensor

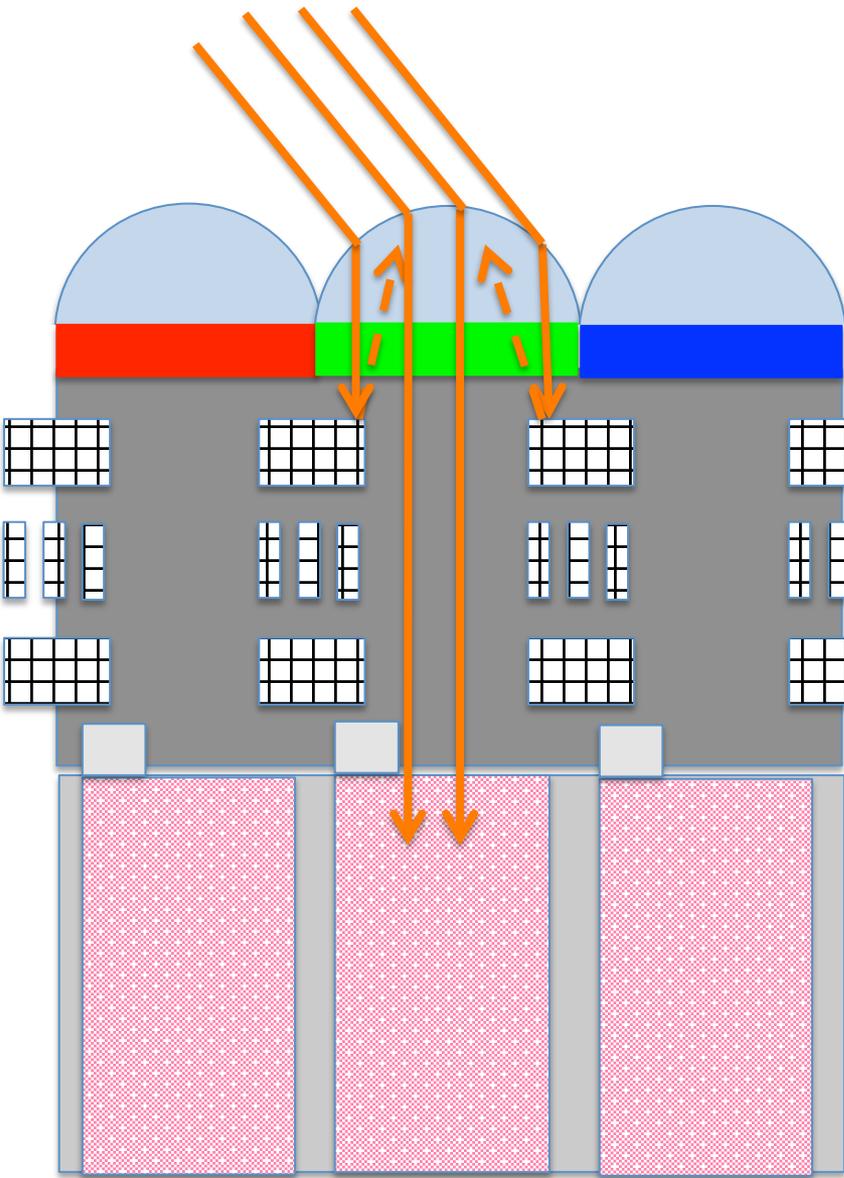
Also called Back-side illumination (BSI)



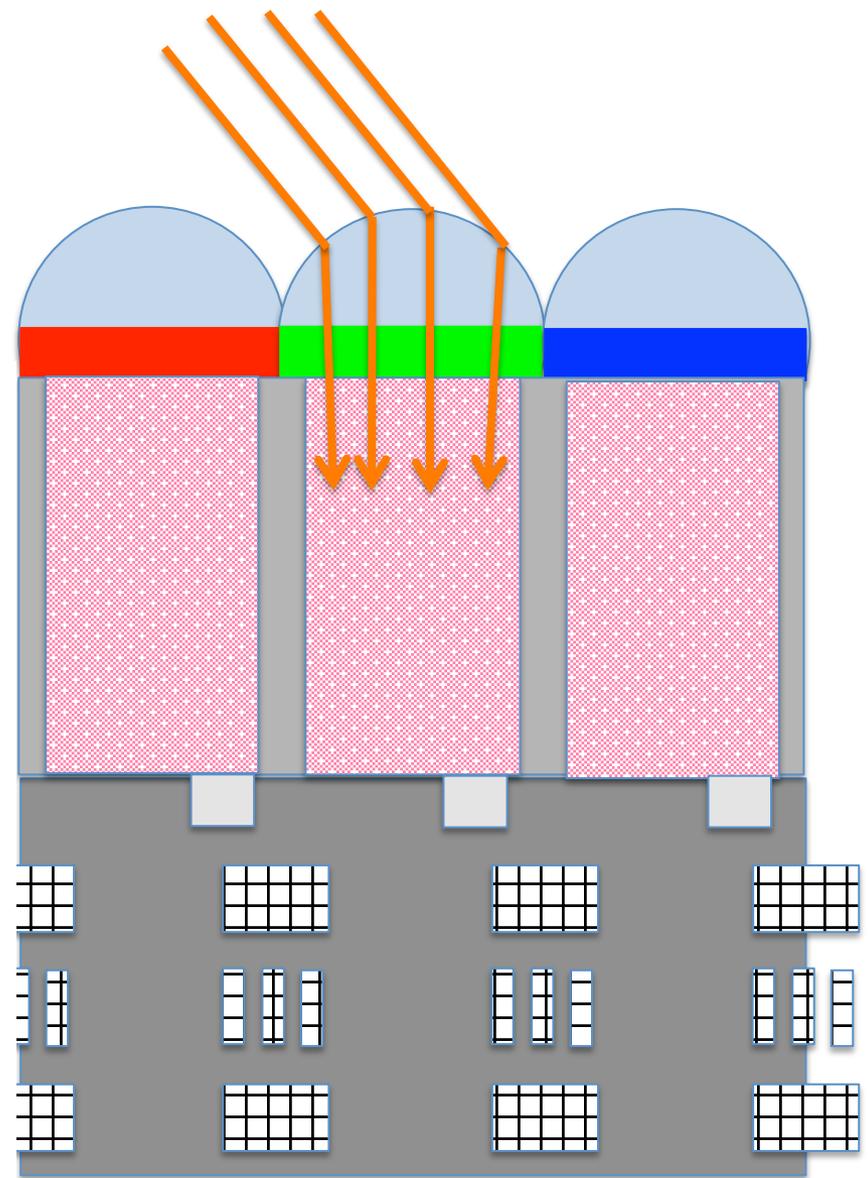
Silicon substrate

Metal layers

# Front vs. Back illuminated

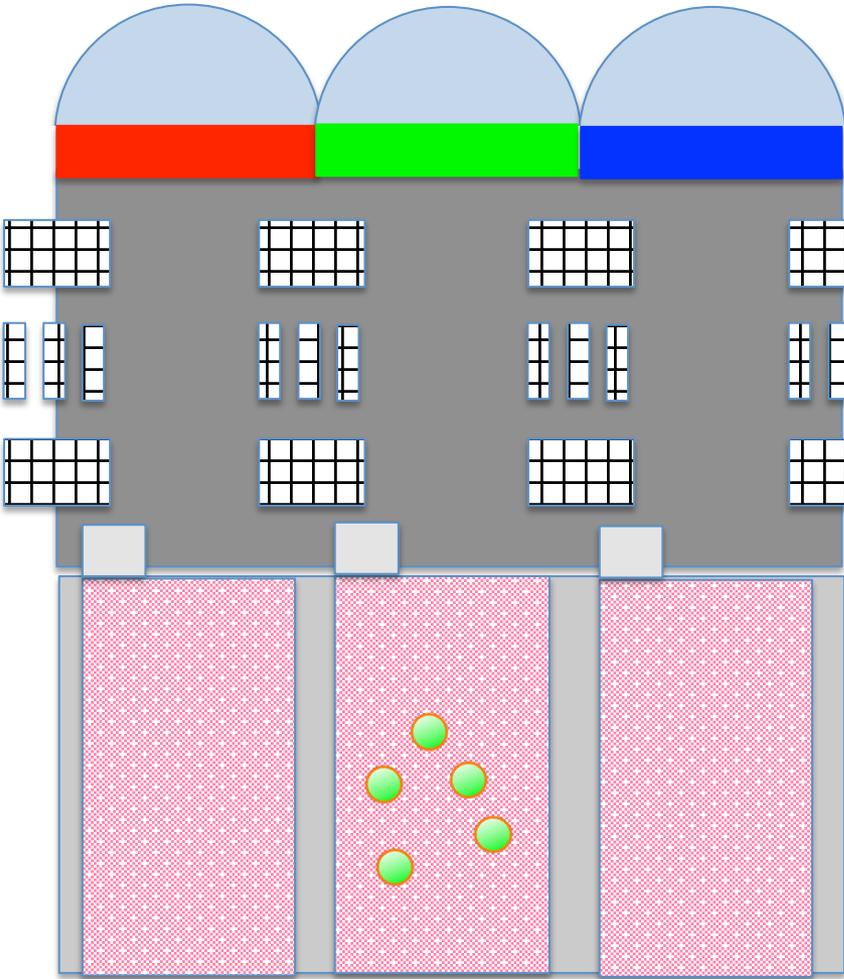


Front illuminated

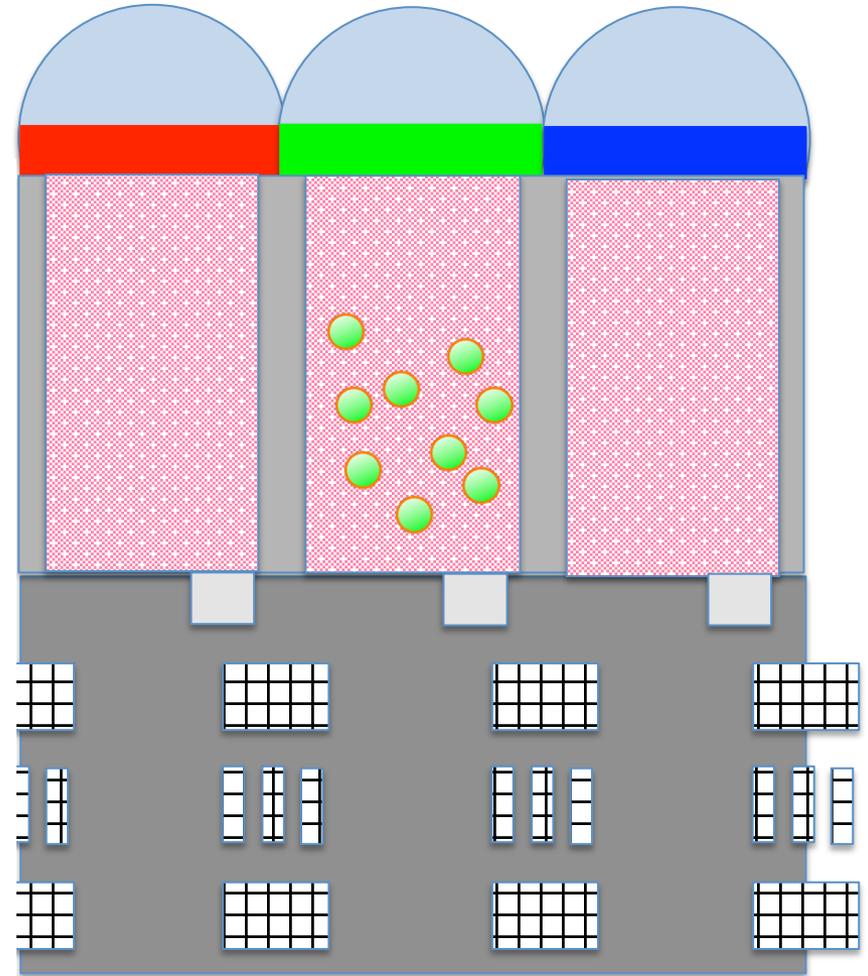


Back illuminated

# Front vs. Back illuminated

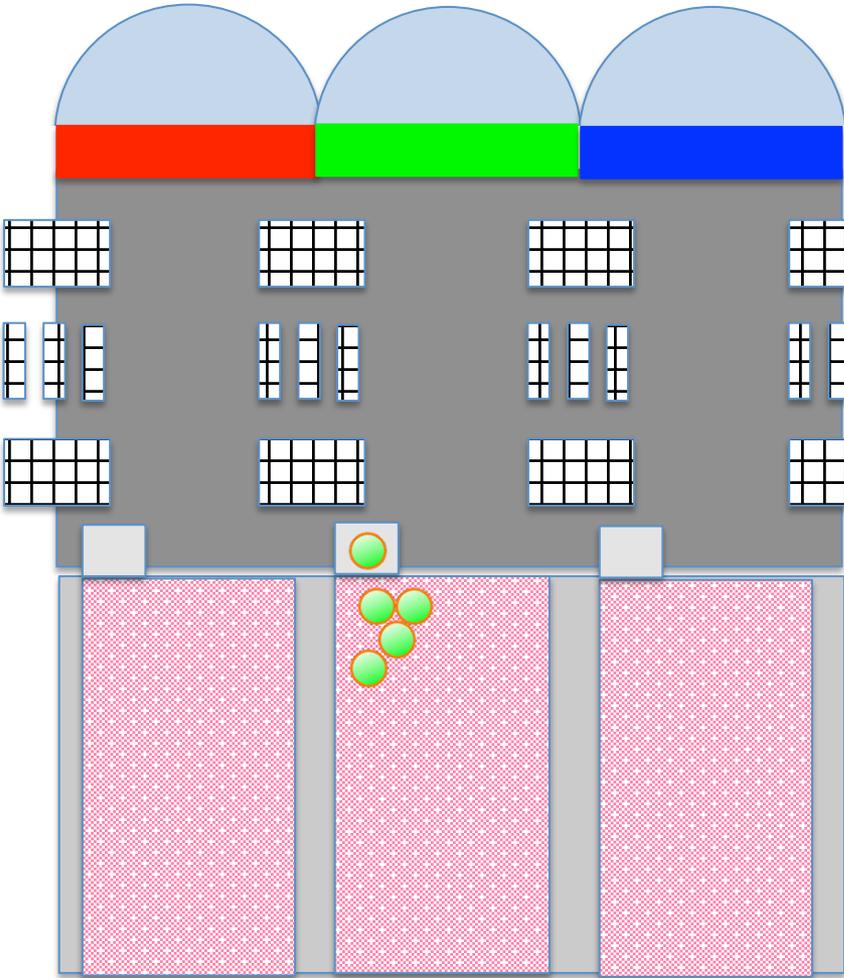


Front illuminated

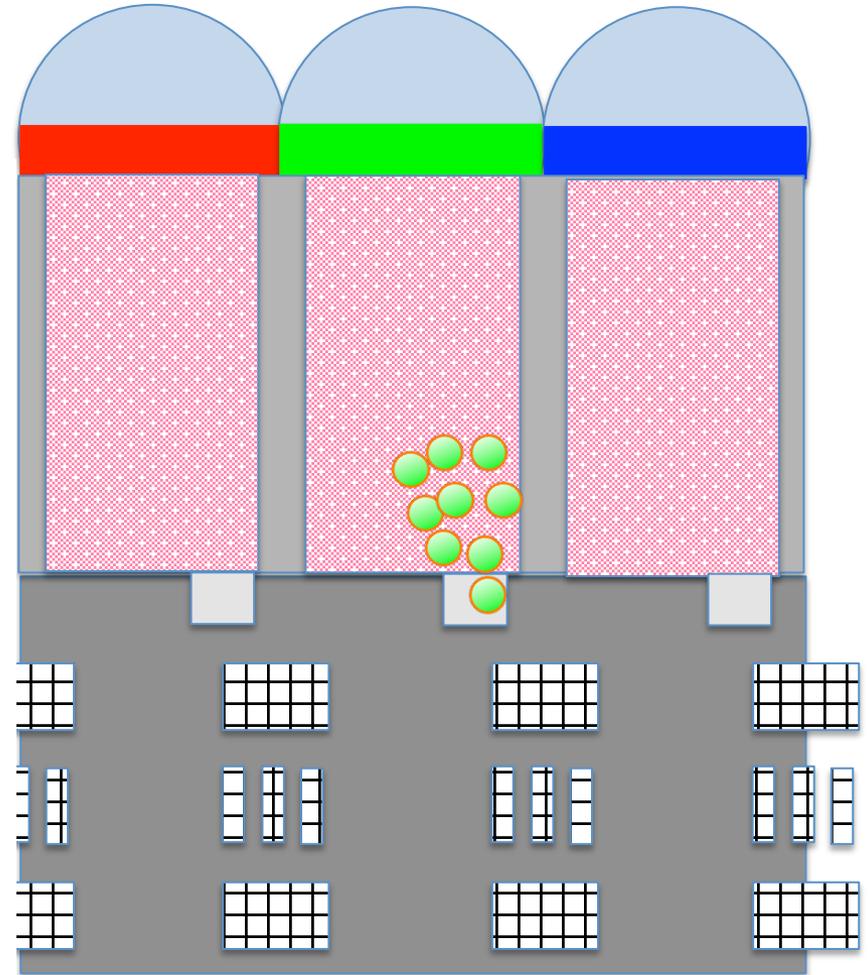


Back illuminated

# Front vs. Back illuminated



Front illuminated



Back illuminated

At equal exposure durations, more photons are captured

Sony comparison of backside illuminated CMOS



Front-illuminated structure

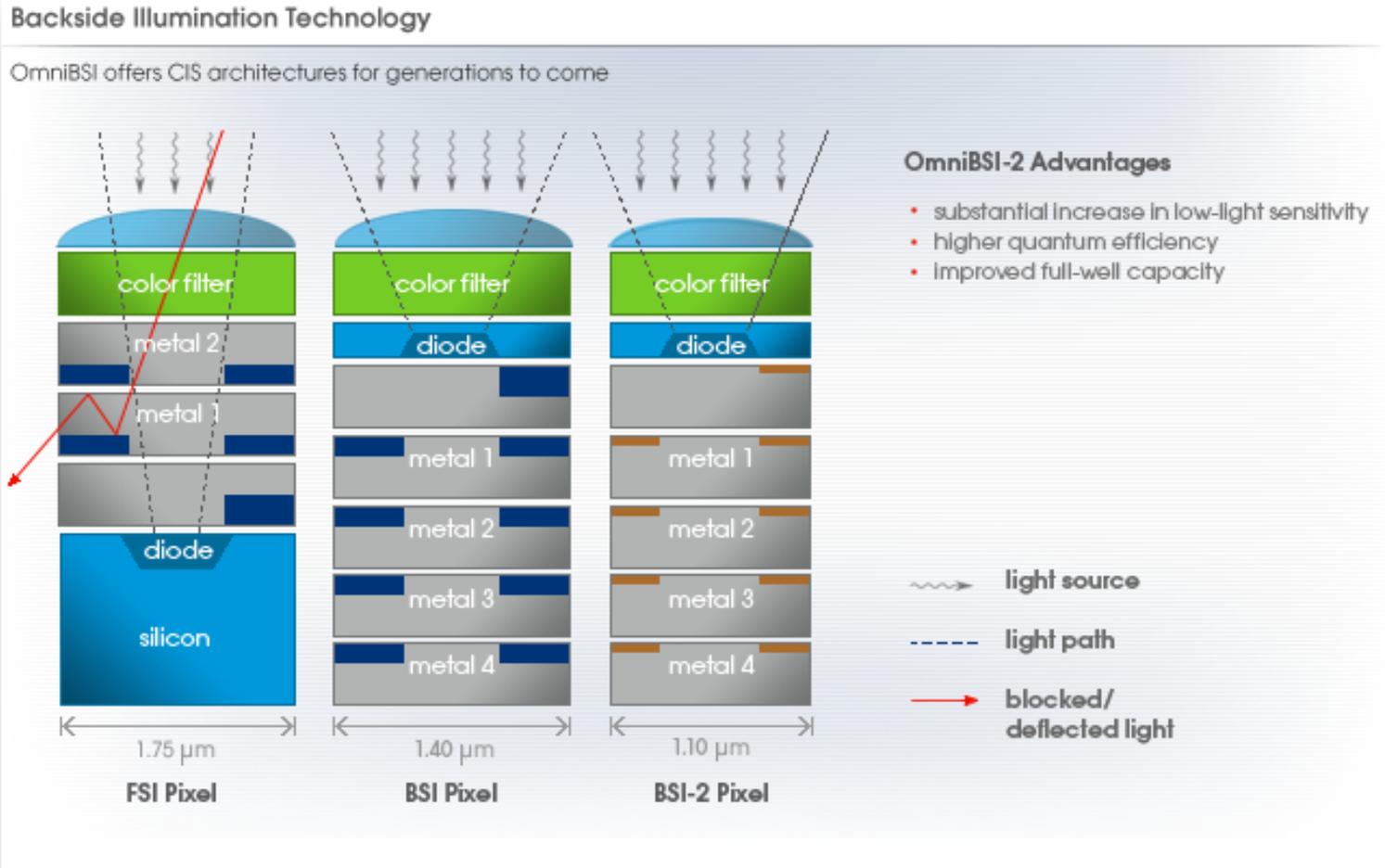


Back-illuminated structure

# Back illuminated sensor

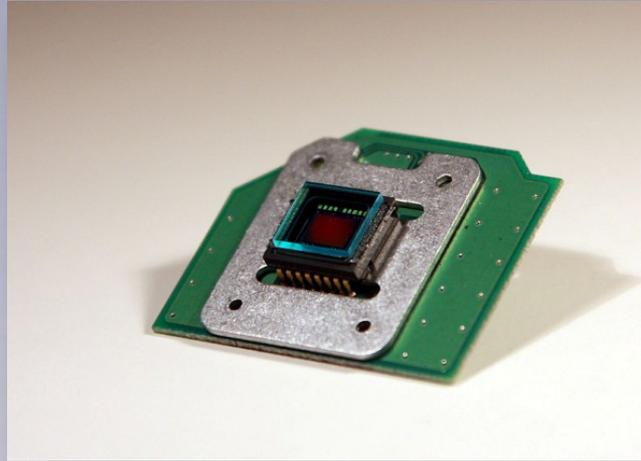
More metal layers for processing without interfering with light capture

Or, thinner form factor for mobile devices



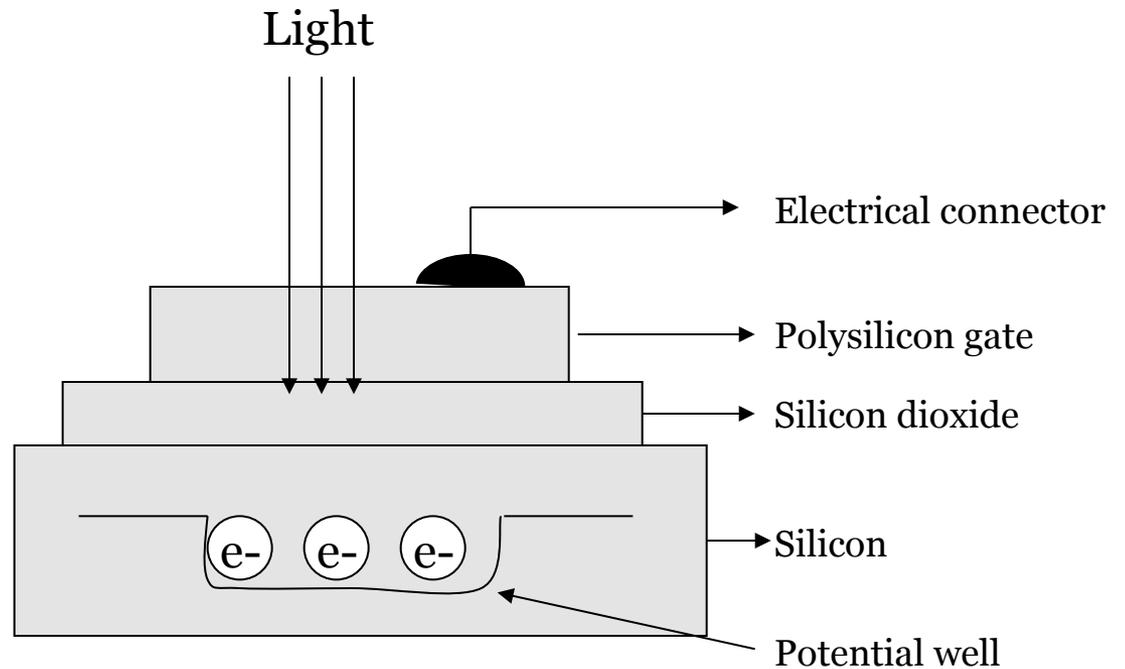
# CCD imagers

- Charge transfer ideas
- Architectures
- Correlated double sampling



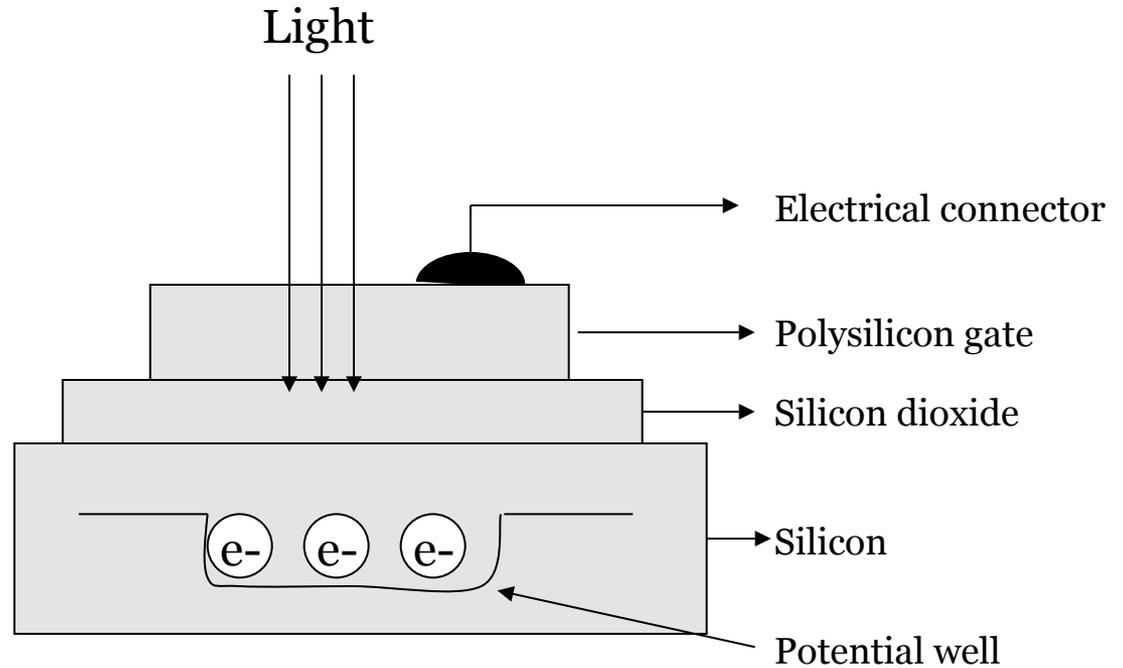
# A few moments for the venerable CCD

Invented in the 1970s as memory devices; light sensitive properties were exploited for imaging applications; a major revolution in Astronomy.

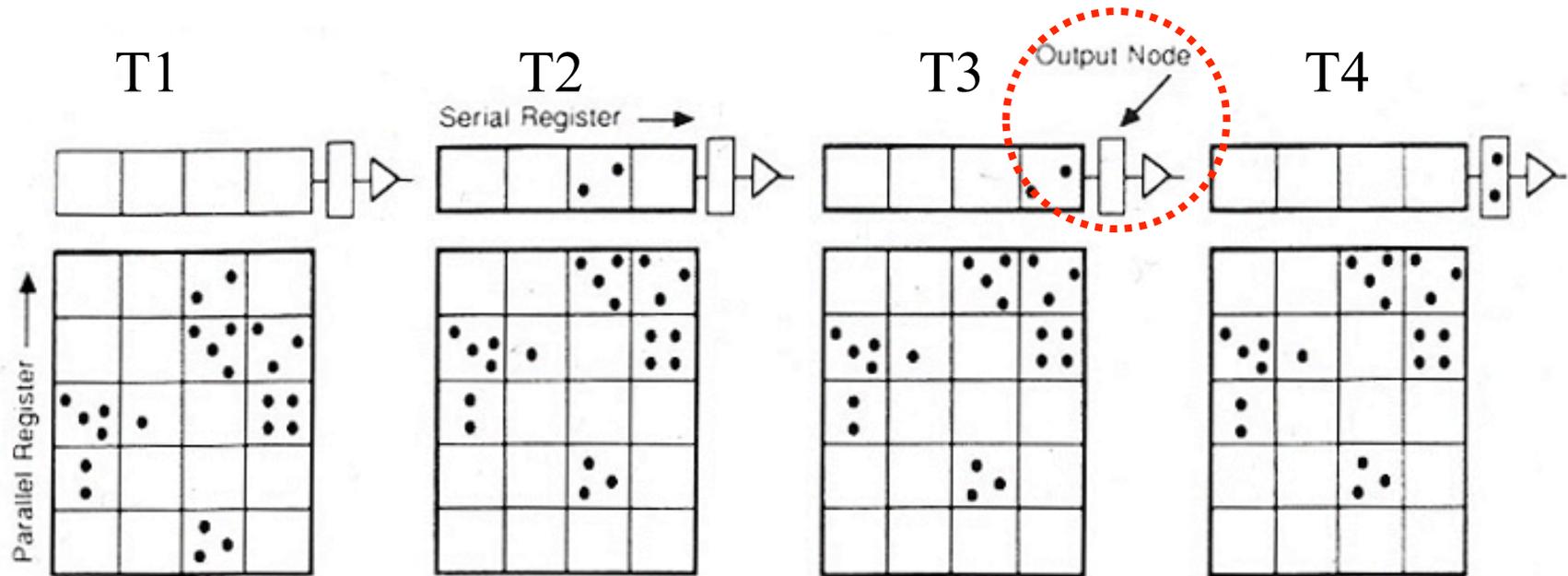


# A few moments for the venerable CCD

They improved the light gathering power of telescopes by almost two orders of magnitude. In 2001 an amateur astronomer with a CCD camera and a 15 cm telescope collects as much light as an astronomer of the 1960s equipped with a photographic plate and a 1m telescope.



# CCD Charge transfer

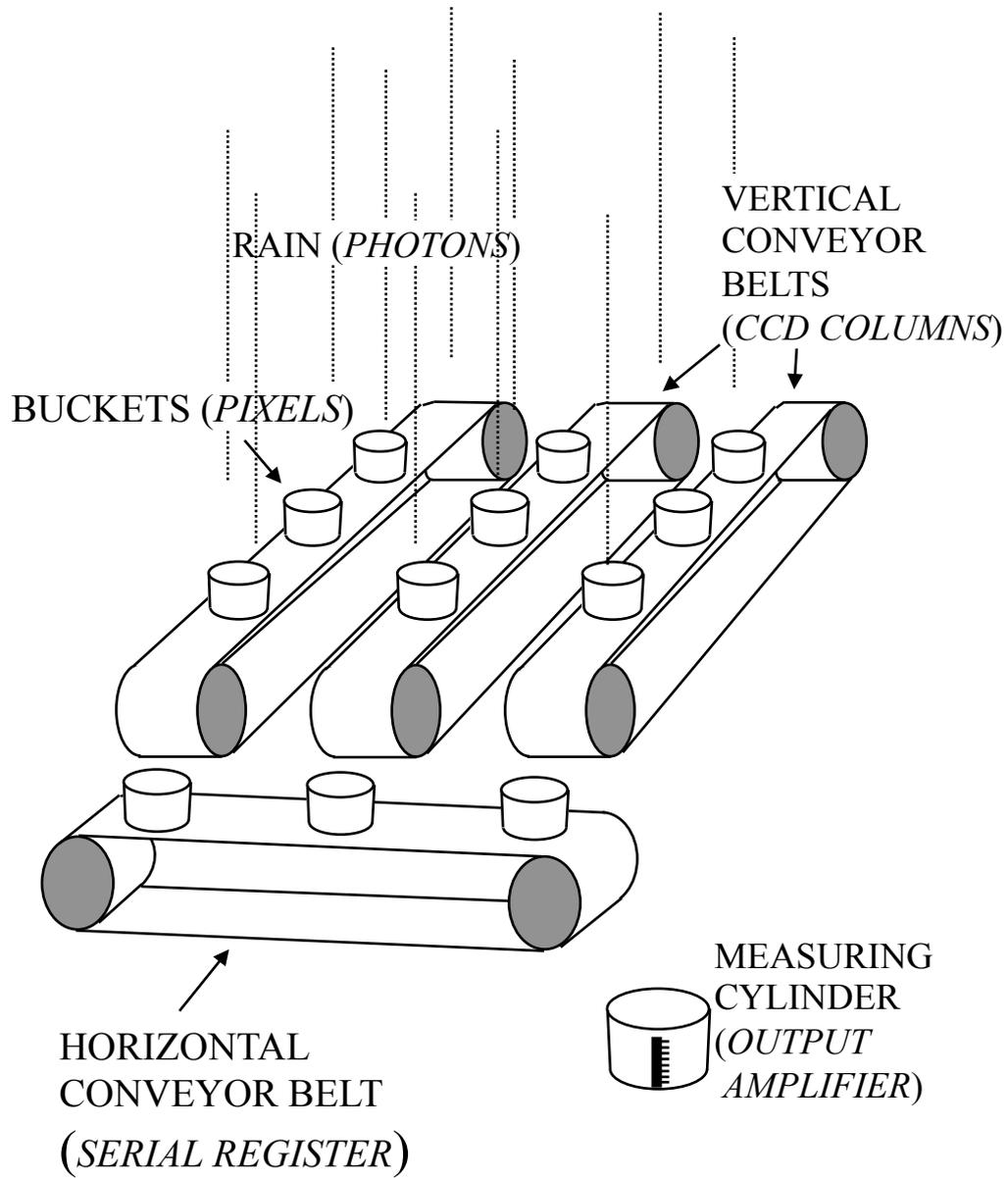


The CCD is exposed to light. An electronic image accumulates as a pattern of charge in the parallel register. The CCD is ready to be read out

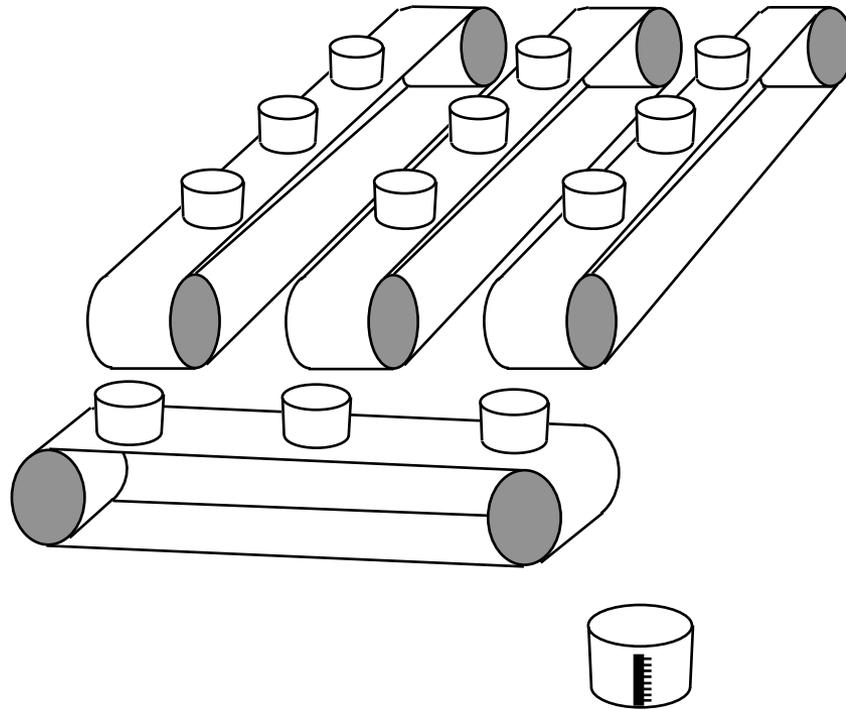
All rows are shifted in parallel. The top row is shifted into the serial register

Once in the serial register, pixels are individually shifted toward the output node

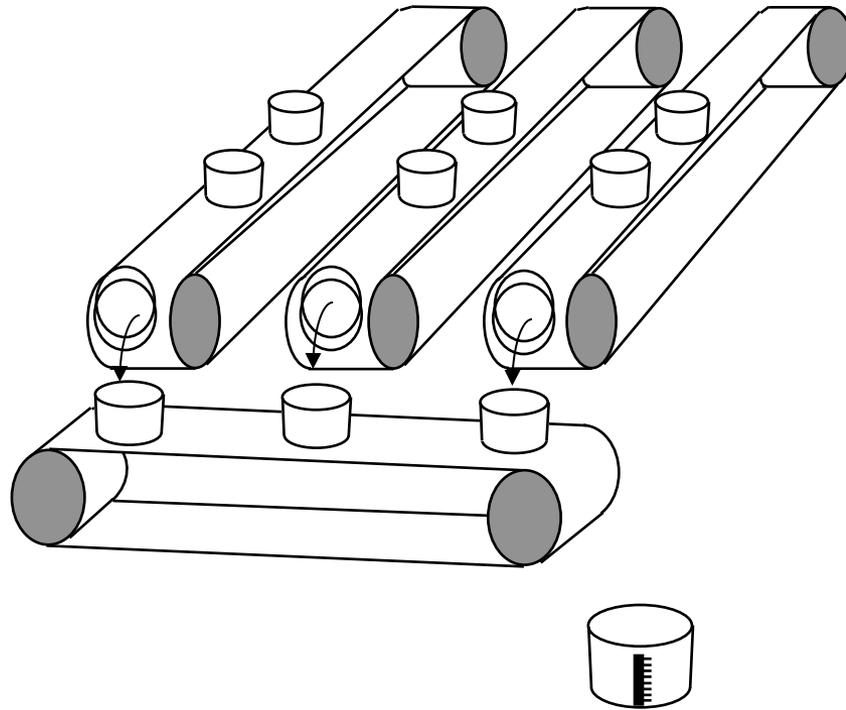
The next row can be shifted into the serial register after that register is cleared



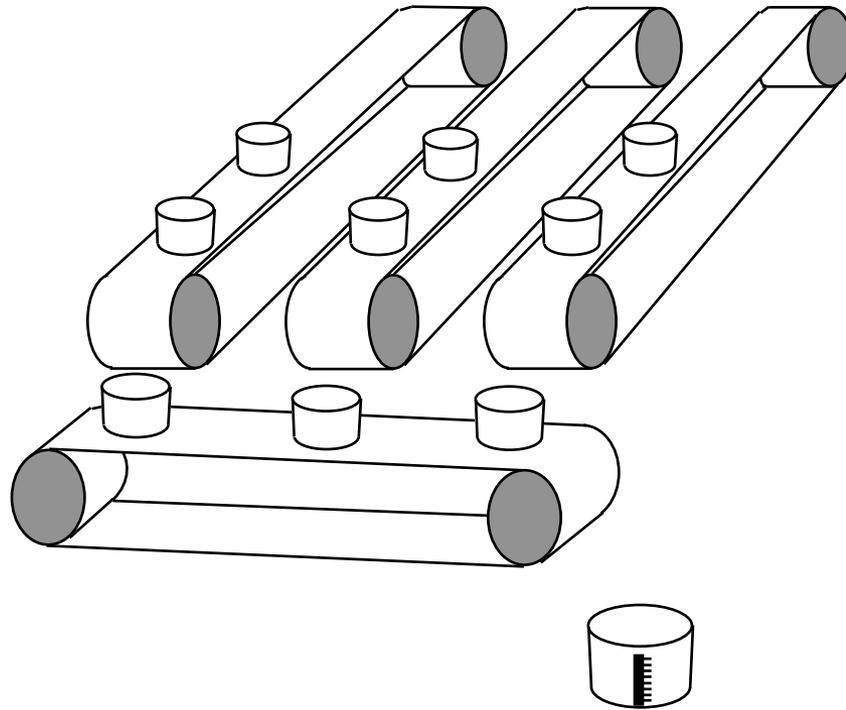
Exposure finished, buckets now contain samples of rain.



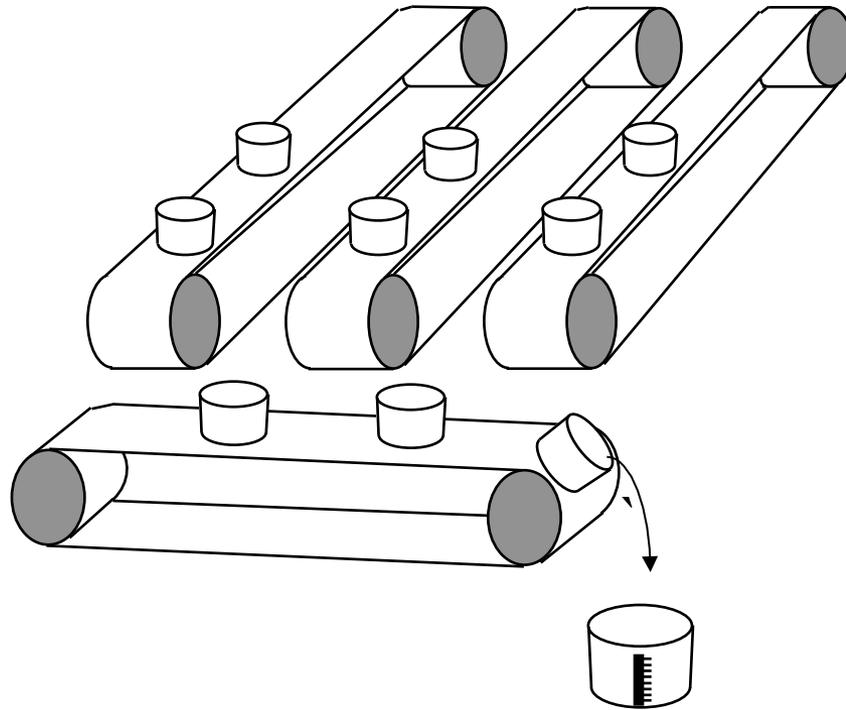
Conveyor belt starts turning and transfers buckets. Rain collected on the vertical conveyor is tipped into buckets on the horizontal conveyor.

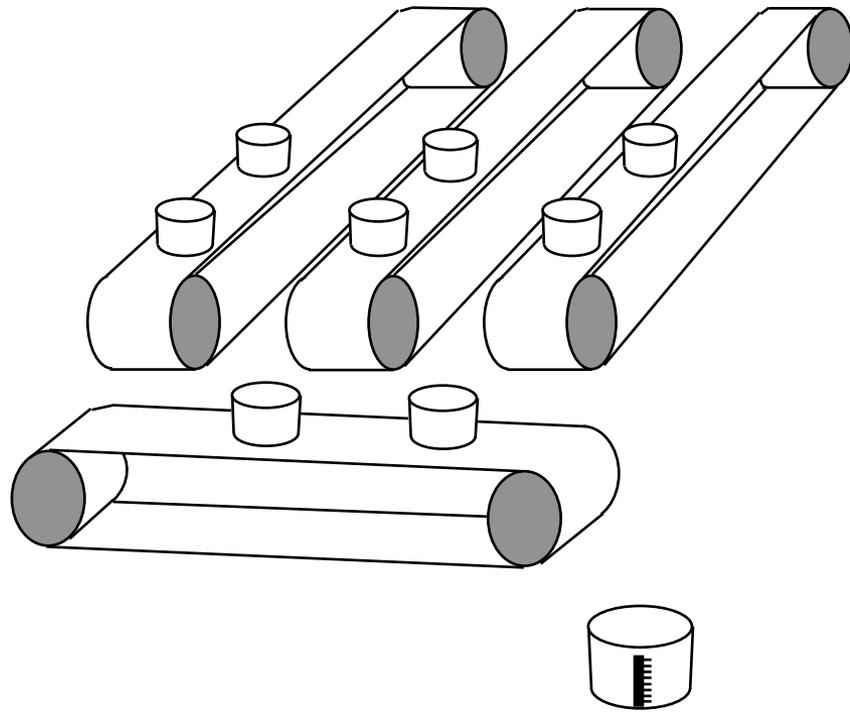


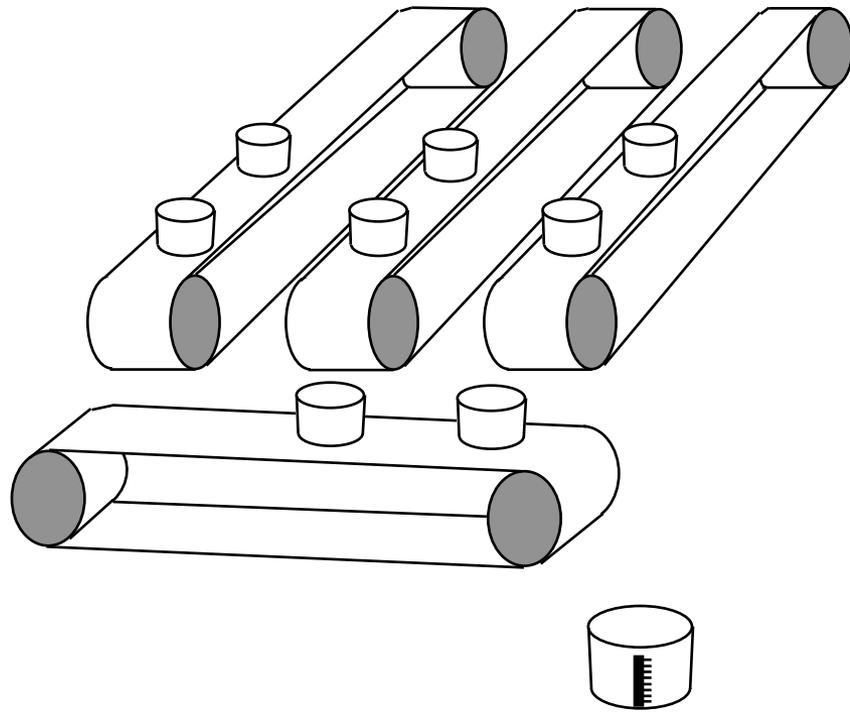
Vertical conveyor stops. Horizontal conveyor starts up and tips each bucket in turn into the measuring cylinder .

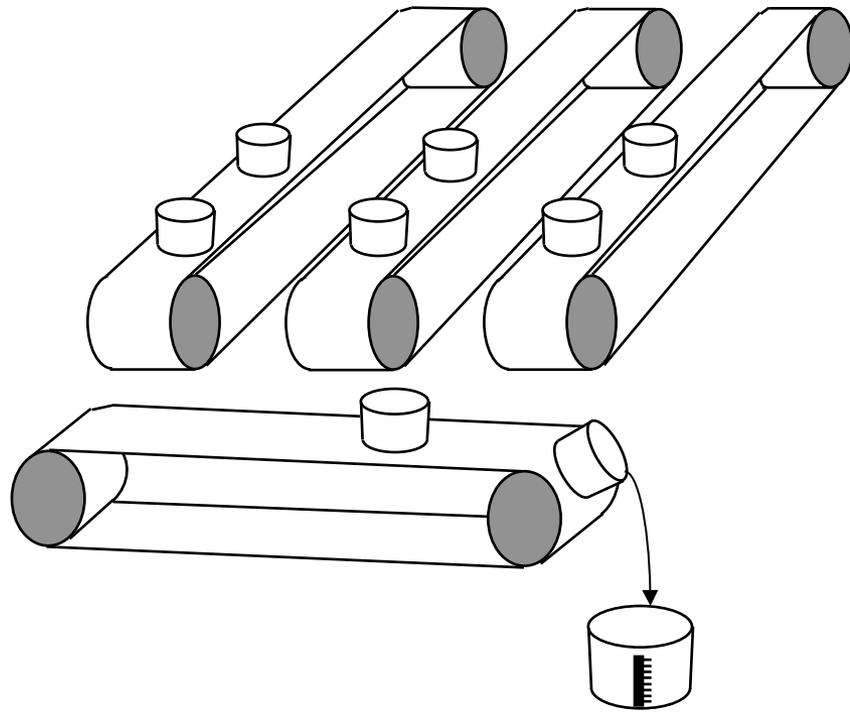


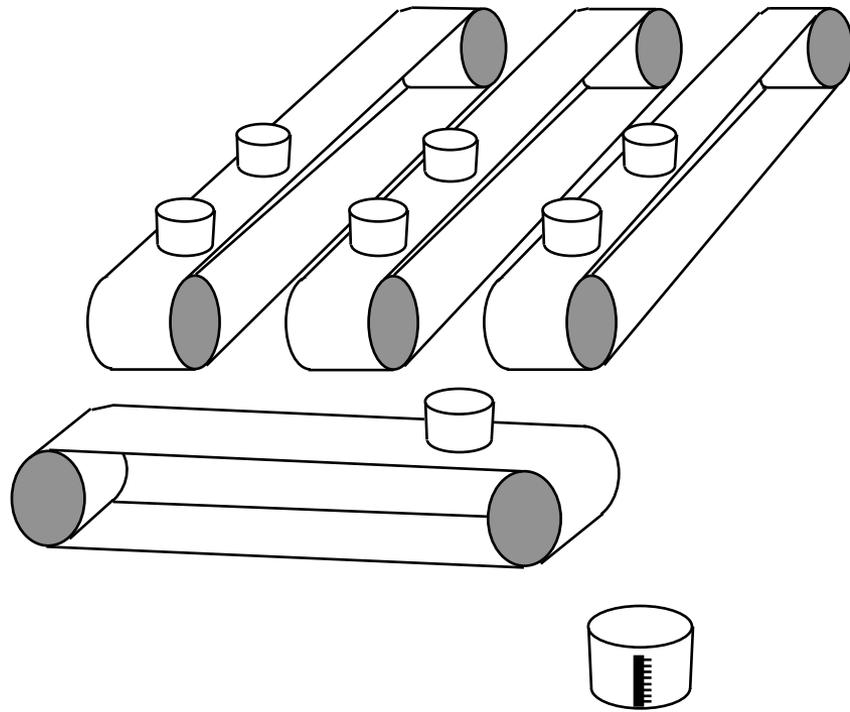
After each bucket has been measured, the measuring cylinder is emptied , ready for the next bucket load.

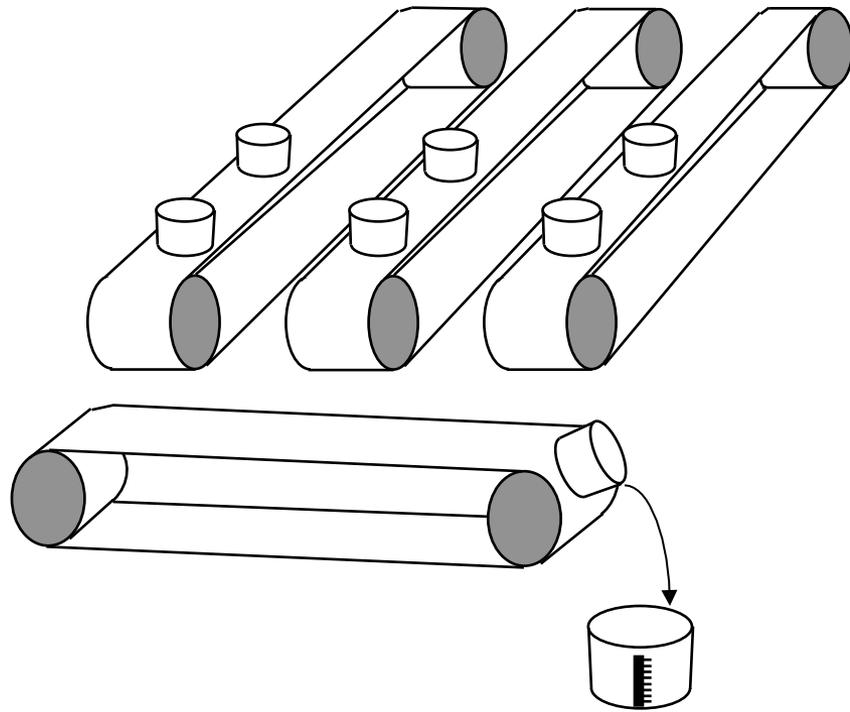


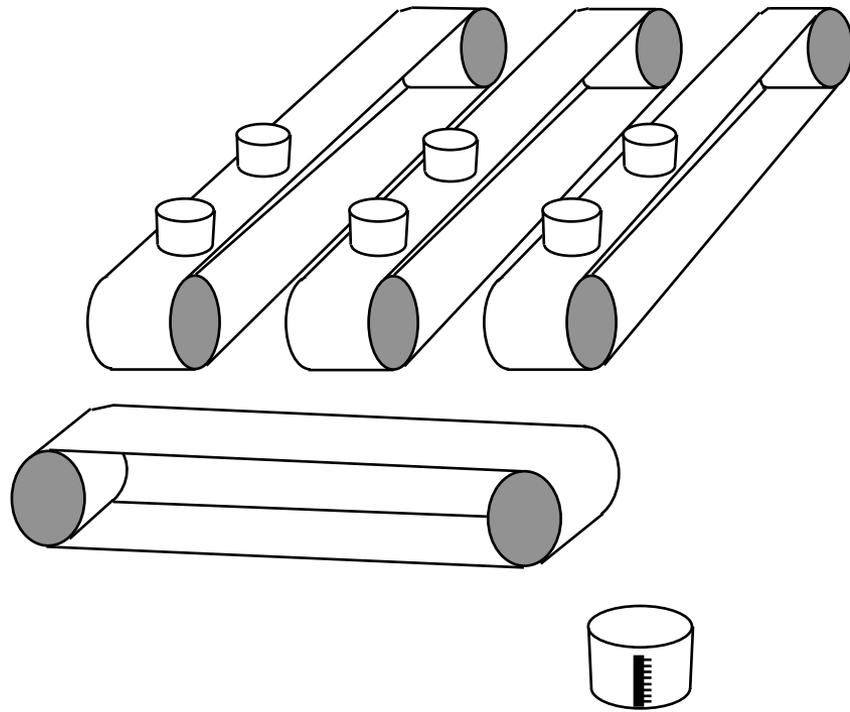




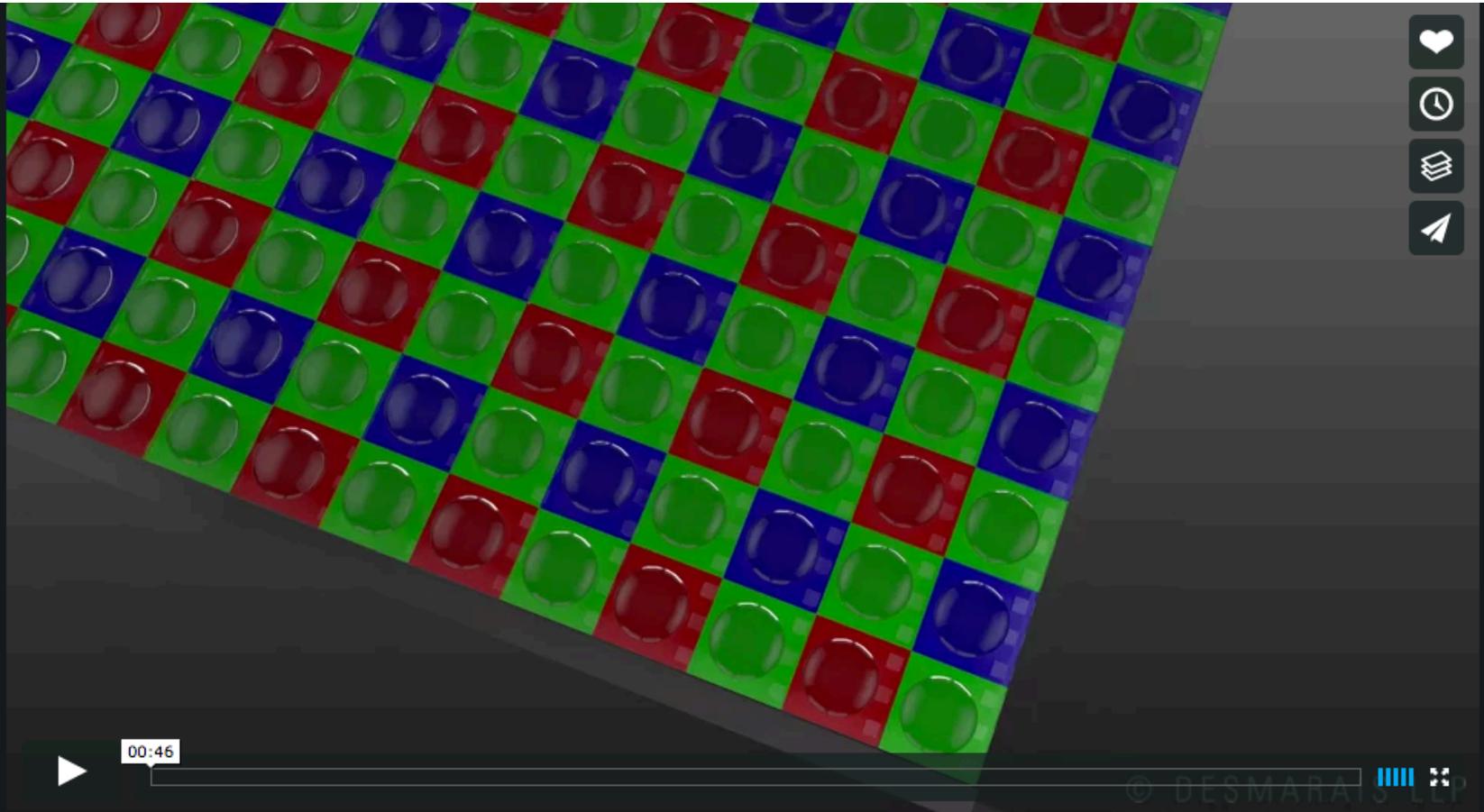








# Is this better?



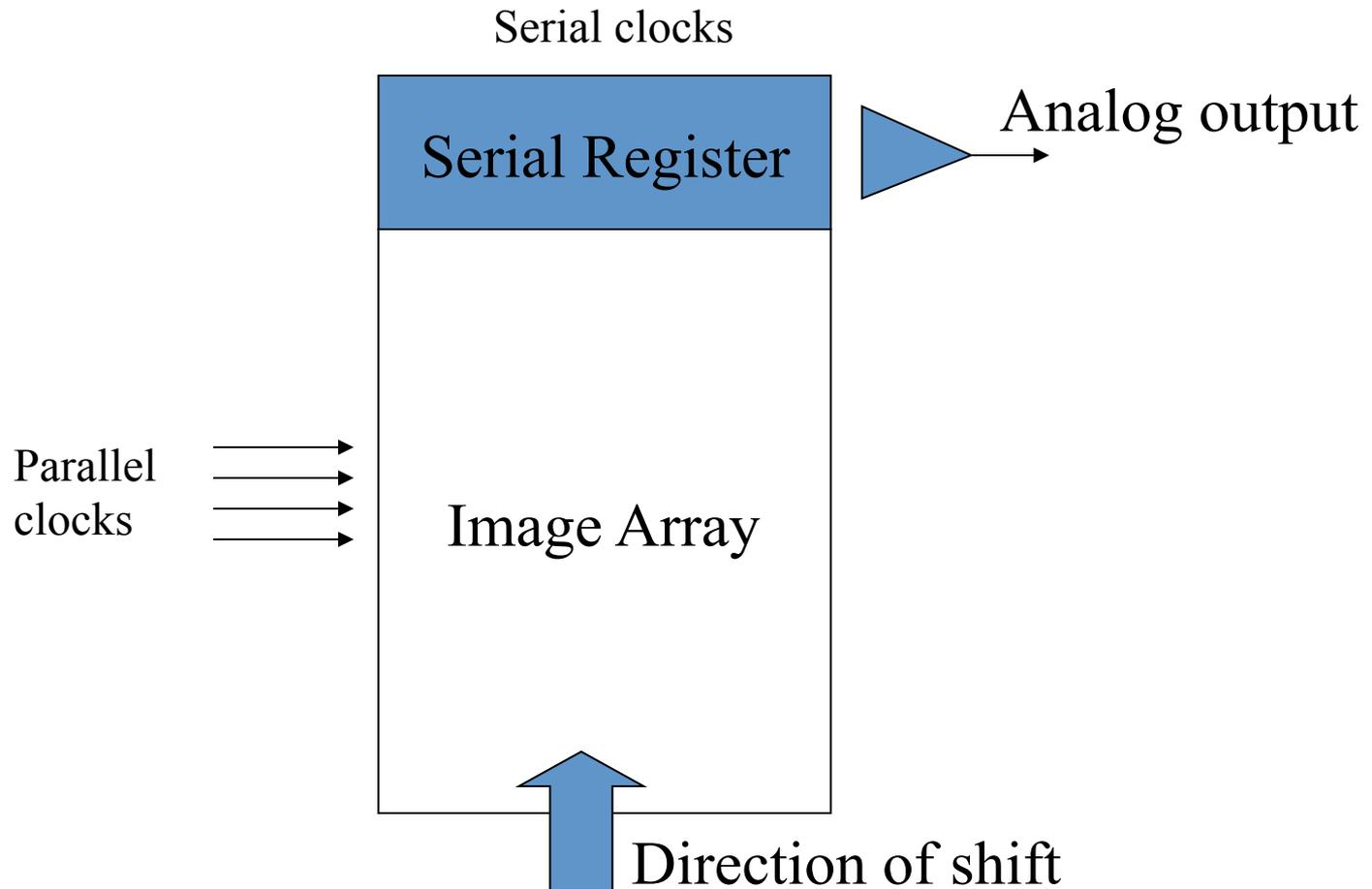
## CCD Animation Sequence (Full HD 15-25Mbps)

from Raymond Sirí 2 years ago

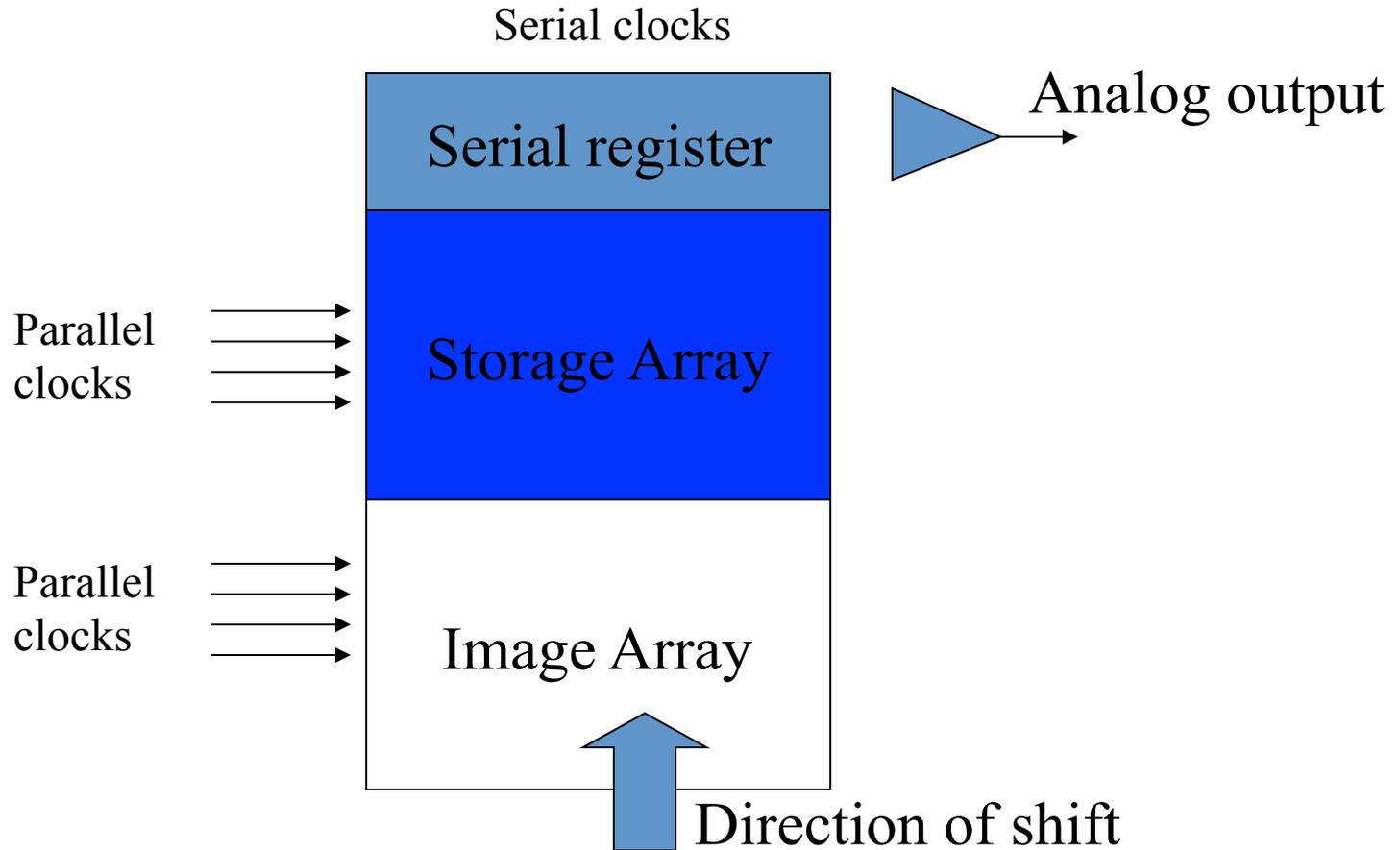
Recommended

Autoplay on

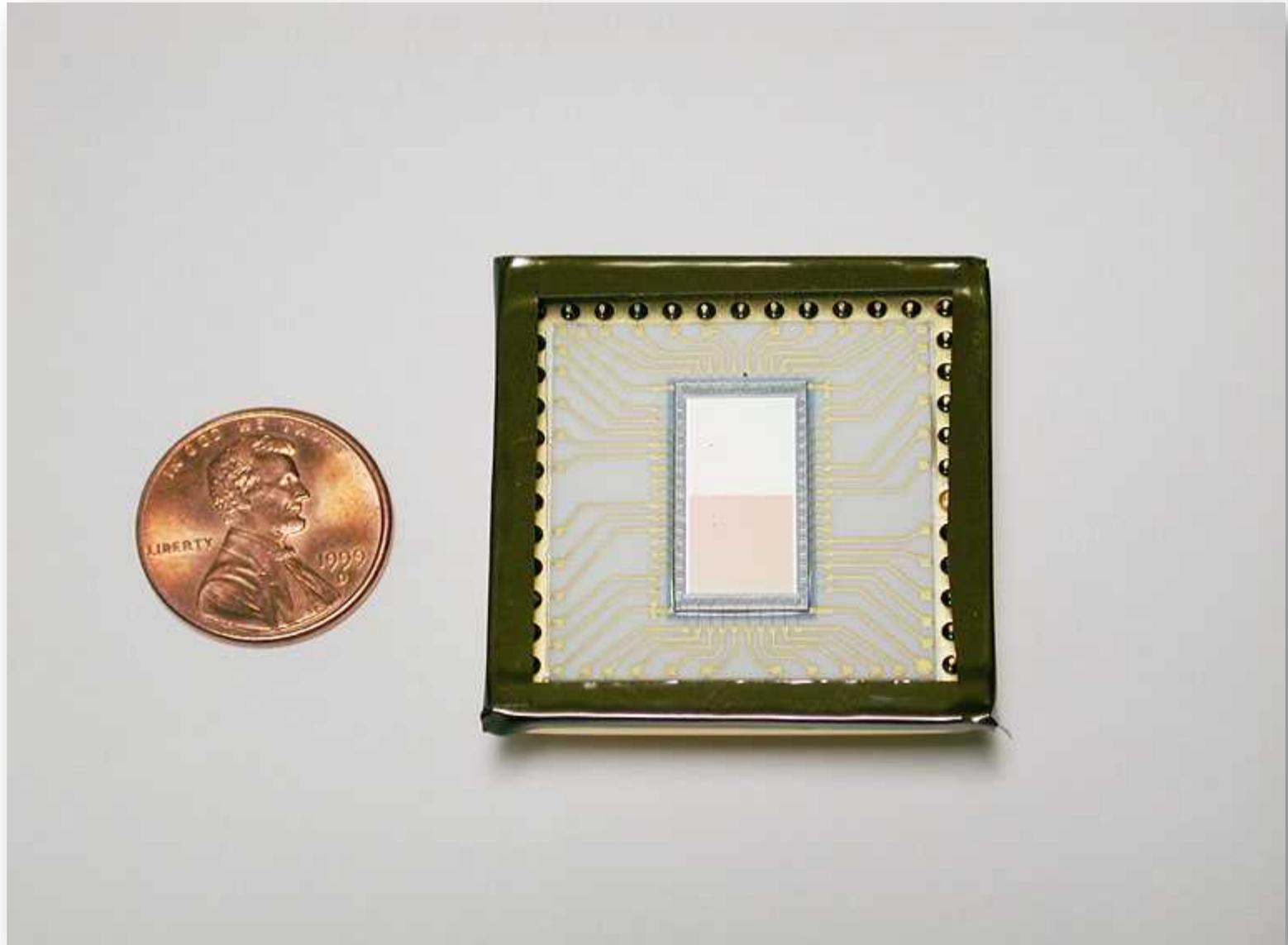
# Full Frame CCD



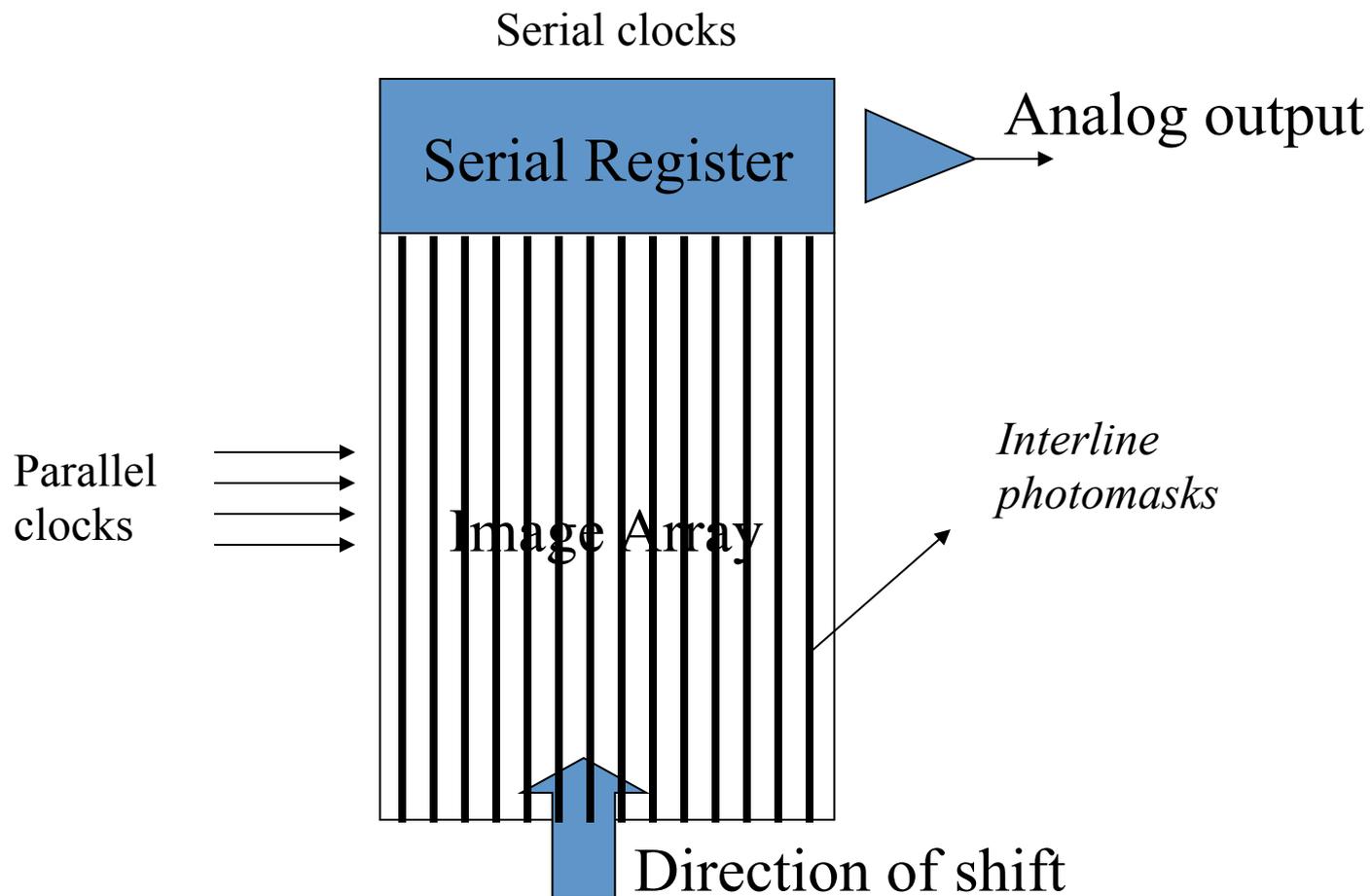
# Frame Transfer CCD



# Frame Transfer CCD



# Interline Transfer CCD



# Electrical Efficiency - Stages ( CCD, see Janesick's books, tutorials)

Incident photons  
(irradiance, in  
photons per square  
micron of the sensor  
per nm)

## Sensor

<u>Interacting photons</u>	<u>Electrons collected</u>	<u>Volts</u>
Incident photons	Interacting photons	Electrons collected

*Interacting  
Quantum  
Efficiency*

*Effective  
Quantum  
Yield*

*Sensitivity of  
CCD on-chip  
amplifier*

## Electrical

<u>Volts</u>	<u>Digital Count</u>
Volts	Volts

*Analog  
Processor  
gain*

*Analog-  
digital  
conversion*

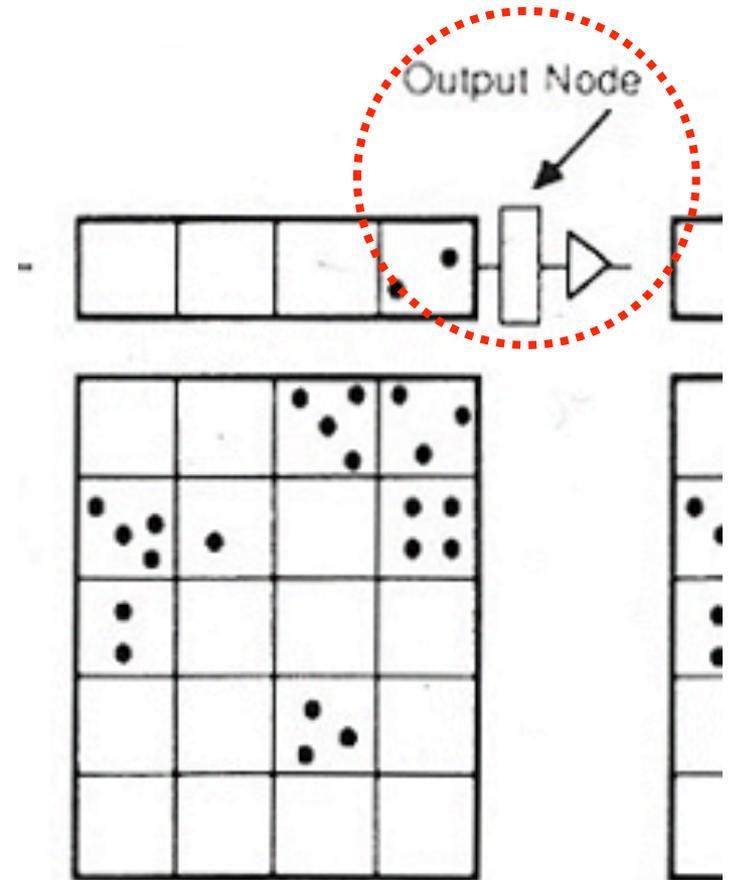
*(After J. Janesick, Pixel Vision)*

# Engineering: Reducing 'reset' noise (CDS)

The image from a CCD is read out by transferring rows of charge into a single horizontal register, followed by transfer of individual pixel charge along the horizontal register towards a single output node.

As each pixel's charge reaches the output node, it is digitized and transferred to the computer for display.

There can be significant unwanted charge at this output stage. This unwanted signal is due to inaccurate resetting of the output.



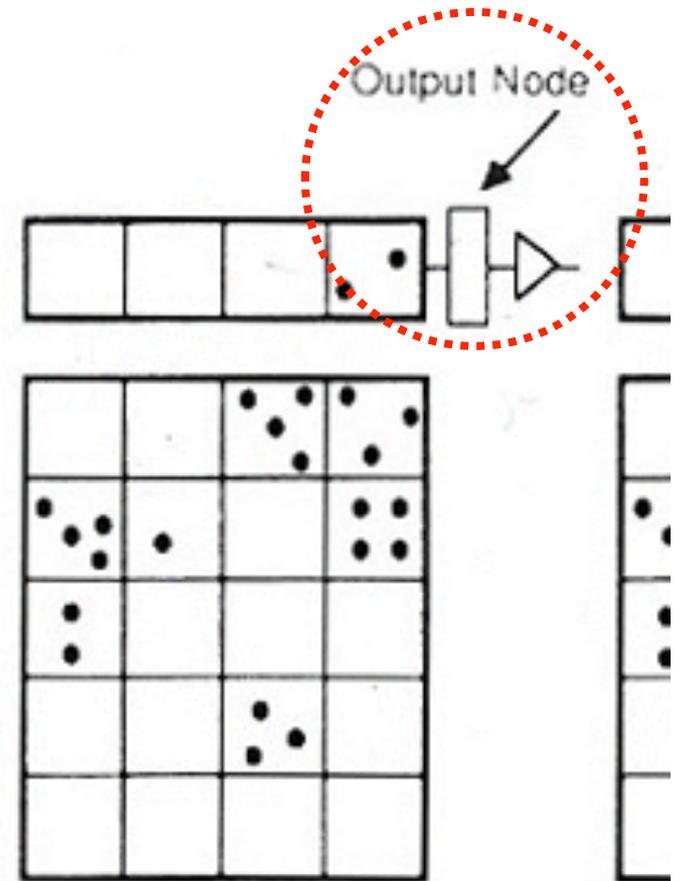
# Engineering: Correlated Double Sampling (CDS)

Before the charge of each pixel is transferred to the output node, the node is reset to a fixed **reference value**. This value has Fixed and Variable Unwanted Effects.

The difference between the **reference value** and the transferred charge is measured and assigned to the pixel. This process is called Correlated Double Sampling (CDS).

Measuring the difference removes the Fixed Unwanted Effects. But reading twice causes extra noise (Variable Unwanted Effects)

It increases the Variable Unwanted Effects. When the Fixed  $\gg$  Variable Unwanted, CDS is useful.



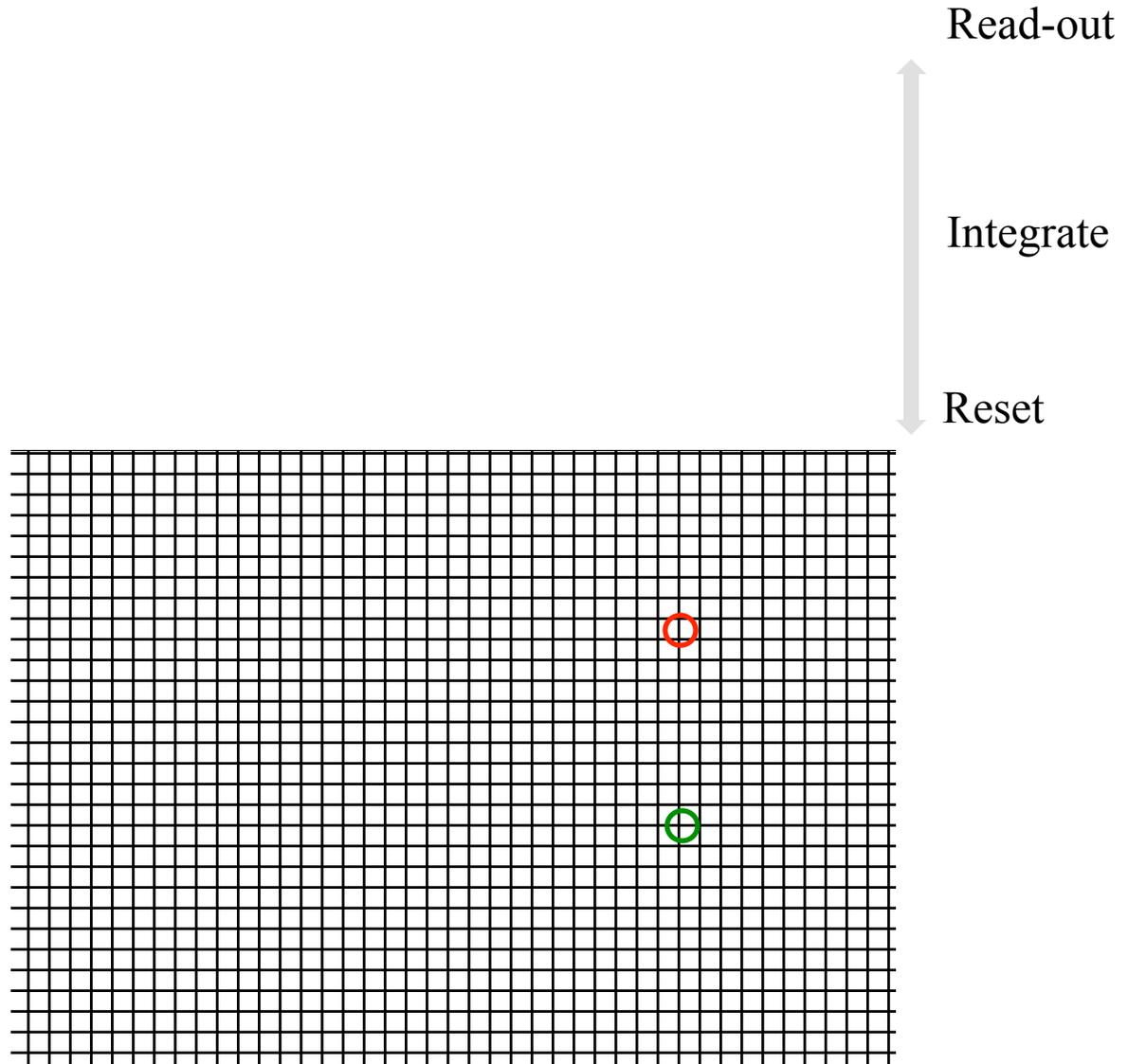
# Shuttering

- Rolling
- Global



# Rolling shutter

- Sensor is reset-integration-read a row (or column) at a time; this takes some time
- The scene changes during the read-out
- Temporal sampling artifacts
- These appear as spatial distortions



# Movie of telephone lines



Note the power line



# Rolling shutter

- Sensor is reset-integration-read a row (or column) at a time; this takes some time
- The scene changes during the read-out
- Temporal sampling artifacts
- These appear as spatial distortions



# Global shutter – single pixel

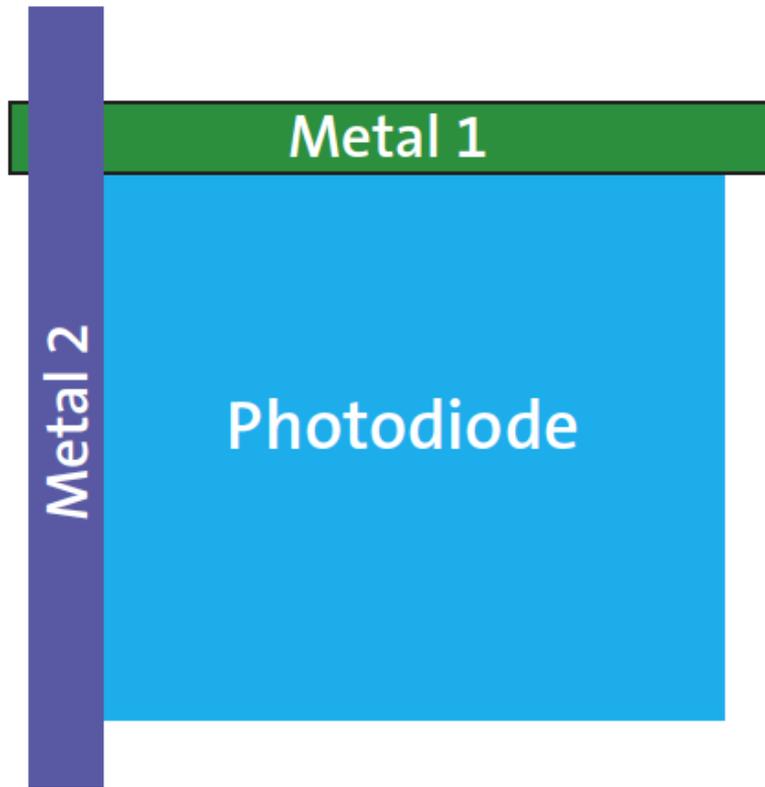


Figure 3. Rolling Shutter Pixel

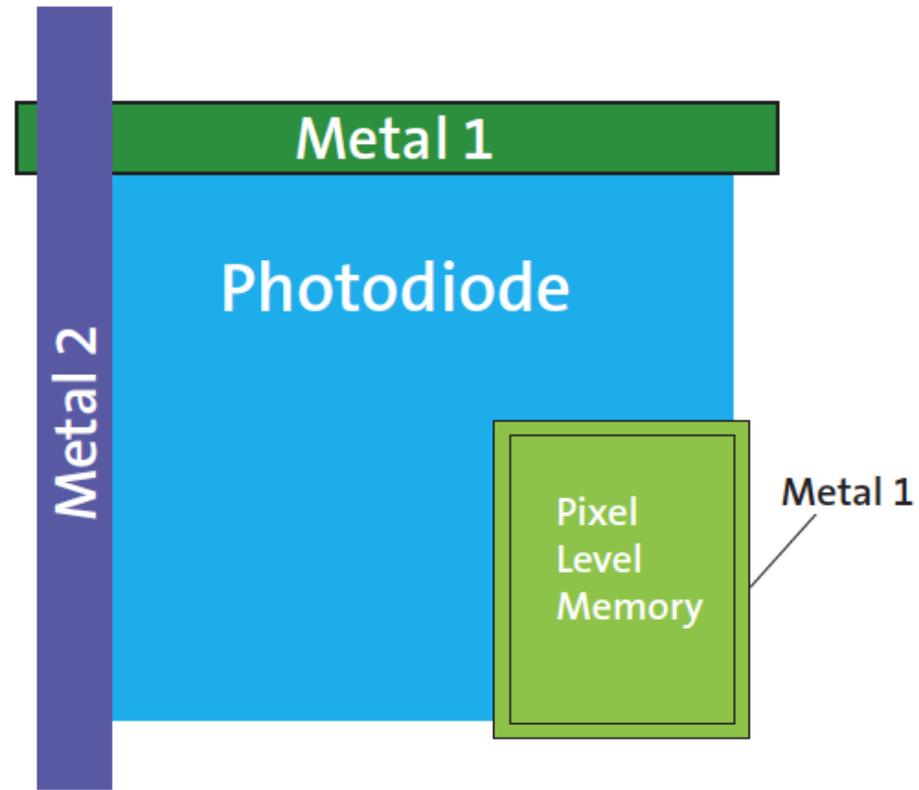
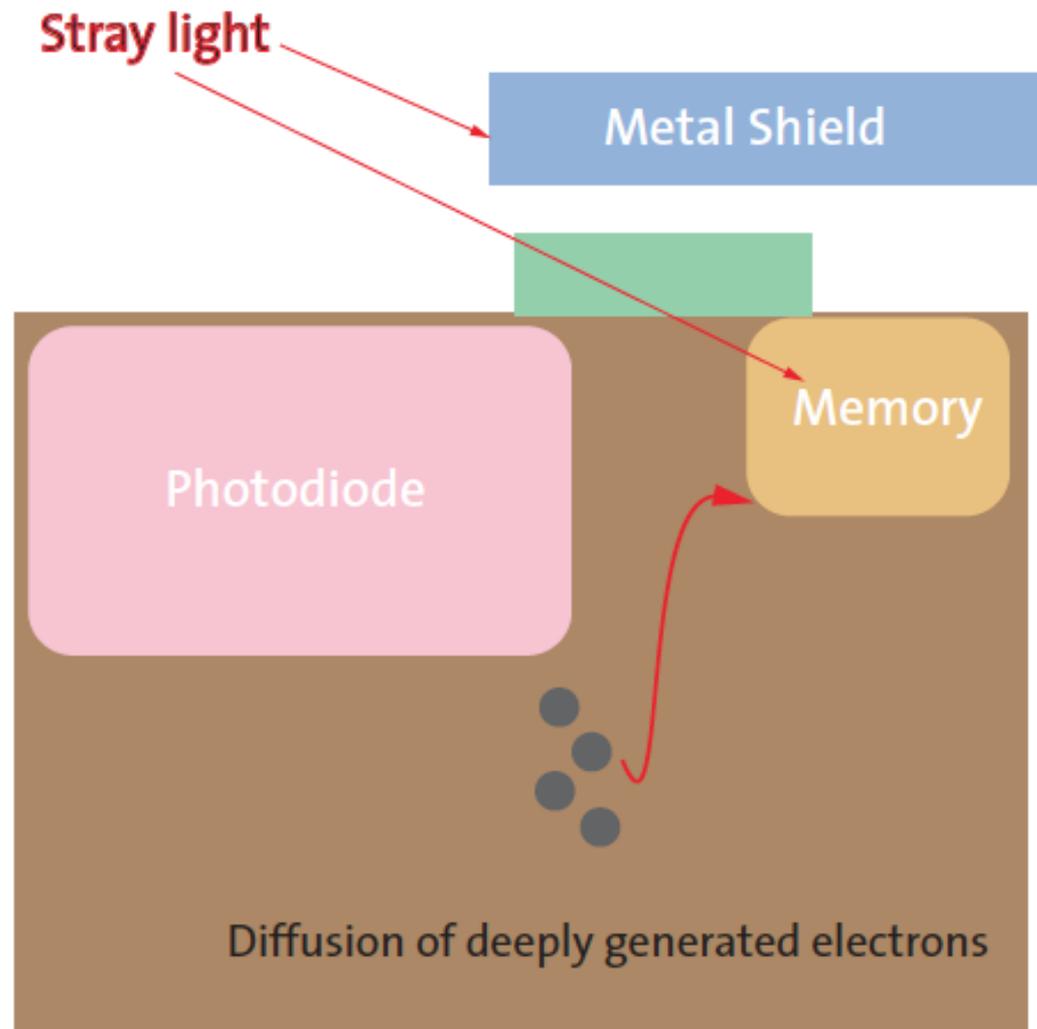


Figure 4. Global Shutter Pixel

# Global shutter readout (Aptina)

- Global shutter efficiency measures how well electrons are stored in the memory without being contaminated by unwanted electrons
- This image illustrates two ways in which unwanted electrons enter the memory node

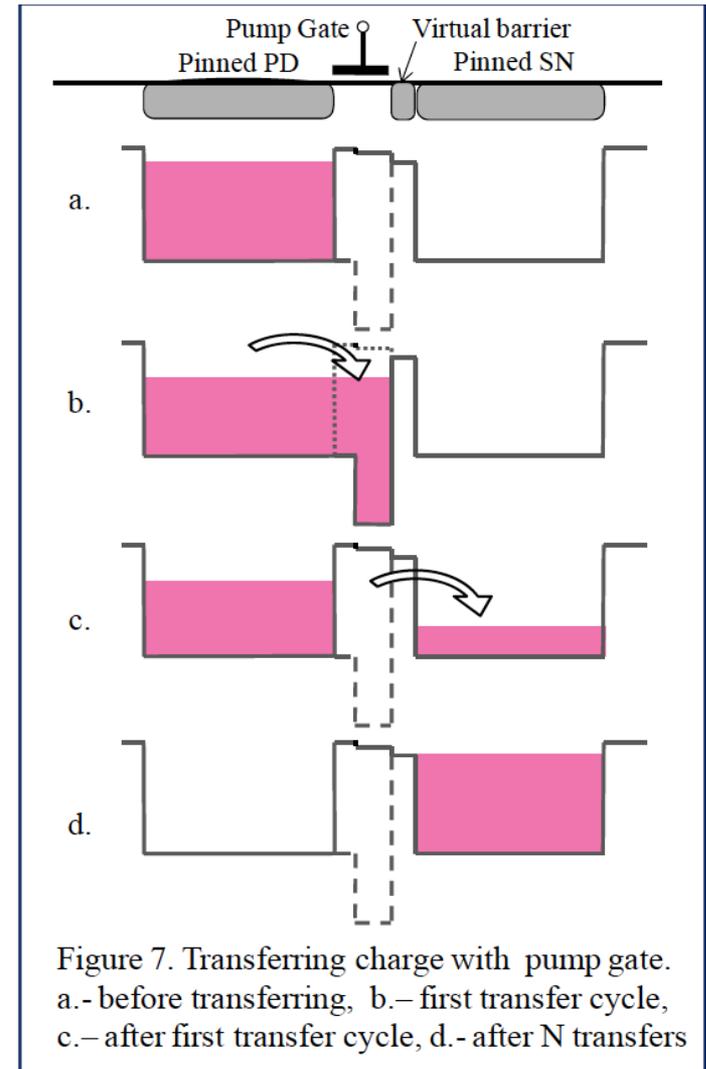


# Global shutter readout (Aptina)

Charge from the pinned photodiode is pumped to a surface-pinned storage node.

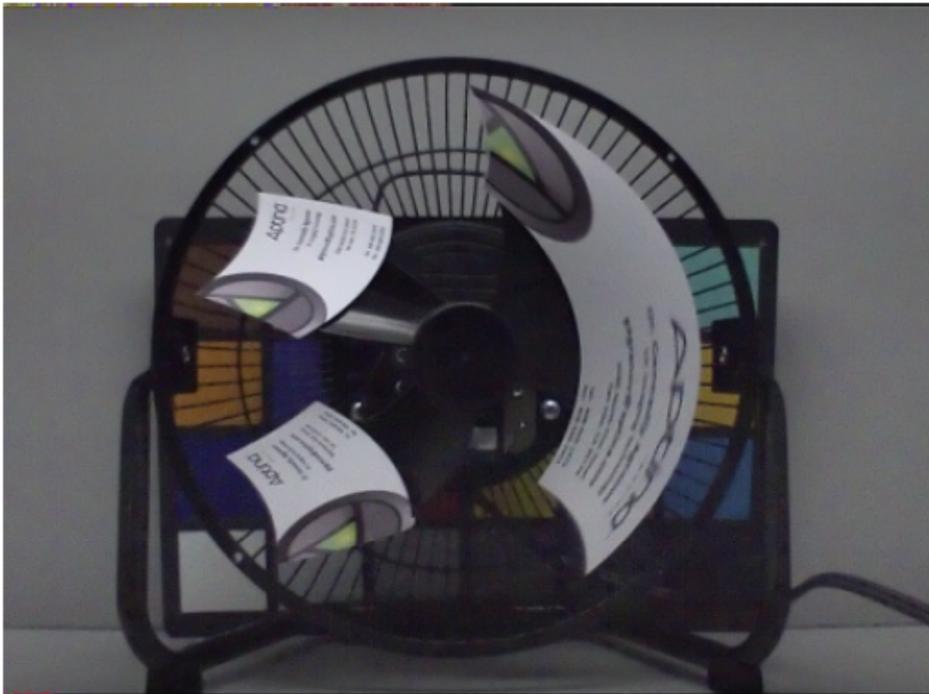
There is an anti-reflective metal light shield in close proximity to the node to shield from stray light

The pump technology reduces the number of stray (diffusing) electrons



# Global shutter

Rolling shutter

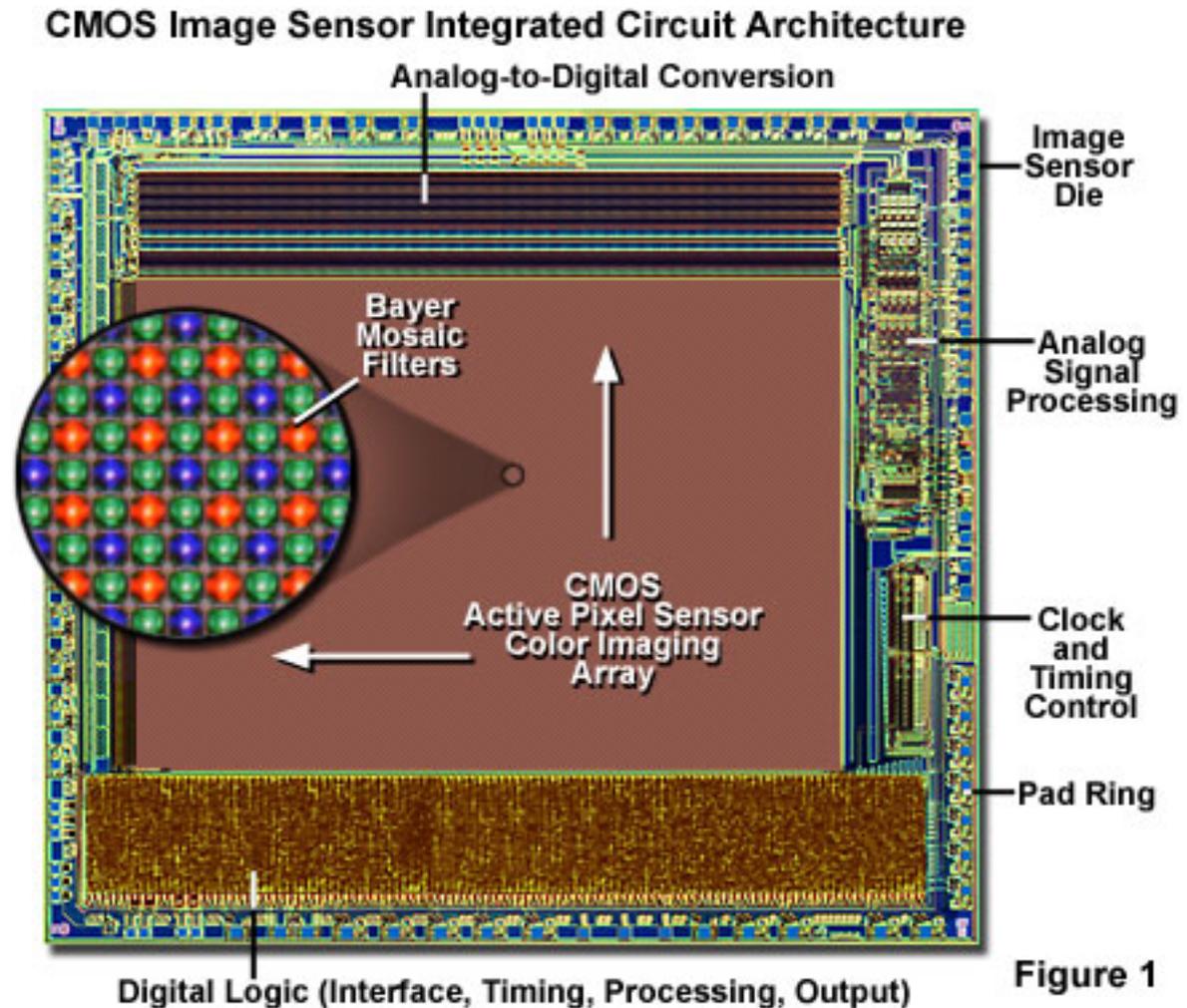


Global shutter



# System on a chip

- The sensor is embedded in other circuitry
- Much of the circuitry controls the sensor read and reset
- There can be additional elements (such as masked pixels) that are used for image processing (noise)



# Camera equation – (No noise)

- Linear spectral responsivity
- Counting photons
- Photon noise

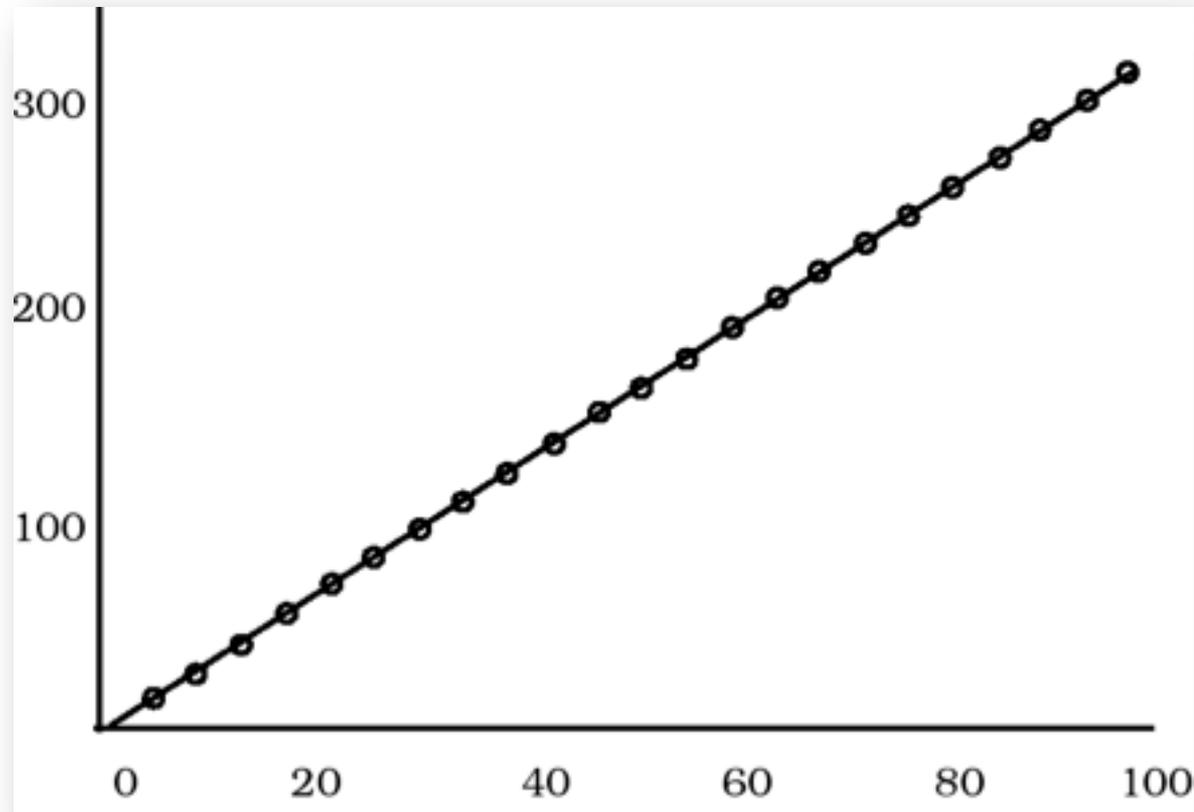


# CCD and CMOS transfer functions

*(Epperson, P.M. et al. Electro-optical characterization of the Tektronix TK5 ..., Opt Eng., 25, 1987)*

CCD and CMOS are Si absorptions

Electron absorptions



Photons at  
detector

# Convert photons to electrons at the pixel

$$e = GT \int i(\lambda) r(\lambda) f(\lambda) d\lambda$$

$G$  = geometric factors (pixel optical cross-section,  $m^2$ )

$T$  = integration time (s)

$i$  = spectral irradiance (photons/s/nm/ $m^2$ )

$r$  = spectral responsivity of channel (electrons/photon)

$f$  = filter and media transmissivities

$e$  = electrons at the pixel

Check units:  $e = m^2 \text{ s } \int \text{p/s/nm/m}^2 \text{ e/p d(nm)}$

# Camera equation (noise-free) as a matrix tableau

Electrons in each color channel

color filter transmissivity and other (e.g., lens)

photodiode quantum efficiency

Irradiance

Wavelength samples

$$\begin{pmatrix} R \\ G \\ B \end{pmatrix} = \begin{pmatrix} \cdots & f_R(\lambda)r(\lambda) & \cdots \\ \cdots & f_G(\lambda)r(\lambda) & \cdots \\ \cdots & f_B(\lambda)r(\lambda) & \cdots \end{pmatrix} \begin{pmatrix} i(\lambda) \end{pmatrix}$$

# Camera equation (noise-free) as a matrix tableau

Electrons in each color channel

color filter transmissivity and other (e.g., lens)

photodiode quantum efficiency

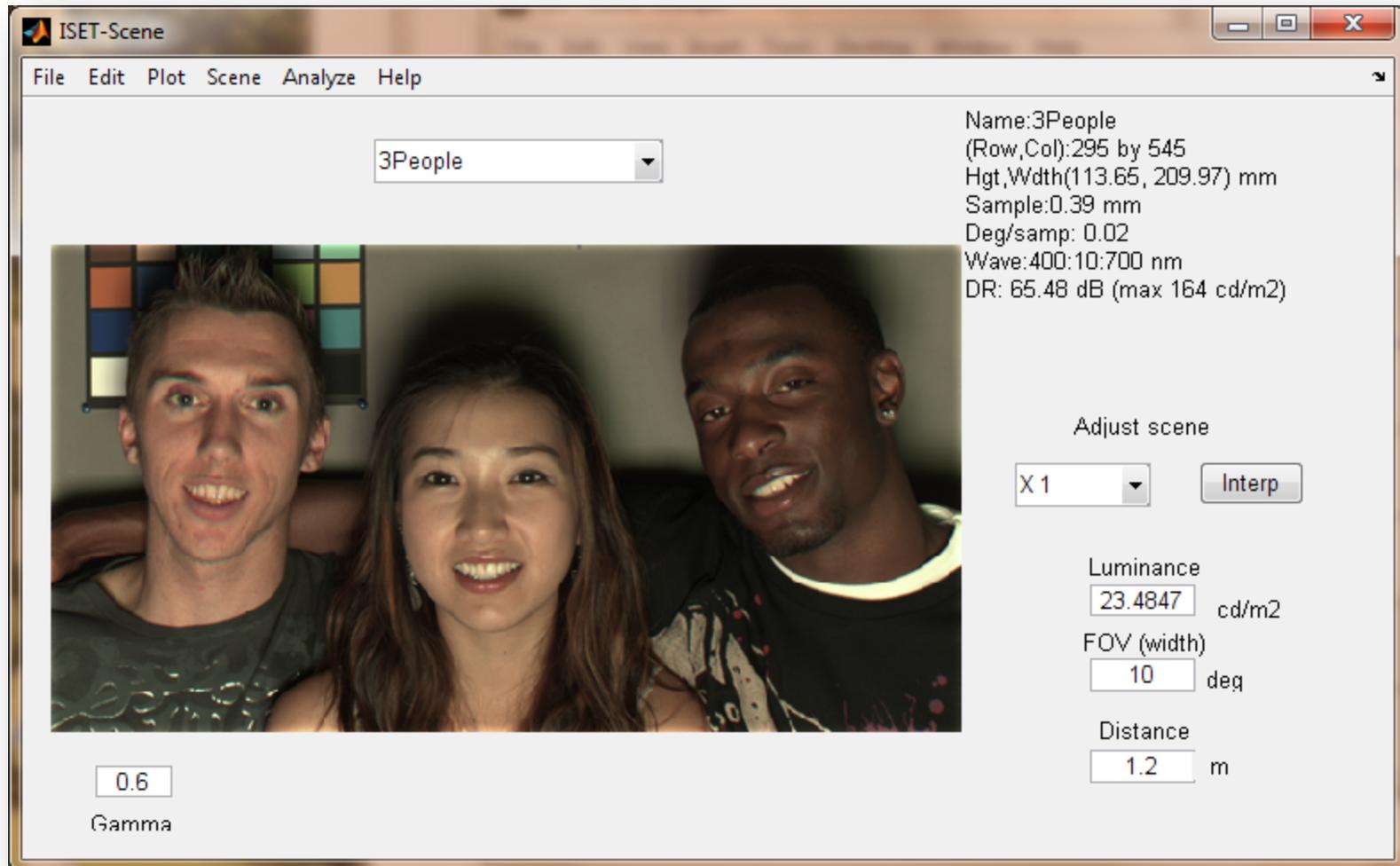
Irradiance

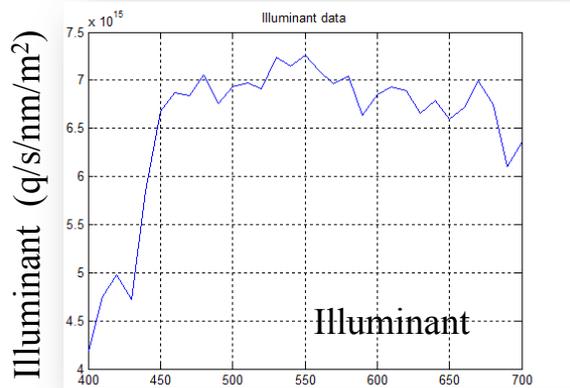
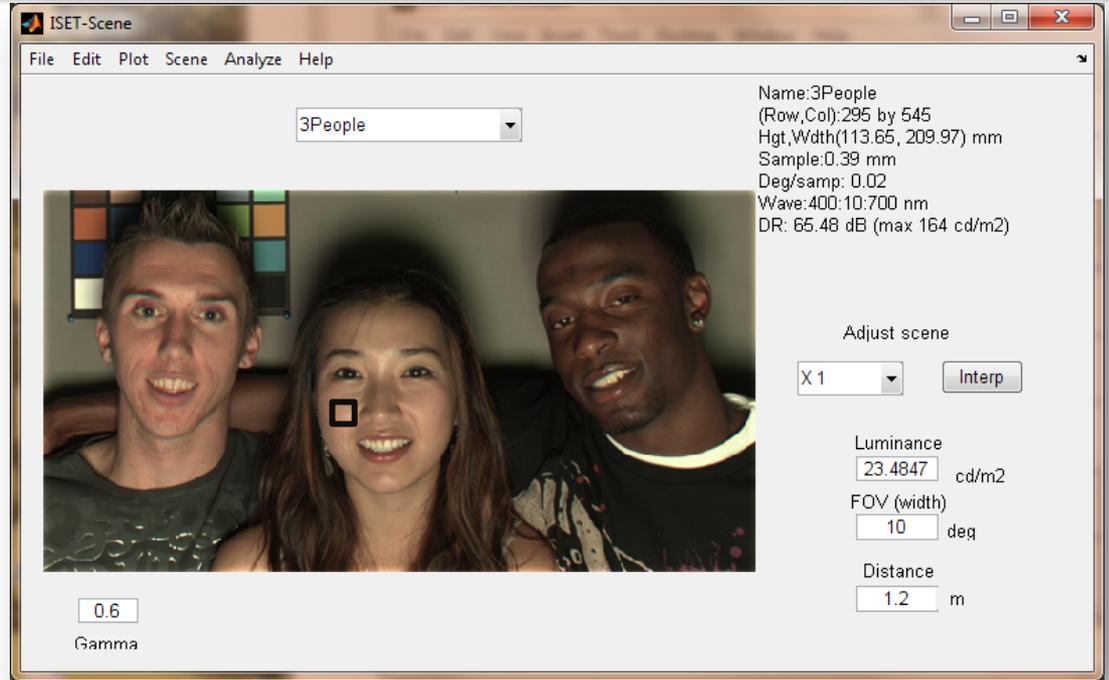
Illuminant

Surface

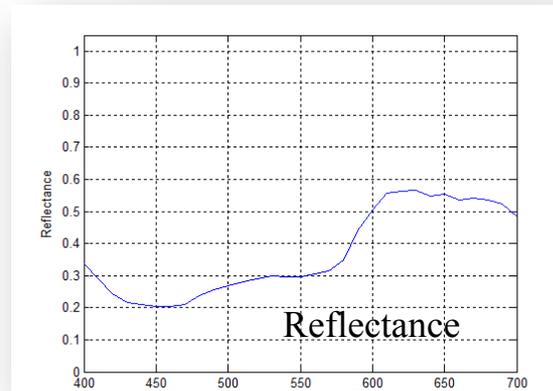
$$\begin{pmatrix} R \\ G \\ B \end{pmatrix} = \begin{pmatrix} \dots & f_R(\lambda)r(\lambda) & \dots \\ \dots & f_G(\lambda)r(\lambda) & \dots \\ \dots & f_B(\lambda)r(\lambda) & \dots \end{pmatrix} \begin{pmatrix} \dots & 0 & \dots \\ \vdots & e(\lambda) & \vdots \\ 0 & \dots & \dots \end{pmatrix} \begin{pmatrix} \dots \\ s(\lambda) \end{pmatrix}$$

# Follow the photons

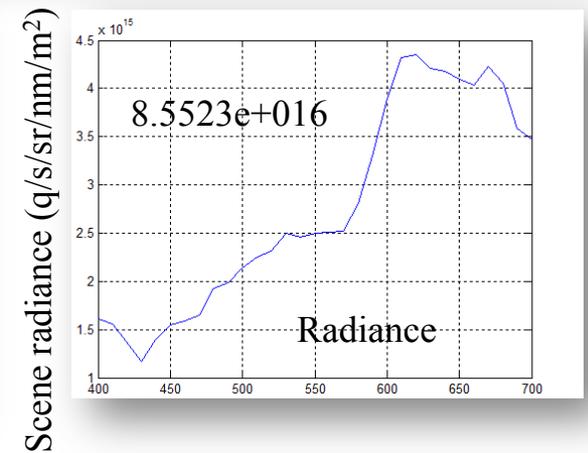




X



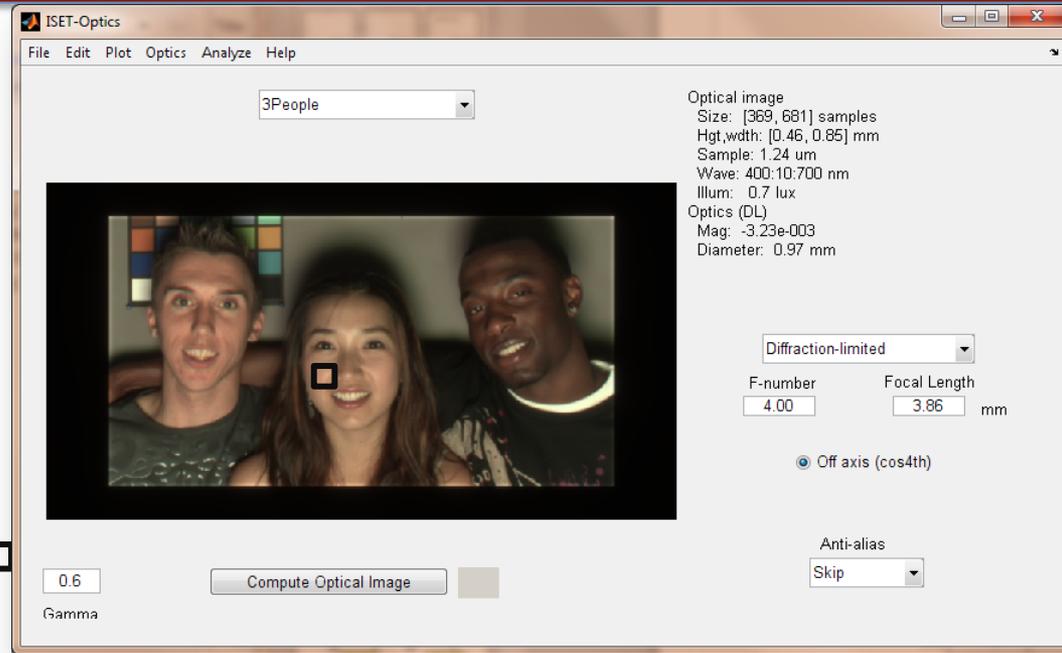
=



Wavelength (nm)

# Optical image (irradiance)

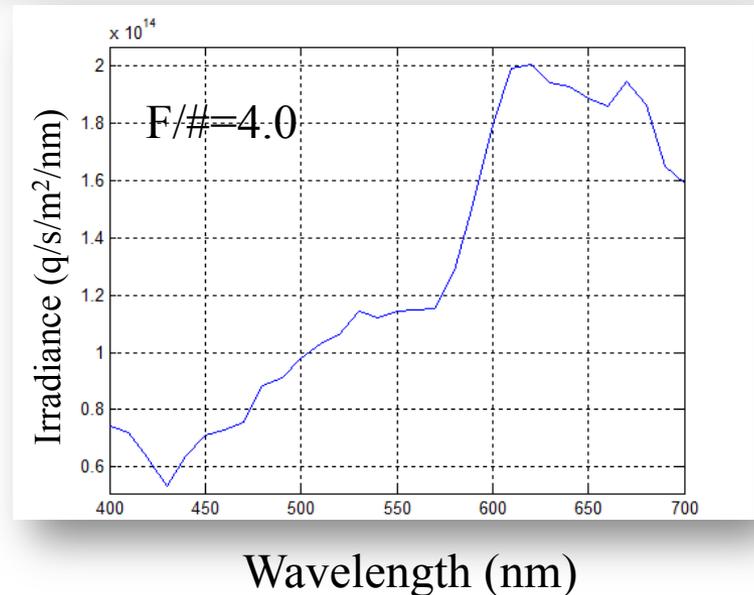
If there is only loss due to the aperture, how many photons arrive at a pixel?



Total per  $\mu\text{m}^2$  in  
10 ms      CNR (dB)

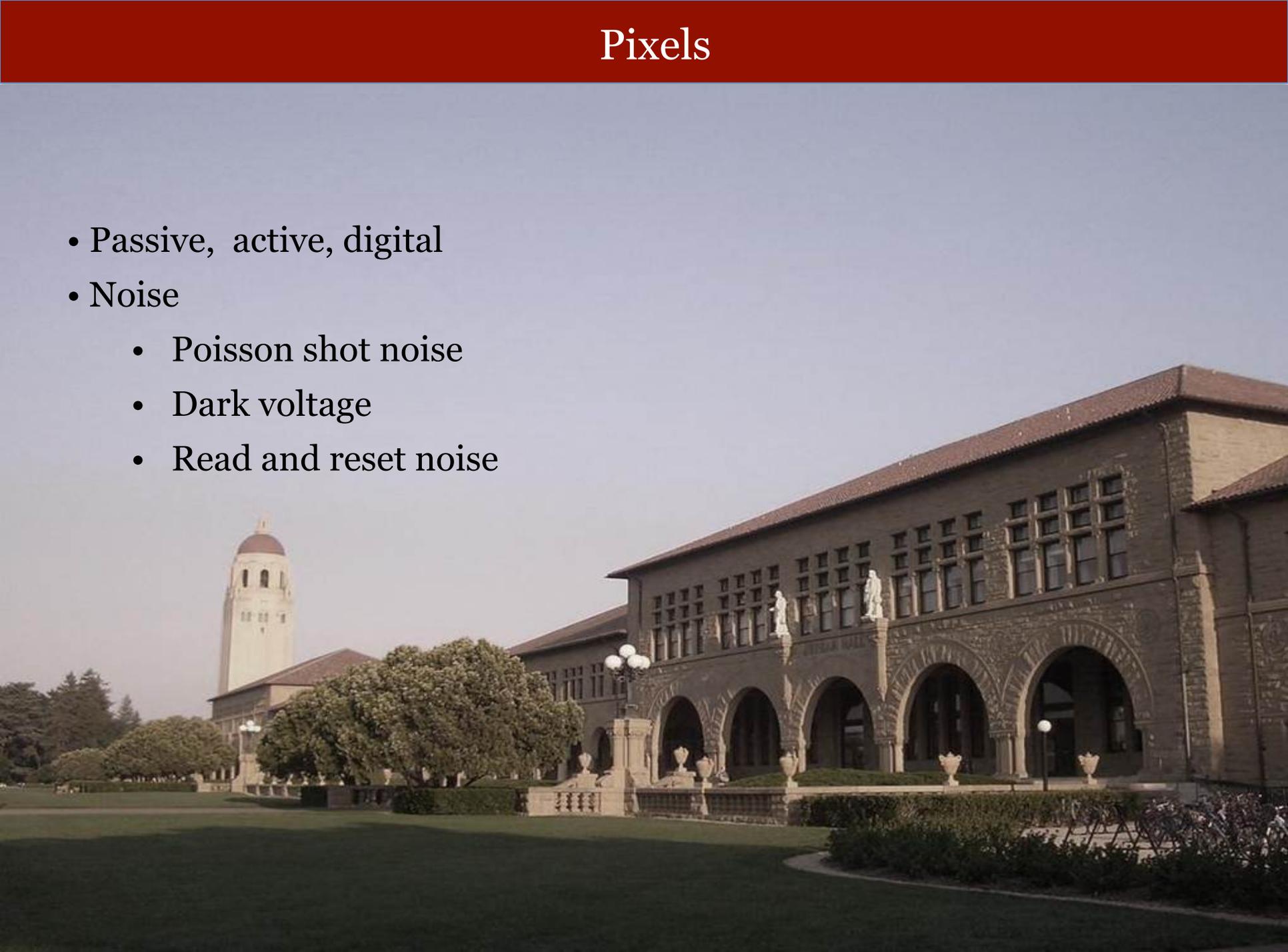
F/#=2.0	1.5193e+016	152	21.8
F/#=4.0	3.9298e+015	39	16
F/#=8.0	9.7244e+014	10	10

Thousand photon (30 dB) limit



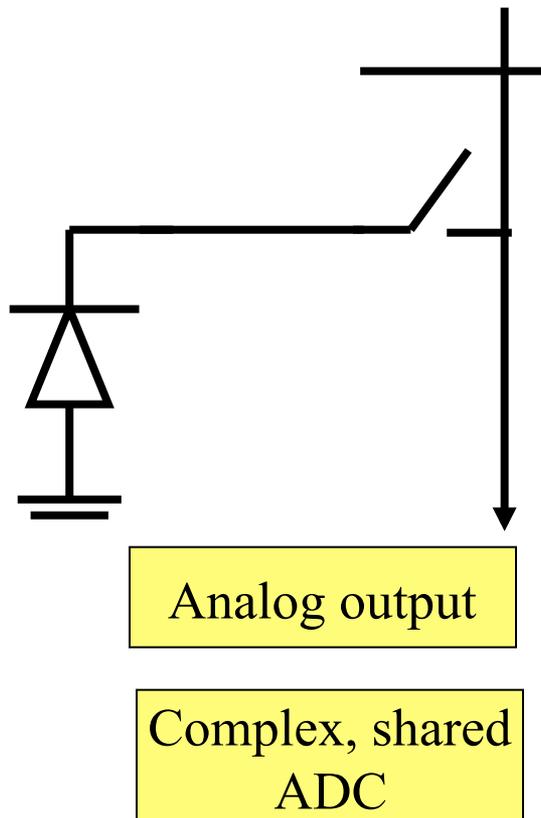
# Pixels

- Passive, active, digital
- Noise
  - Poisson shot noise
  - Dark voltage
  - Read and reset noise

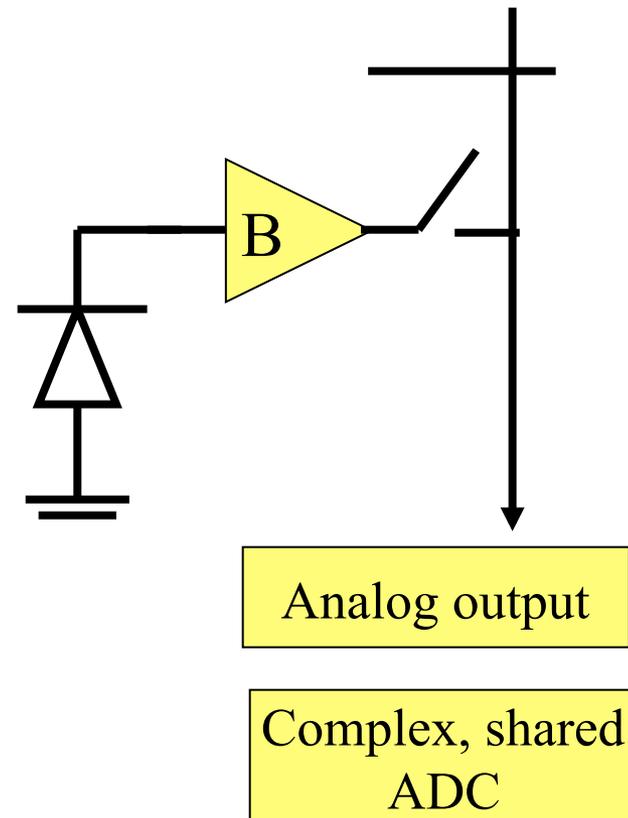


# Hardware Development: CMOS pixels: PPS, APS, DPS

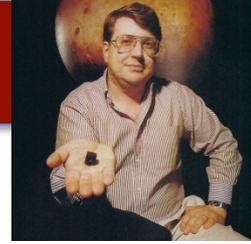
Passive pixel sensor (PPS)



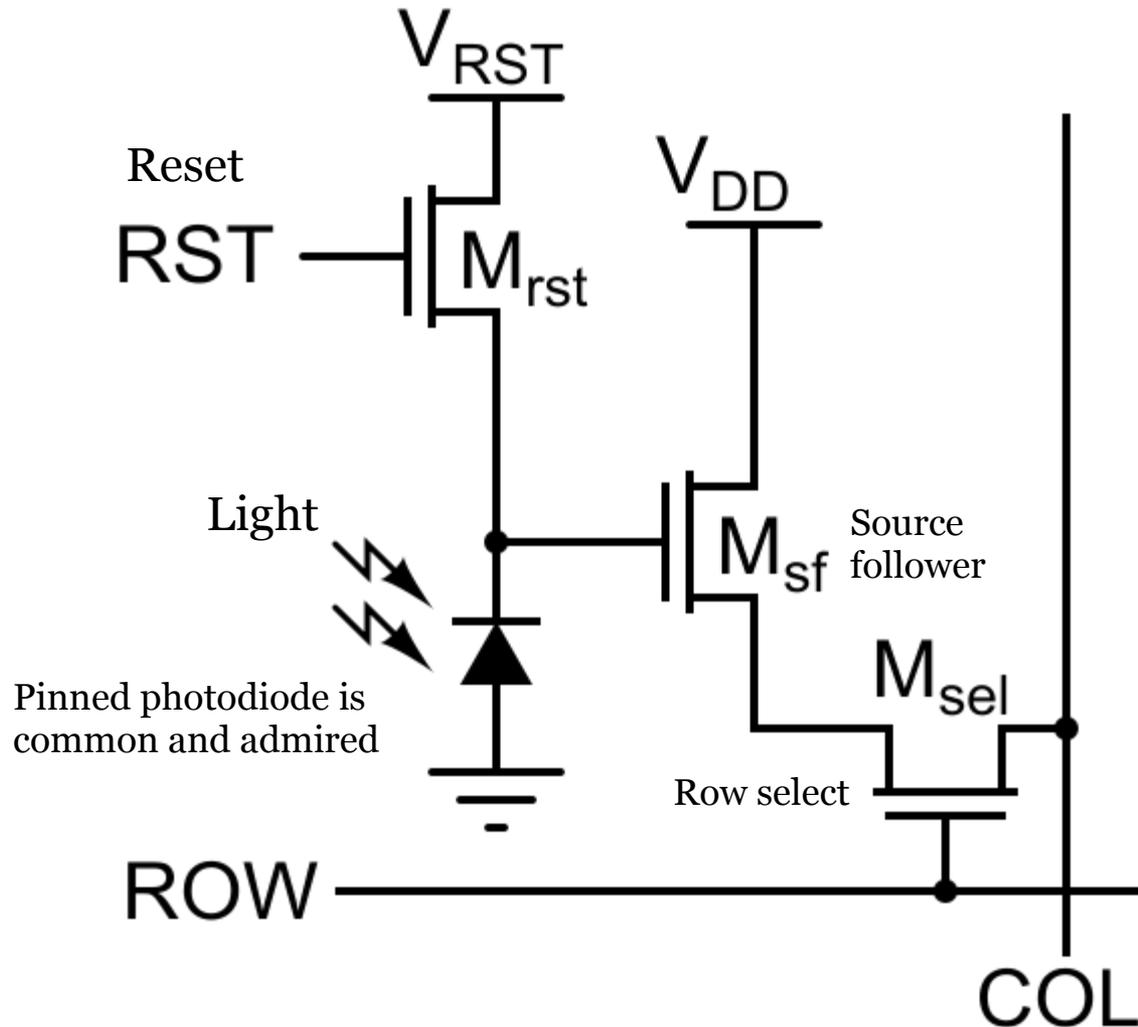
Active pixel sensor (APS)



# CMOS pixel circuit (APS, 3T)



Eric Fossum



- Reset transistor clears the charge on the photodiode by coupling to power
- Light induces charge to accumulate at photodiode
- Source follower allows voltage to be observed without clearing the charge
- Columns tied together, one row selected at a time

# A correction about the history

Hi Prof. Wandell,

I listened to your PSYCH 221 recording (lecture 6, 2013). I have a comment about who invented the idea of using in-pixel buffers in CMOS sensors.

Please take a look at this 1969 paper. Figure 1 and 8 show a photodiode equipped with a source follower and a reset transistor. Despite the cumbersome output mechanism, the idea of buffering each photodiode is evident.

Prof. Fossum patented this idea along with a modern readout mechanism. A heroic contribution, but the idea of buffering each pixel predates that.

Thanks,

*XXX (heroic and smart young student)*

# Pixel-level circuit noise

t\_cameraNoise.m

hwSensorFundamentals.m

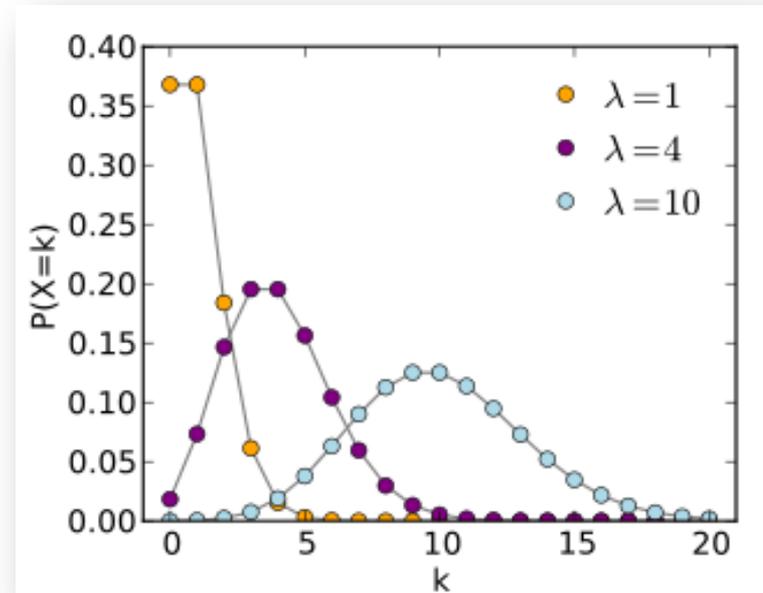
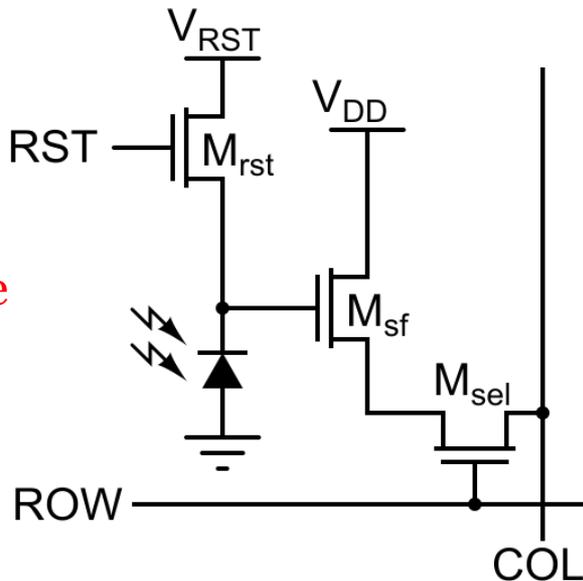
- Electrons (Poisson random variable) are converted to volts by circuit properties (conversion gain)

$$v_0 = c \tilde{e}$$

Poisson distribution

$$f(k; \lambda) = \frac{\lambda^k e^{-\lambda}}{k!},$$

Shot noise



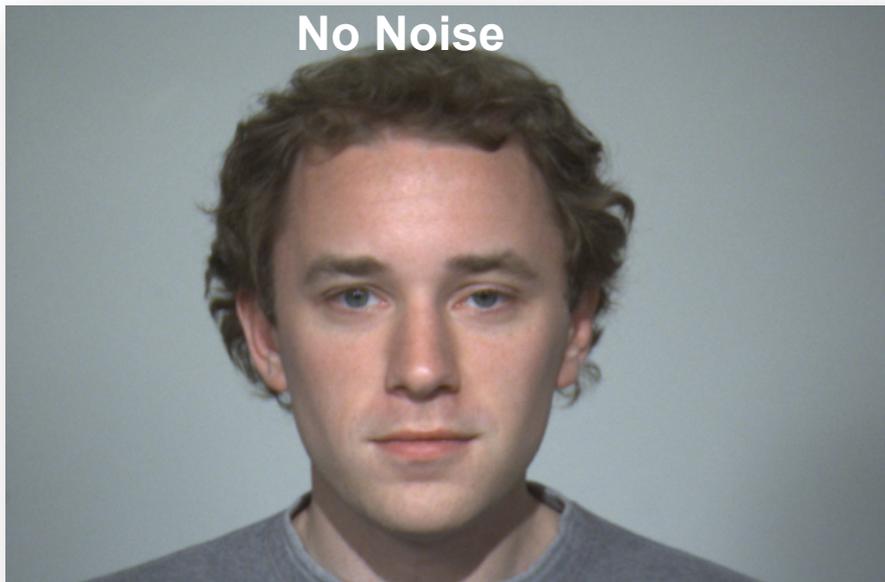
# Photon noise (shot noise)

No spatial structure

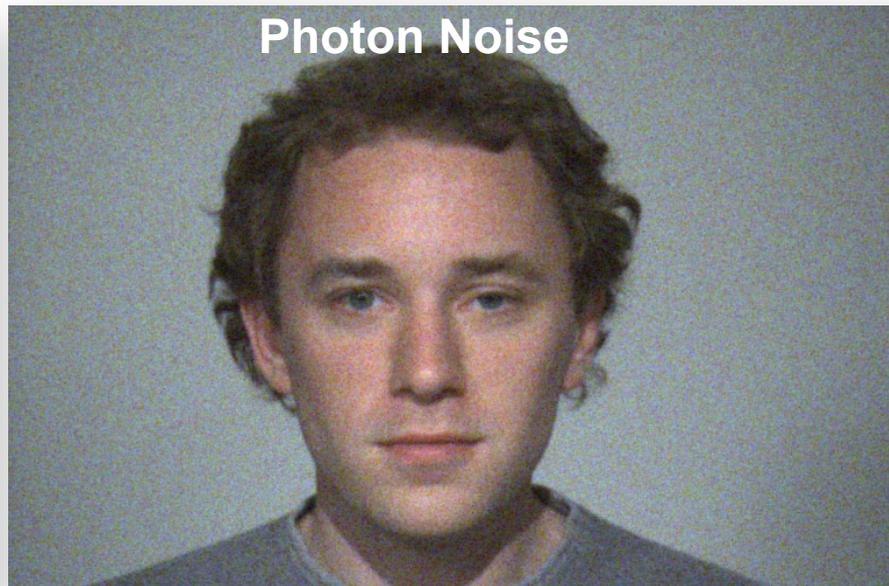
Averaged away by repeated measures

Visible at an SNR of 30 dB (1000 photons, Xiao et al.)

No Noise



Photon Noise



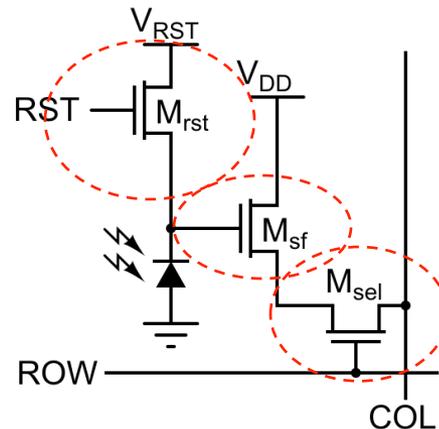
# Pixel noise

- Electrons (Poisson random variable) are converted to volts by circuit properties (conversion gain)
- Circuit imperfections introduce dark voltage that grows over time ( $T \cdot V / \text{sec}$ )
- The acts of reading and resetting the voltage are noisy (and can be grouped)

$$v_0 = c \tilde{e}$$

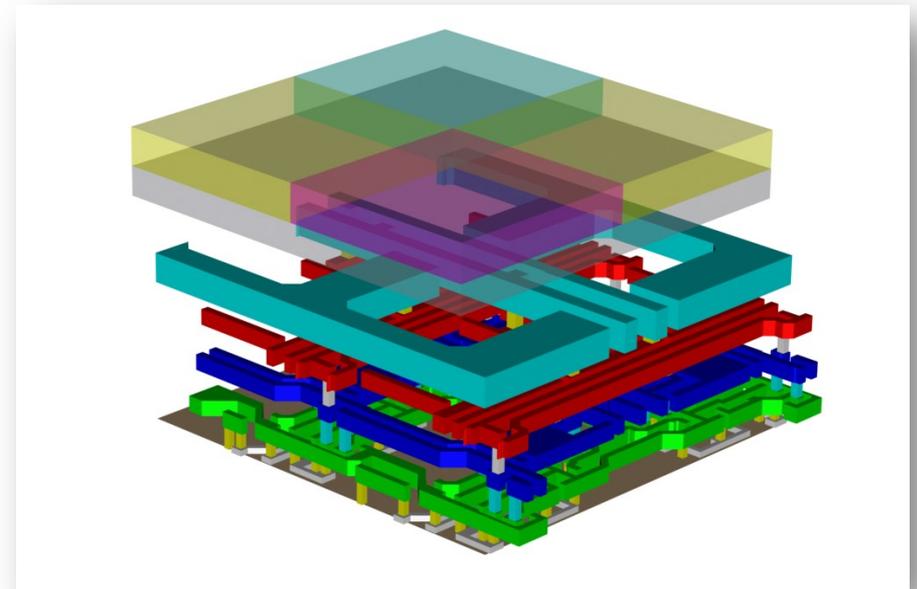
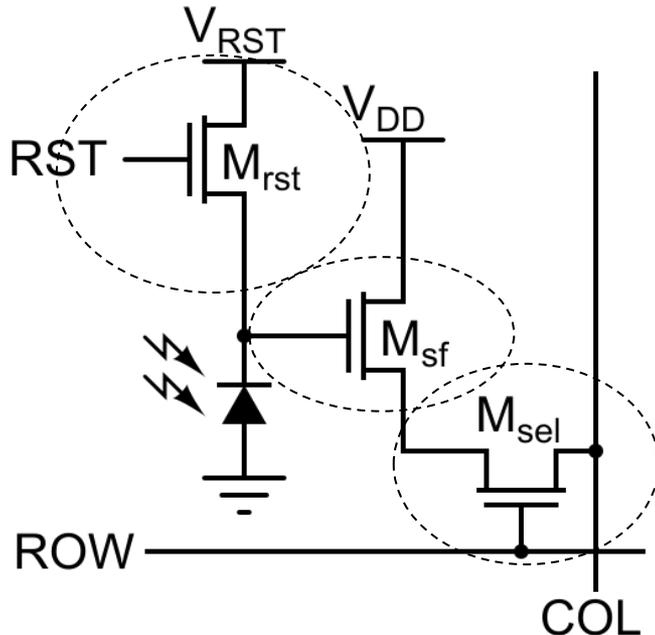
$$v_1 = v_0 + T \tilde{d}$$

$$v_2 = v_1 + \tilde{r}_0 + \tilde{r}_1$$



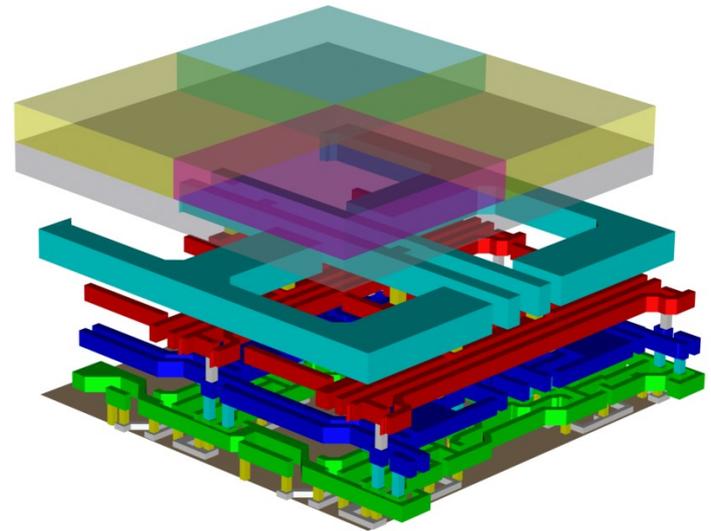
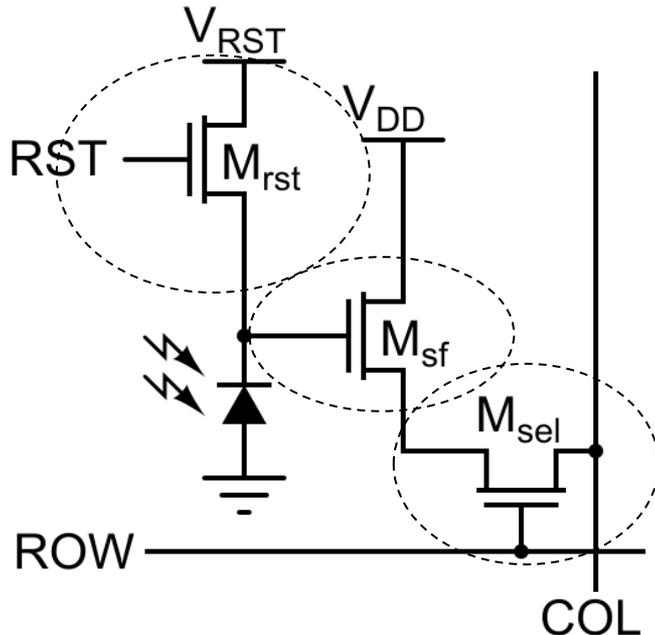
# Dark noise

Thermally generated electrons are indistinguishable from photo-generated electrons. They constitute a noise source known as 'Dark Current.' High end CCDs are designed (e.g., by cooling or in CMOS special circuitry) to reduce the amount of dark current.



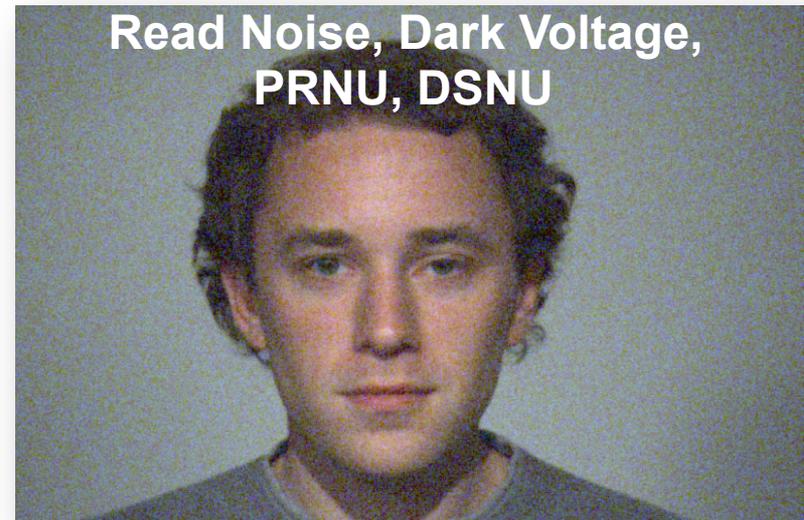
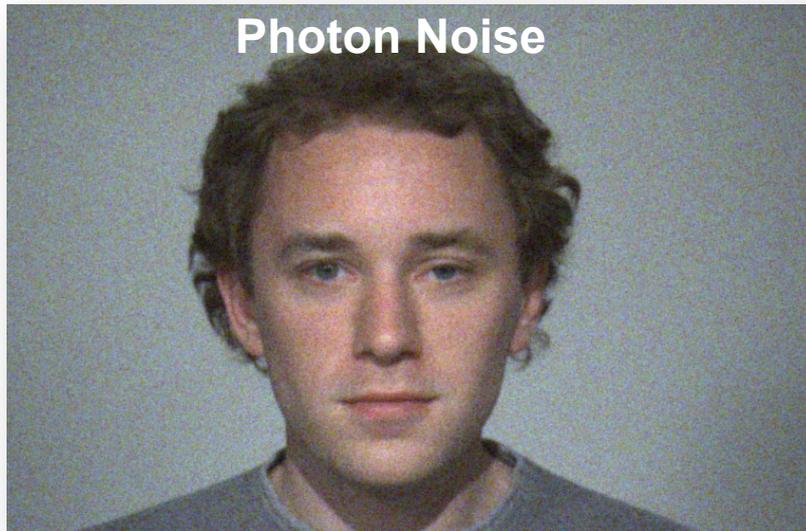
# Read and reset noise

The act of reading data from a pixel and resetting the pixel level to an initialized state involve imperfect circuit events. These imperfections are sensor read and sensor reset noise. They can be separately identified, but in simulation it is convenient to group them.



# Photon, read, reset, dark, prnu, dsnu

Adds to photon noise – so 1000 photons not enough for noise-free

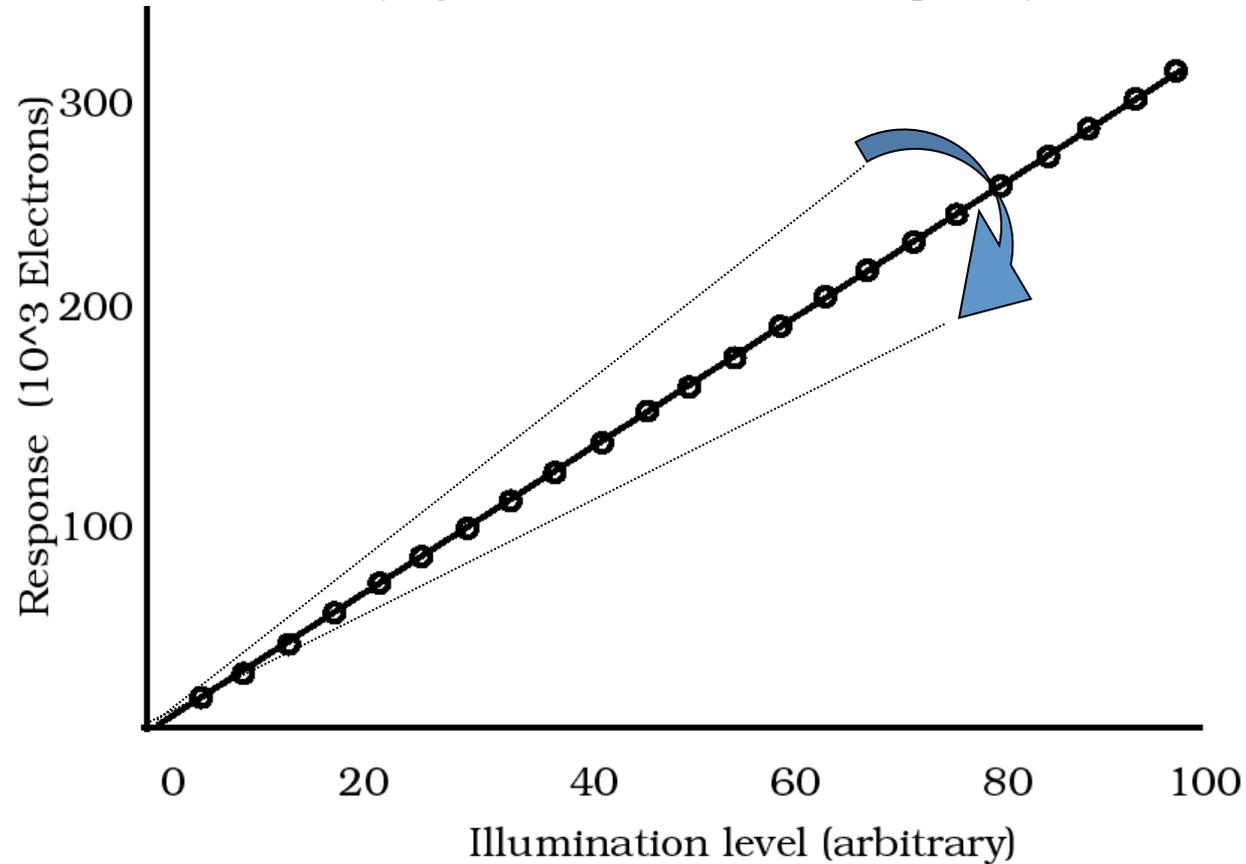


# Sensor imperfections: PRNU

Across the imager surface there are two principal imperfections:

DSNU and PRNU

Photoresponse non-uniformity (**PRNU**)  
Varying surface area or media transparency



(Epperson, P.M. et al. Electro-optical characterization of the Tektronix TK5 ..., Opt Eng., 25, 1987)

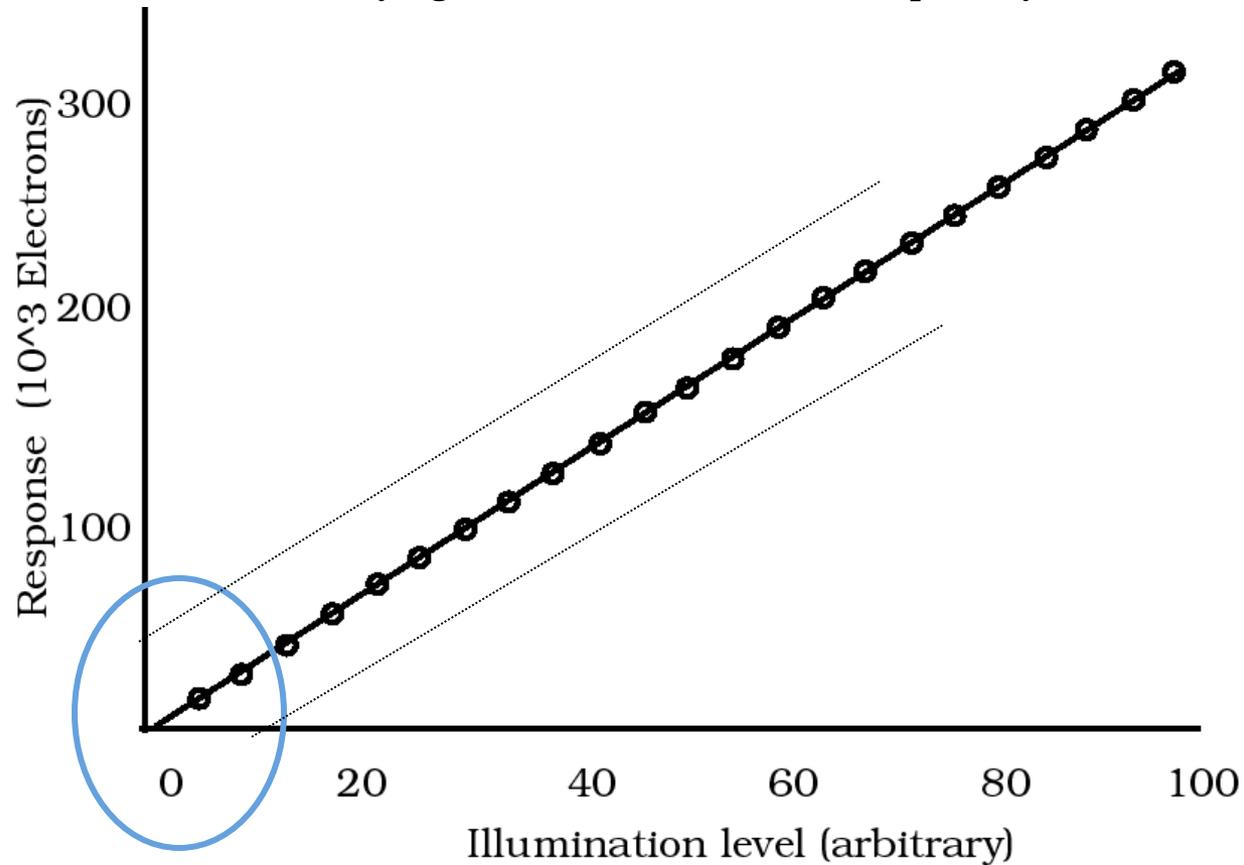
# Sensor imperfections: DSNU

Across the imager surface there are two principal imperfections:

DSNU and PRNU

Dark signal non-uniformity (**DSNU**)  
Varying leakage, reset

Photoresponse non-uniformity (**PRNU**)  
Varying surface area or media transparency



(Epperson, P.M. et al. Electro-optical characterization of the Tektronix TK5 ..., Opt Eng., 25, 1987)

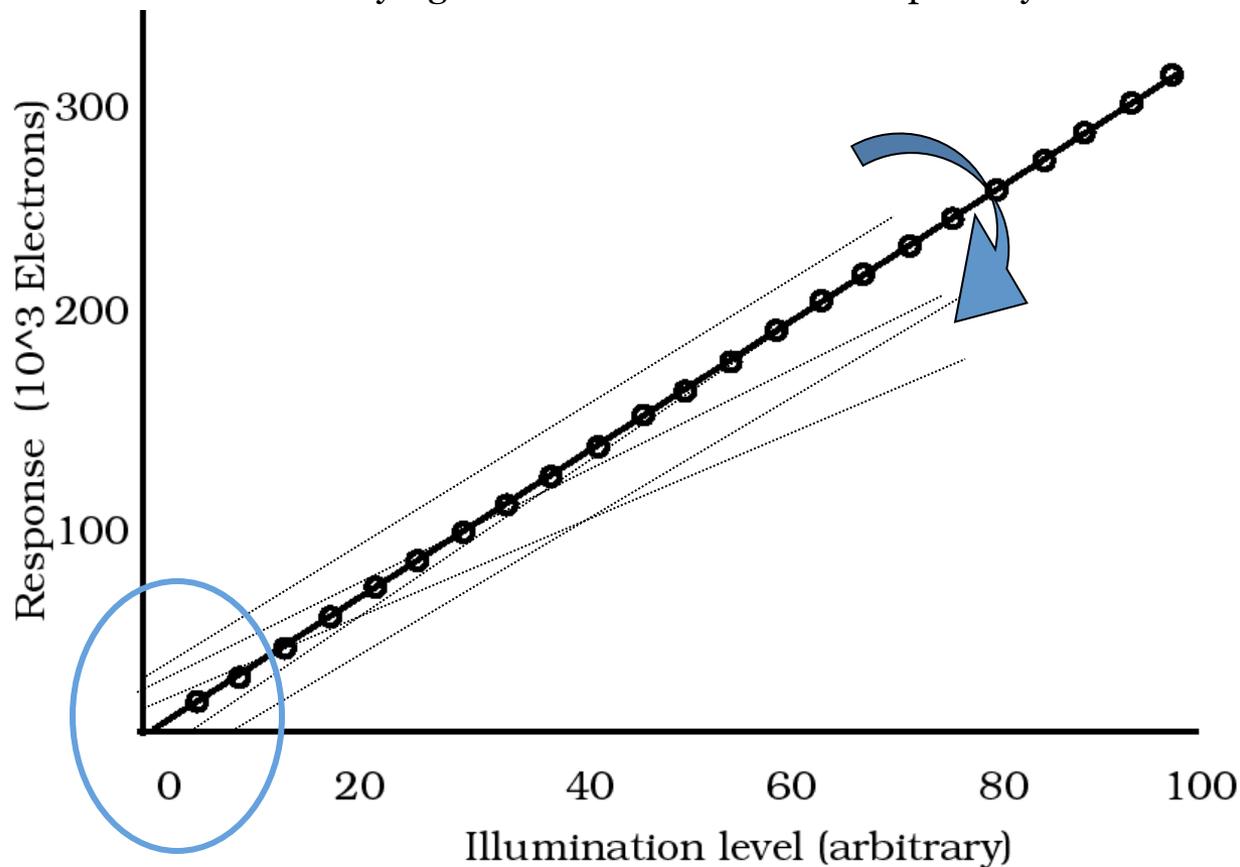
# Combined PRNU and DSNU

Across the imager surface there are two principal imperfections:

DSNU and PRNU

Dark signal non-uniformity (**DSNU**)  
Varying leakage, reset

Photoresponse non-uniformity (**PRNU**)  
Varying surface area or media transparency



(Epperson, P.M. et al. Electro-optical characterization of the Tektronix TK5 ..., Opt Eng., 25, 1987)

# Sensor imperfections

## Programmable gain/offset

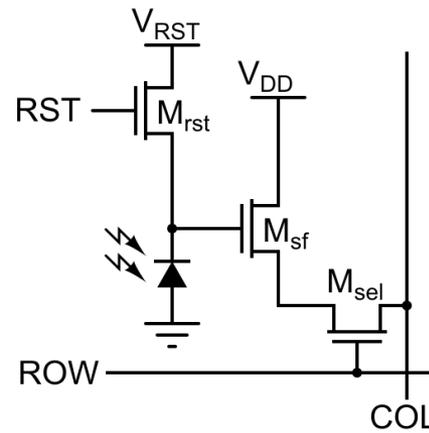
- Electrons (Poisson random variable) are converted to volts by circuit properties (conversion gain)
- Circuit imperfections introduce dark voltage ( $d$ ) that grows over time ( $T \cdot V/\text{sec}$ )
- The acts of reading and resetting the voltage are noisy (and can be grouped)
- Variations across the sensor in analog offset and gain; offset can be due to leakage and thus time-dependent

$$v_0 = c\tilde{e}$$

$$v_1 = v_0 + T\tilde{d}$$

$$v_2 = v_1 + \tilde{r}_0 + \tilde{r}_1$$

$$v_3 = \tilde{a}(v_2 + T\tilde{o})$$



Programmable gain amplifier and offset

# Terminology: Temporal and fixed noise

- **Temporal noise:** Some noise terms differ across repeated reads of the pixel (e.g., read noise, reset noise, dark noise, photon noise); these can be averaged away
- **Fixed pattern:** Some noise terms are simply variations of the device properties across the array; these are fixed over time (conversion gain, DSNU, PRNU, Column gain) and are not averaged away

$$v_0 = c\tilde{e}$$

$$v_1 = v_0 + T\tilde{d}$$

$$v_2 = v_1 + \tilde{r}_0 + \tilde{r}_1$$

$$v_3 = \tilde{a}(v_2 + T\tilde{o})$$

# Phenomonological model

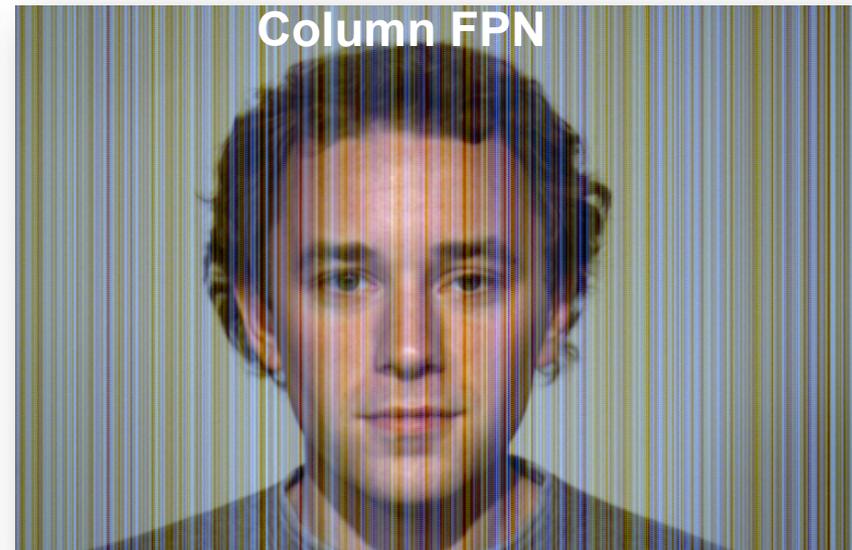
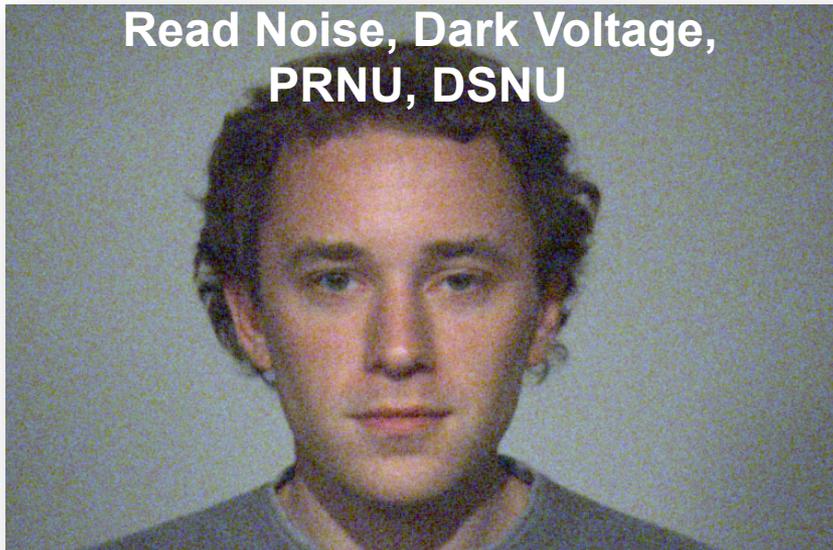
$$v = \tilde{Z}(\tilde{e} + \tilde{X} + T\tilde{Y})$$

Knowledge of the noise mechanisms is important for accurate simulation because the mechanisms have different temporal and spatial characteristics; in this form the equation does not make this important issue clear.

# Column amplifier variation:

A special place in imaging hell

Fixed column noise



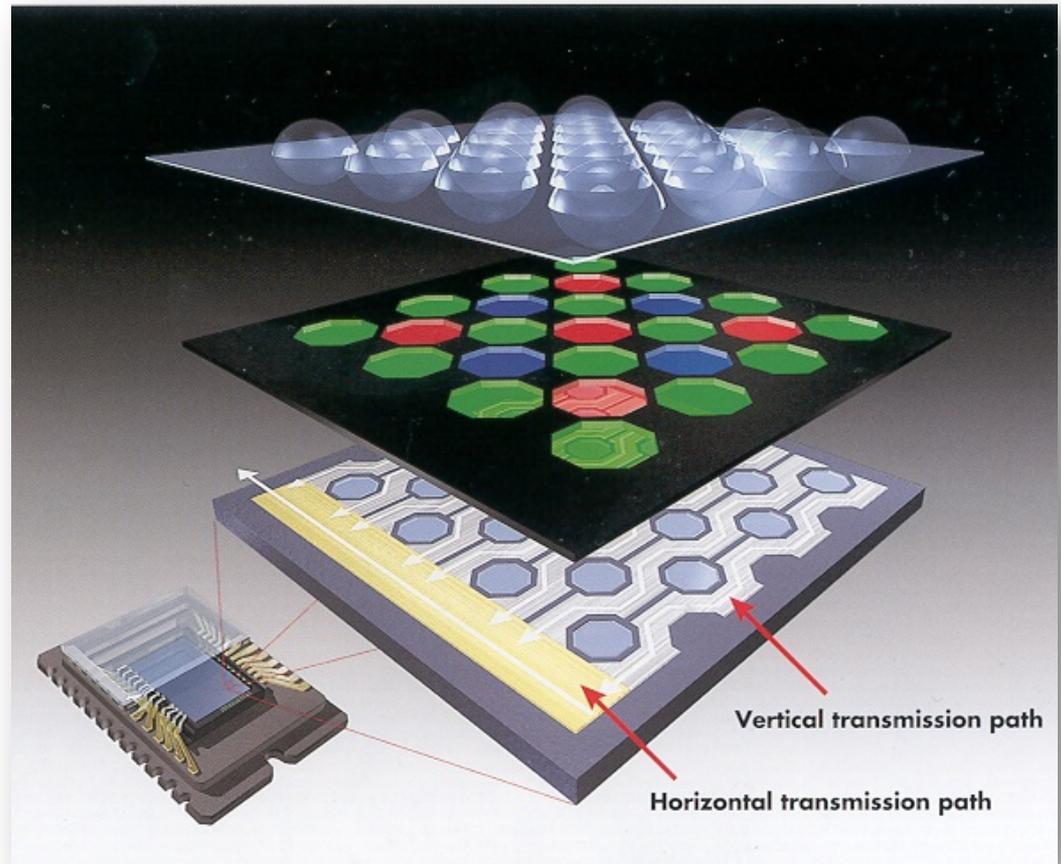
In some systems, an entire column shares an amplifier. In this case, variations between the column amplifiers produce unwanted variations (as above). Consistent column variations are very noticeable and thus must be eliminated.

# Imager components

- Anti-aliasing and infrared filter
- Color filter array types



# Sensor Properties: Overview



- Pixel Properties
  - Pixel height, width
  - Fill factor
  - Dark current
  - Read noise
  - Conversion gain
  - Voltage swing

- Array Properties
  - DSNU and PRNU
  - Pixel spacing
  - Number of pixels

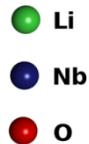
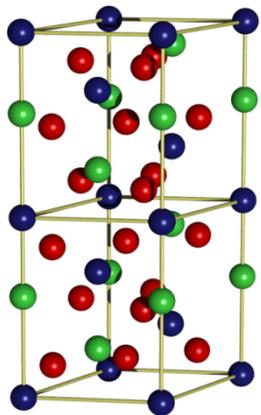
- Color Properties
  - Color filter, transmittance
  - Photodetector QE
  - Infrared filter transmittance
  - Color filter array pattern

- Circuit Properties
  - Analog-to-digital conversion
  - Correlated Double Sampling
  - Column Amplifiers (Column FPN)

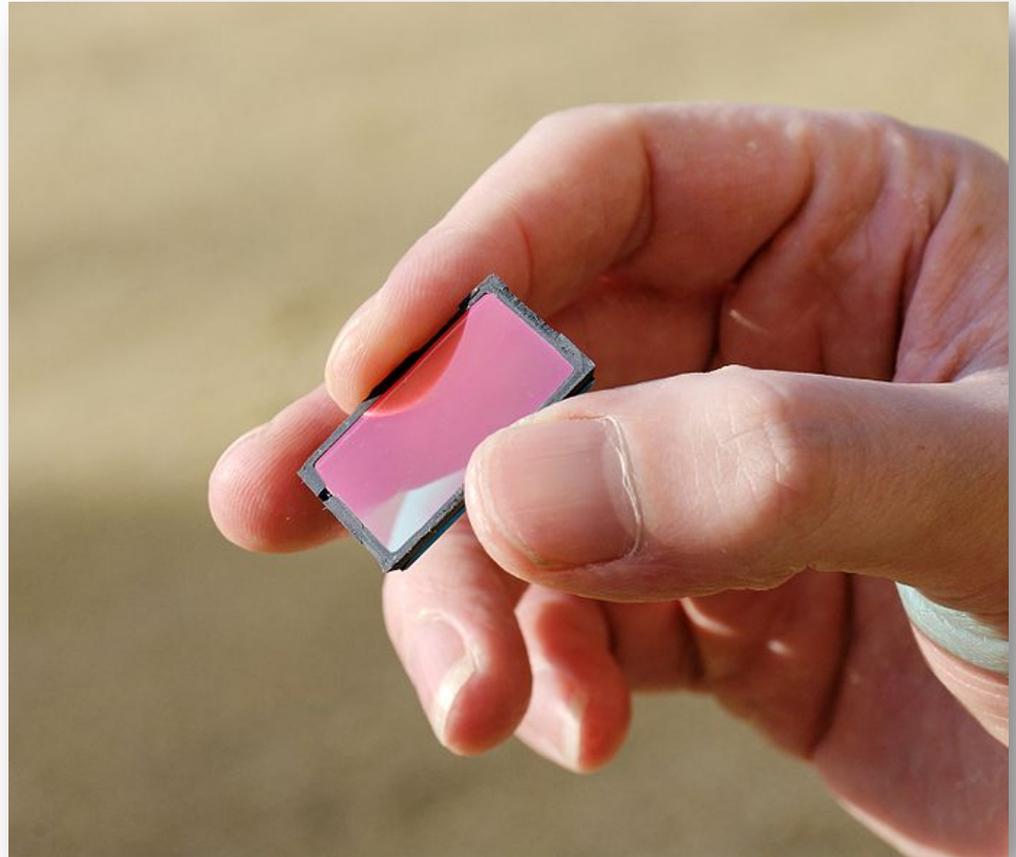
- Pixel Optics
  - Microlens array

# Anti-aliasing and infrared blocking filter

- Placed on the sensor surface
- Blocks IR – to discuss
- Blurs to prevent sampling artifacts –to discuss
- Two types – birefringent and diffusing



*lithium niobate is a  
commonly used  
birefringent material*



# The microlens array

Anti-aliasing IR blocker

Microlens array

CMY Color Filter

Anti-Reflection Coating

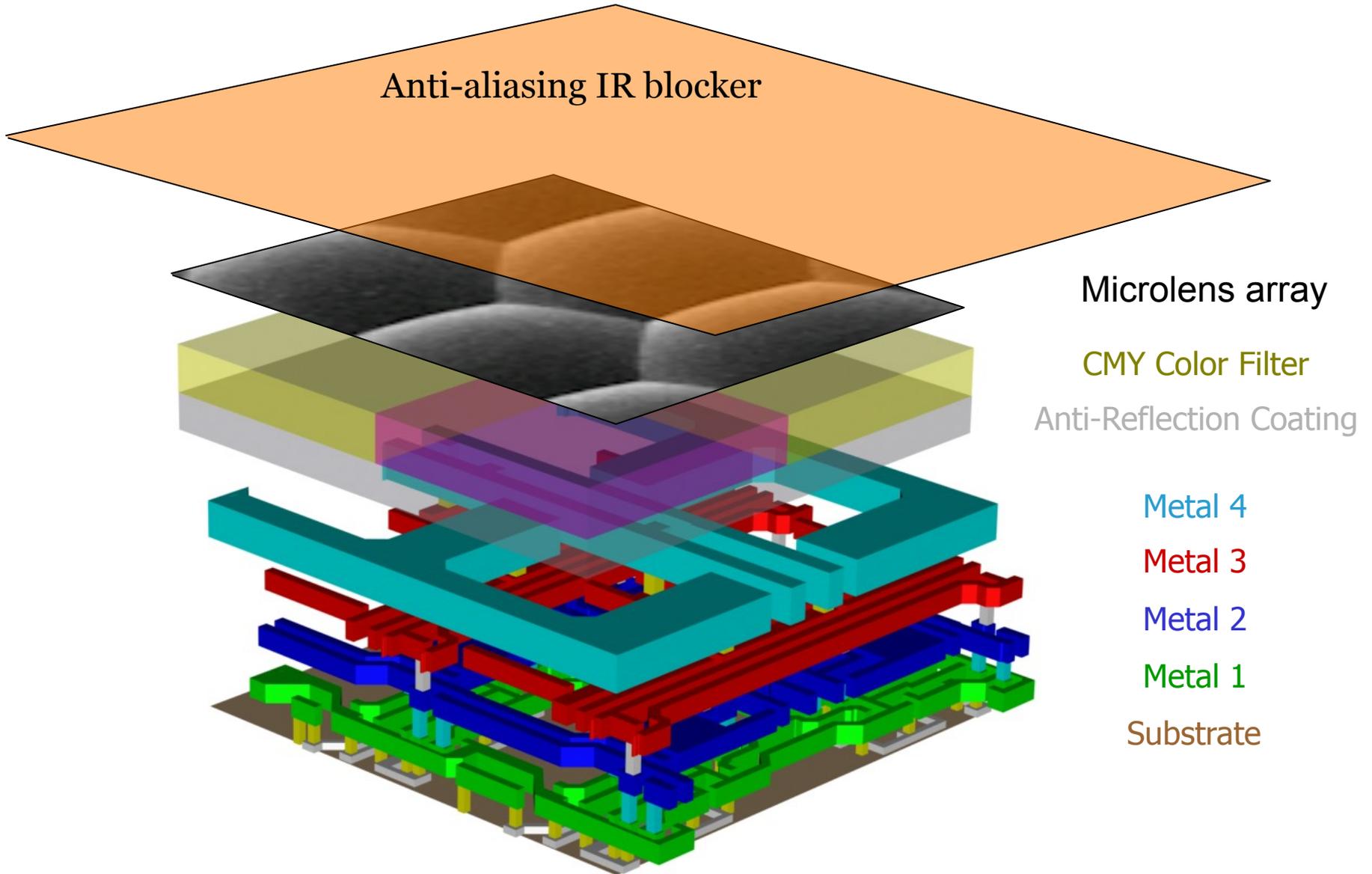
Metal 4

Metal 3

Metal 2

Metal 1

Substrate

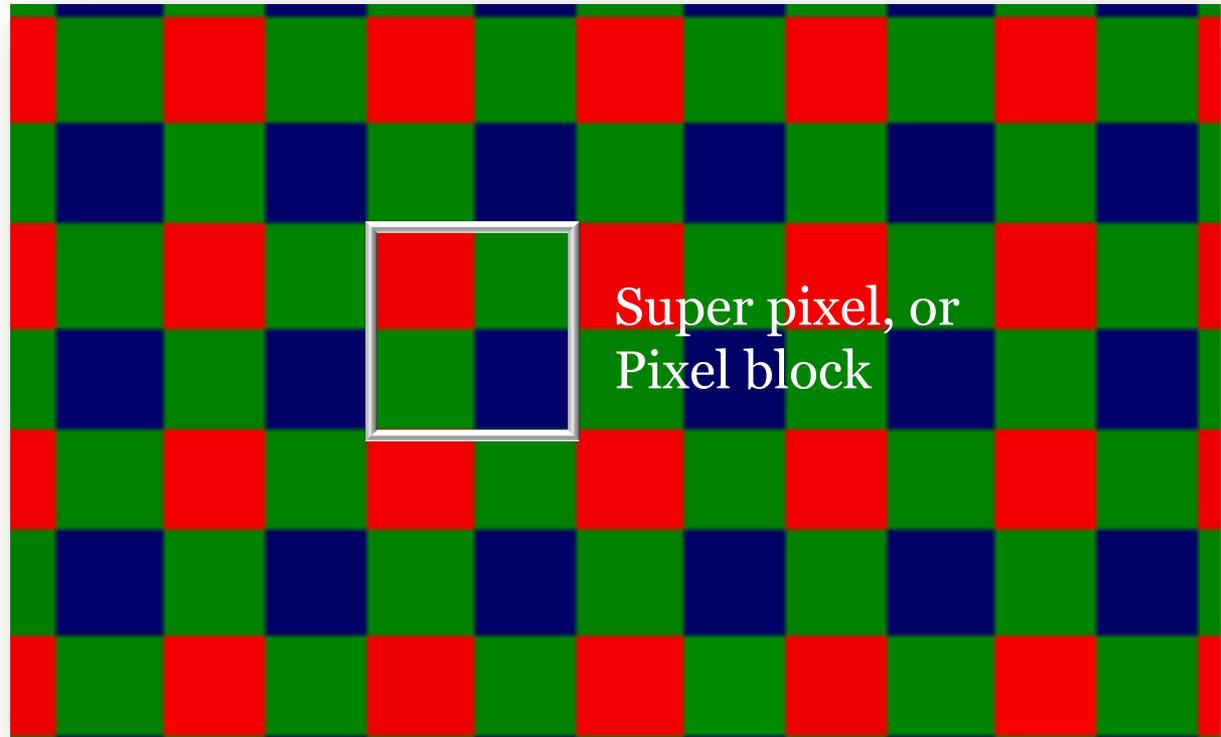


# The anti-aliasing filter and the CFA

The 4 pixels in a Bayer pixel block are combined to produce the RGB values displayed in a single pixel in the display

Thus, we want these 4 pixels to see the same point in the visual field

To achieve this, the image must not vary over space faster than the size of the pixel block



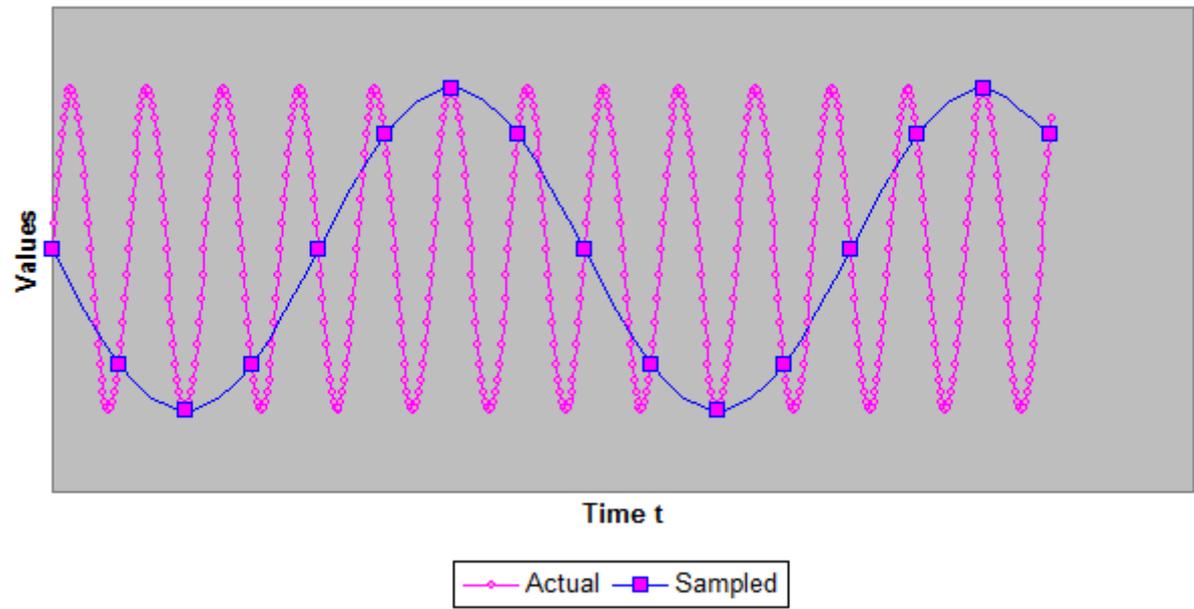
# Anti-aliasing filter effect

t\_cameraAntiAliasing.m

Classically, aliasing refers to the fact that when we under sample a space-varying image, the measured values appear to be at a different frequency from the original signal

In this case, the true signal is rapidly varying; the samples are evenly spaced by too slow to pick up the rapid variation

The sampled signal appears to be low, rather than high, frequency

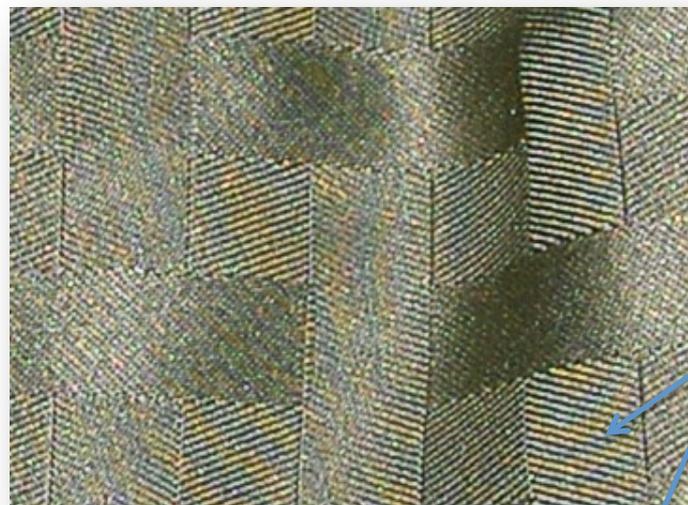


# Anti-aliasing effects

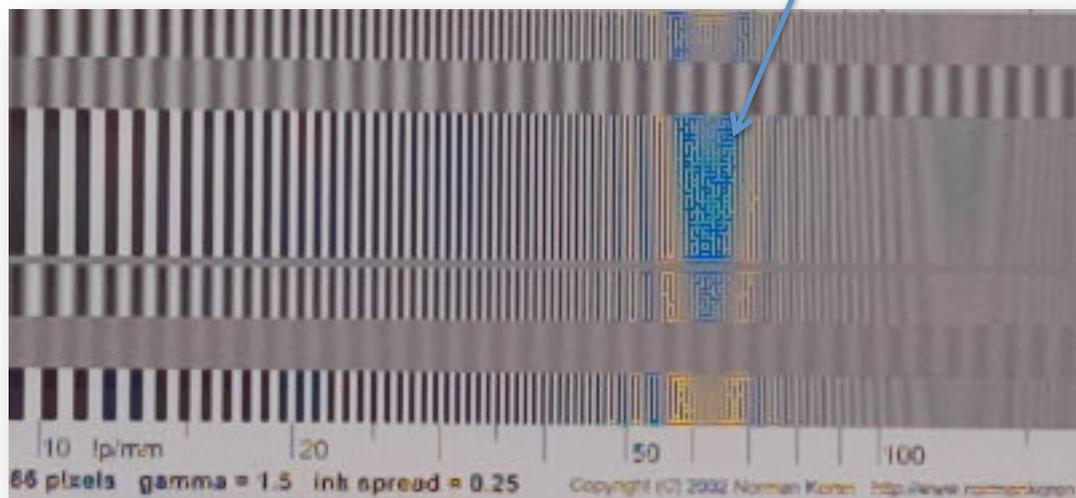
s\_sensorAliasing.m

The consequence of this under-sampling in imaging with color sensors is a combination of aliasing and unwanted chromatic artifacts

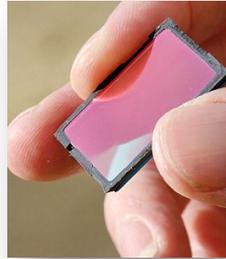
The chromatic artifacts arise because we need to account not only for the sampling rate but for the fact that we are sampling with pixels that have different color sensitivities



Chromatic artifacts



# Anti-aliasing filter effect



No filter  
(Sharp, but aliased)

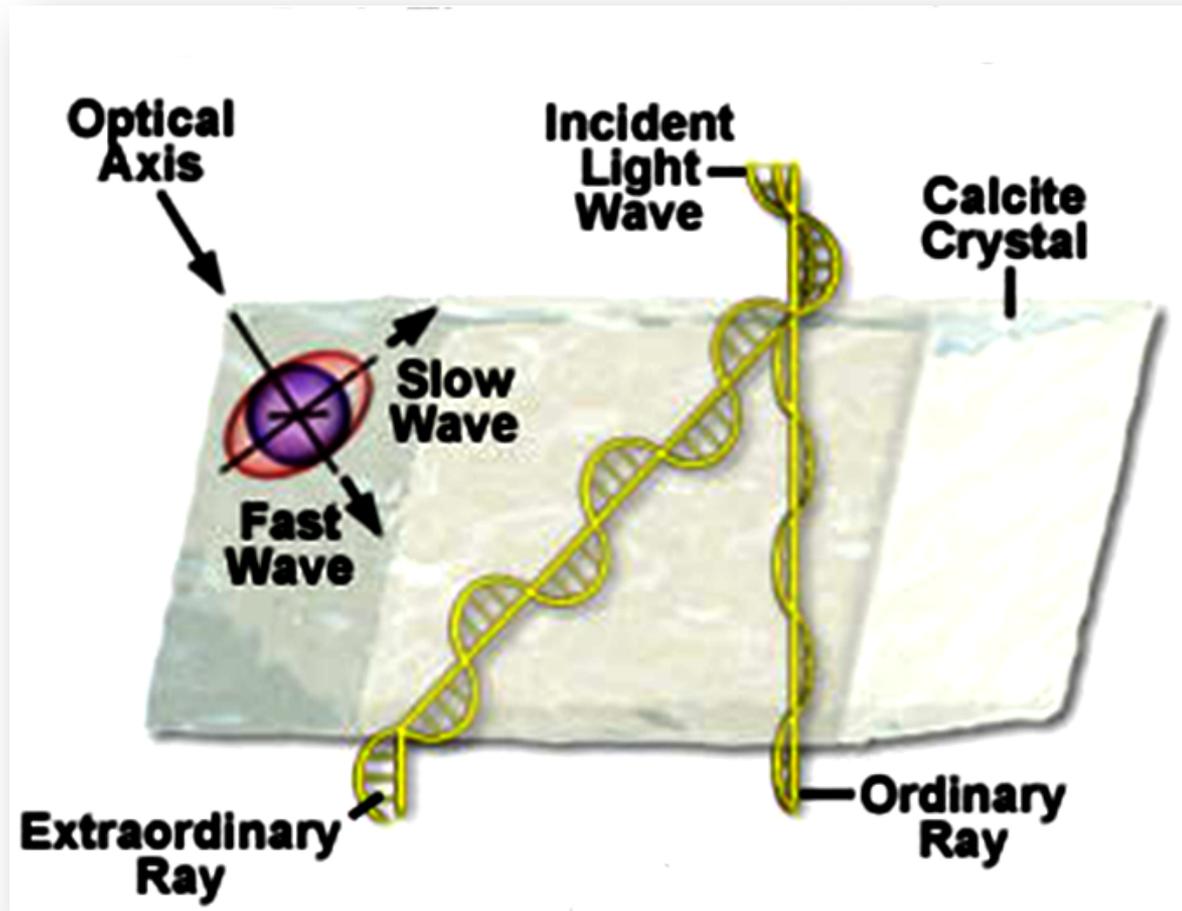


With filter  
(Blurry, but less aliasing)



# Anti-aliasing with birefringence filters

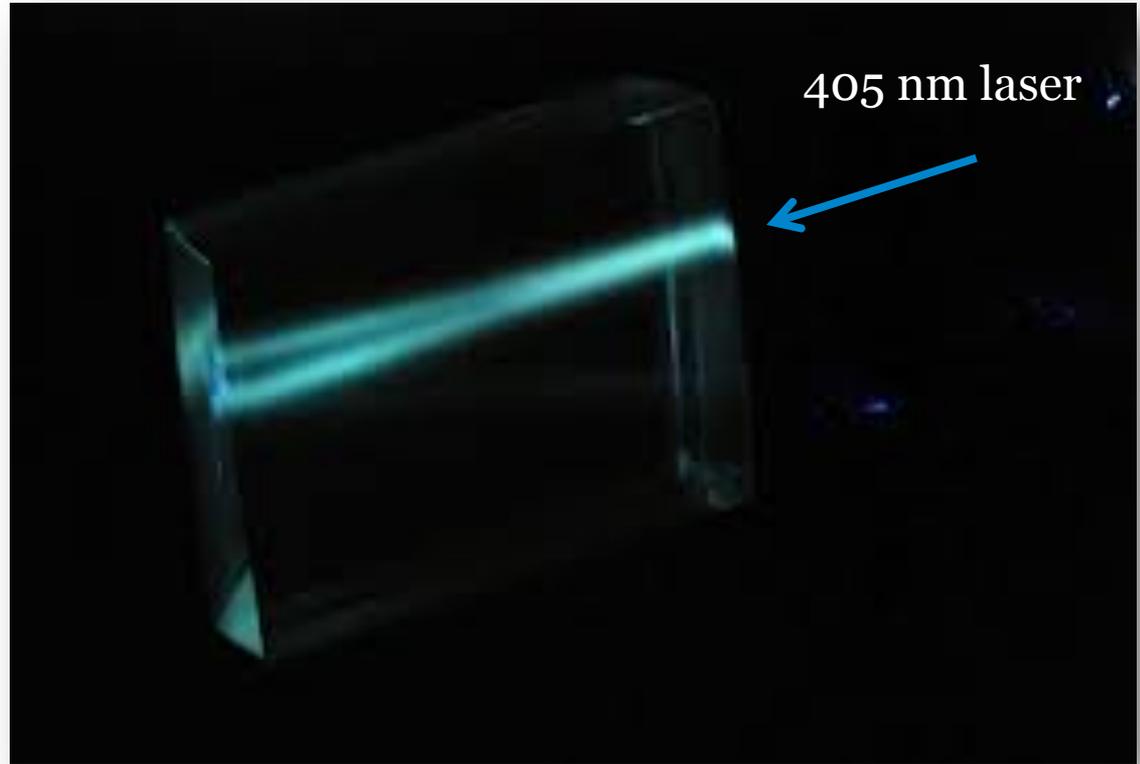
Light through a calcite crystal  
Divided into an ordinary and  
extraordinary ray  
Displaced in position  
Different polarizations



# Birefringence

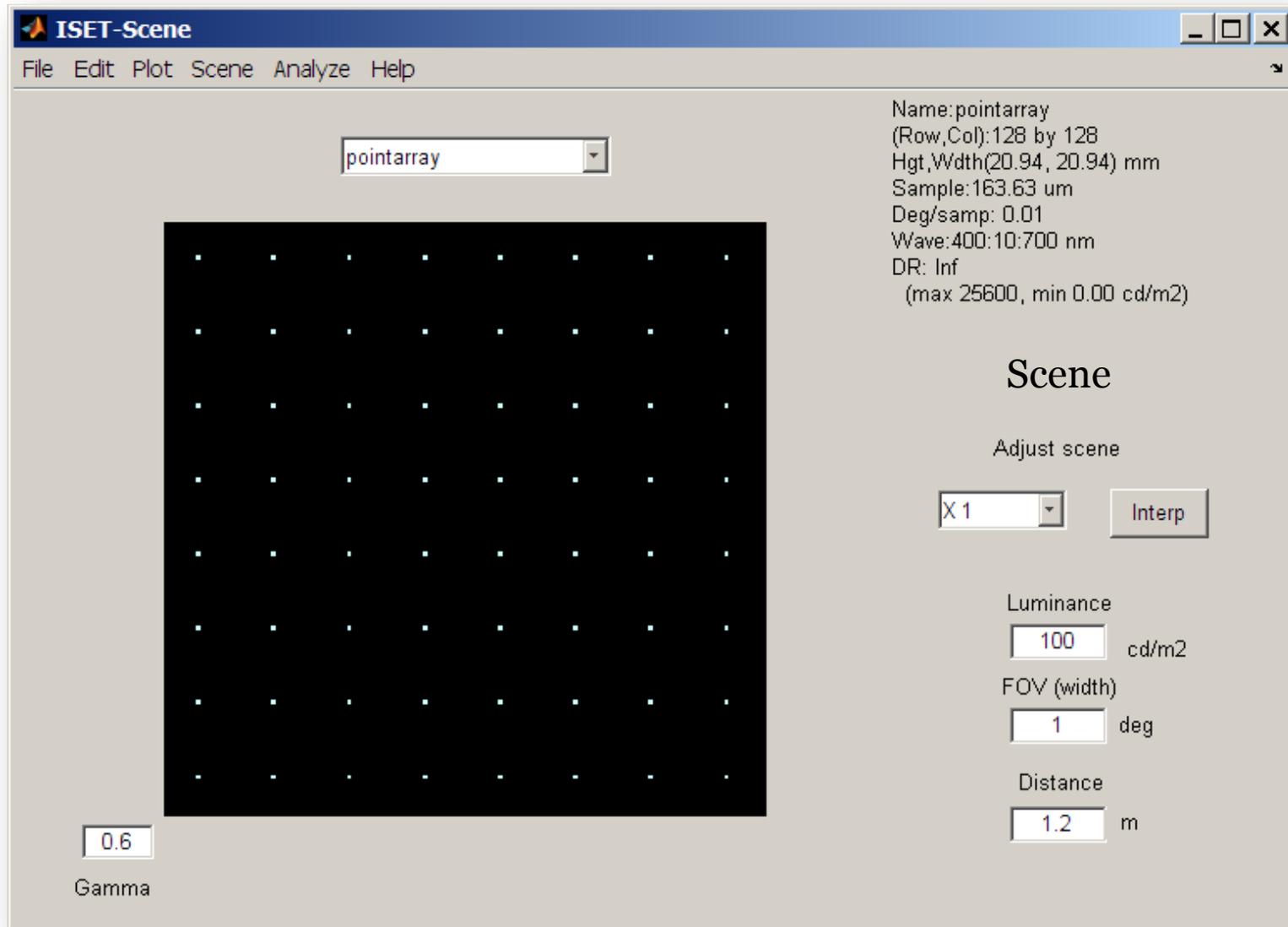
Ordinary and extraordinary ray positions can be seen easily

2mm block of calcite



# Modeling the anti-aliasing filters

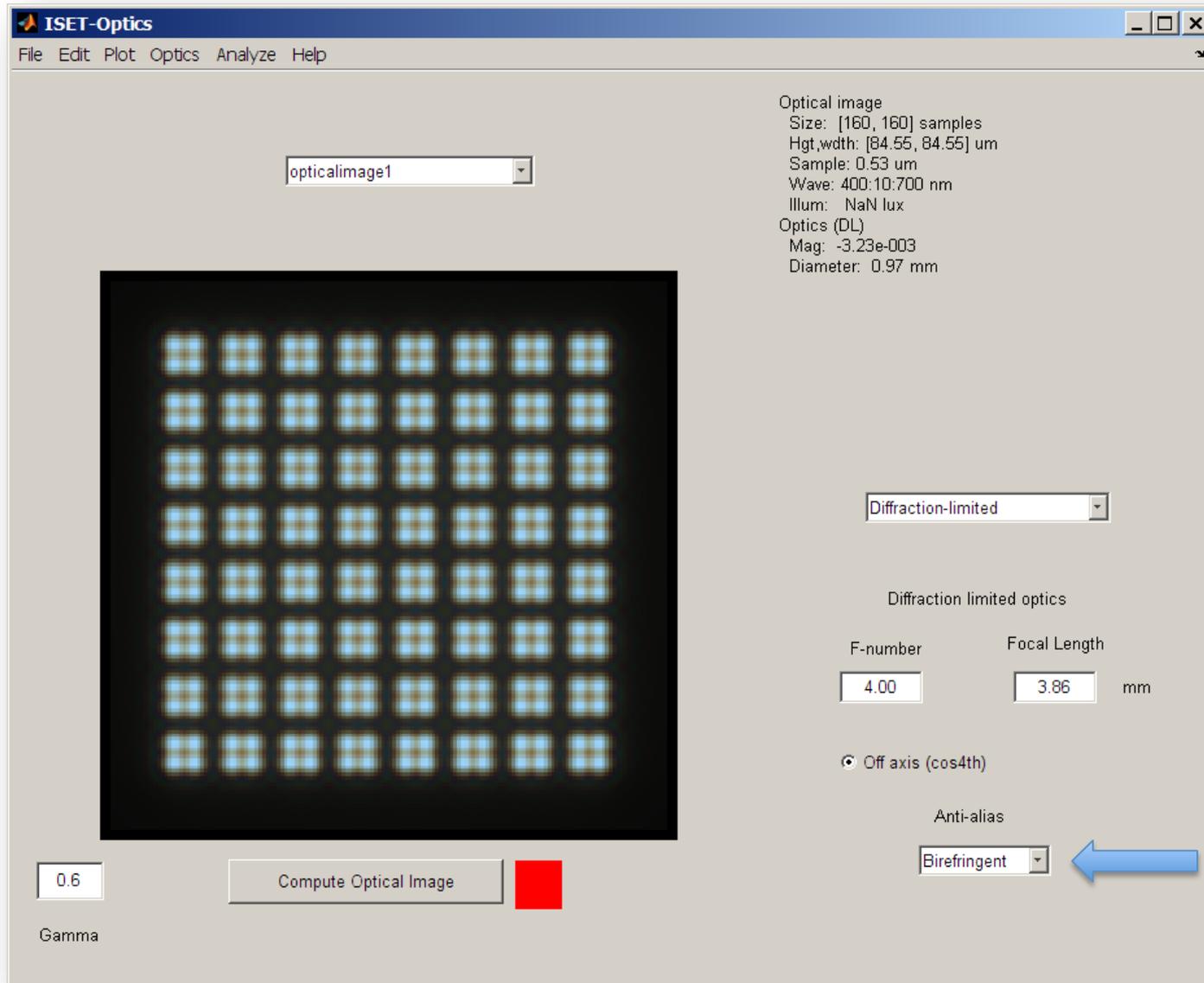
## Scene of point array



# Modeling the anti-aliasing filter:

## Optical image with birefringent filter

Two filter layers,  
rotated,  
produce  
four spots



# Modeling the anti-aliasing filter:

## Diffusing filter

**ISET-Optics**

File Edit Plot Optics Analyze Help

opticalimage1

Optical image  
Size: [160, 160] samples  
Hgt,width: [84.55, 84.55] um  
Sample: 0.53 um  
Wave: 400:10:700 nm  
Illum: 3.1 lux  
Optics (DL)  
Mag: -3.23e-003  
Diameter: 0.97 mm

Optical image

Diffraction-limited

Diffraction limited optics

F-number      Focal Length

4.00      3.86 mm

Off axis (cos4th)

Anti-alias

Blur      2 FWHM (um)

0.6      Compute Optical Image

Gamma      Perform calculation

# ISET simulation

ISET-Sensor

File Edit Plot Sensor Analyze Help

Pixel (H,W): (1.5,1.5) um  
PD (H,W): (1.3, 1.3) um  
Fill percentage: 75  
Well capacity 10000 e-  
DR (1 ms): 57.0 dB  
Peak SNR: 40 dB

Size (H,W): (0.28, 0.34) mm  
Sensor DR: 60.0 dB  
Sensor FOV: 5.01 deg  
Wave: 400:10:700 nm  
CFA: [rgb] CDS: [off] - OE Method: [skip]

<- bayer-0 >-

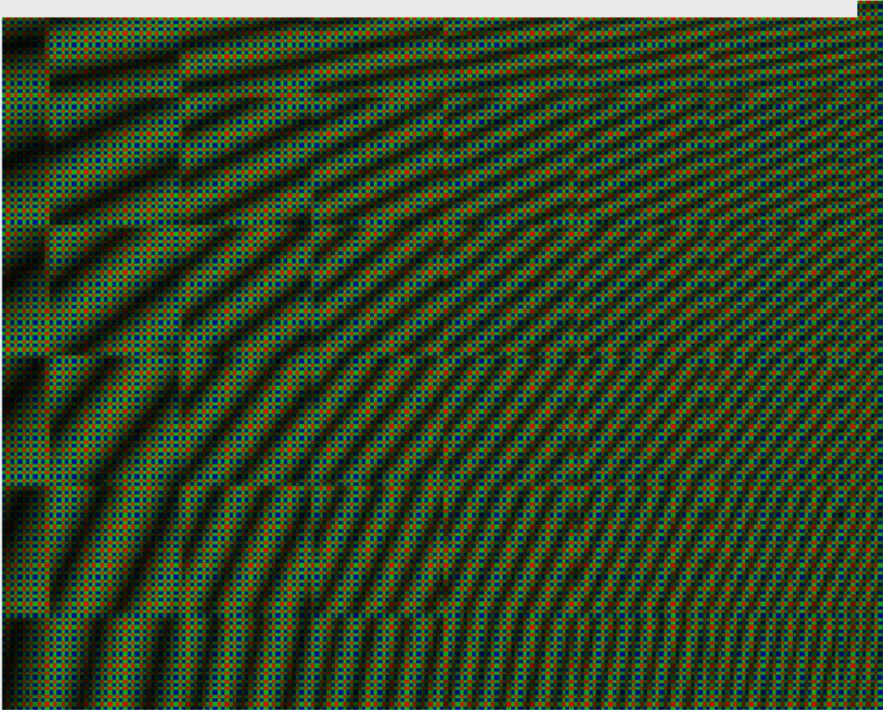
**Pixel**

Dk  
1.0 mV/pixel/se

Read  
1.0 mV

Conv.  
100.0 uV/e-

Volt  
1.00 V



Standard CFA  
bayer-g... >-

Quantization  
Analog >-

Sensor pixels (r,c)  
184 226 >-

Single >-

... 84.82 (ms)

DSNU PRNU  
0.0 0.0  
mv %

1  Scale  
Gamma

Compute Sensor Image 

# No real difference at sensor

**ISET-Sensor**

File Edit Plot Sensor Analyze Help

Pixel (H,W):(2.8,2.8) um  
PD (H,W):(2.0, 2.0) um  
Fill percentage:50  
Well capacity:10000 e-  
DR (1 ms):57.0 dB  
Peak SNR:40 dB

## Diffuser

bayer-0

Size (H,W):(0.40, 0.49) mm  
Sensor DR:38.6 dB  
Sensor FOV:7.28 deg  
Wave:400:10:700 nm  
CFA: [gbrg] CDS: [off] - OE Method: [skip]

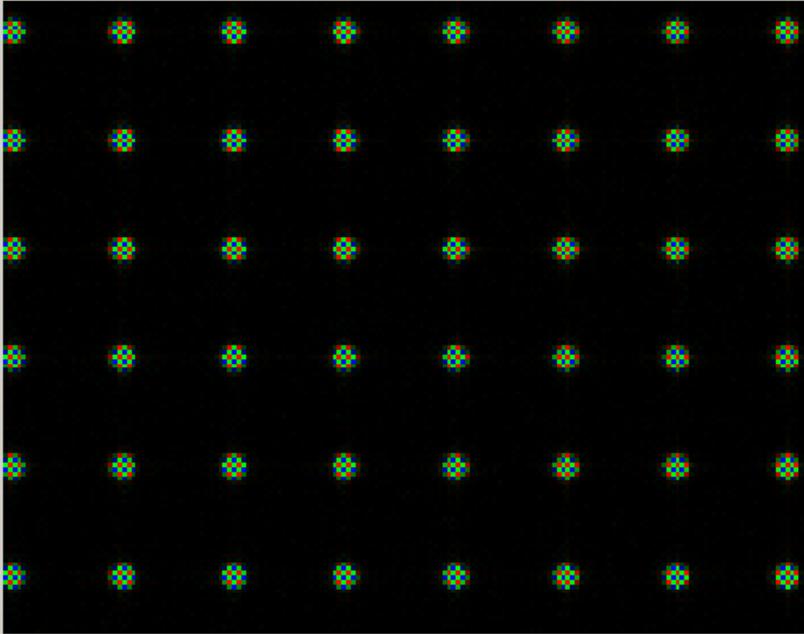
**Pixel**

Dk Voltage  
1.0 mV/pixel/sec

Read Noise (sd)  
1.0 mV

Conv. Gain  
100.0 uV/e-

Volt Swing  
1.00 V



Custom Compute

Standard CFA  
bayer-grbg

Quantization  
Analog

Sensor pixels (r,c)  
144 176 X 4

Single

Auto 35.92 (ms)

DSNU 10.0 mv  
PRNU 5.0 %

1  Scale  
Gamma

Compute Sensor Image

# No real difference at sensor

**ISET-Sensor**

File Edit Plot Sensor Analyze Help

Pixel (H,W):(2.8,2.8) um  
PD (H,W):(2.0, 2.0) um  
Fill percentage:50  
Well capacity:10000 e-  
DR (1 ms):57.0 dB  
Peak SNR:40 dB

## Birefringent

bayer-0

Size (H,W):(0.40, 0.49) mm  
Sensor DR:38.6 dB  
Sensor FOV:7.28 deg  
Wave:400:10:700 nm  
CFA: [gbrg] CDS: [off] - OE Method: [skip]

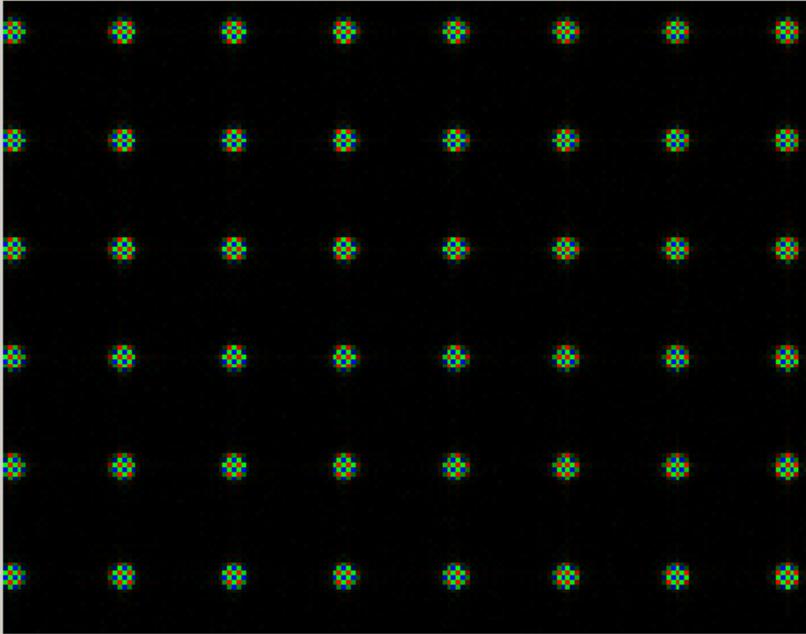
**Pixel**

Dk Voltage  
1.0 mV/pixel/sec

Read Noise (sd)  
1.0 mV

Conv. Gain  
100.0 uV/e-

Volt Swing  
1.00 V



Custom Compute

Standard CFA  
bayer-grbg

Quantization  
Analog

Sensor pixels (r,c)  
144 176 X 4

Single

Auto 35.92 (ms)

DSNU 10.0 mv  
PRNU 5.0 %

1  Scale  
Gamma

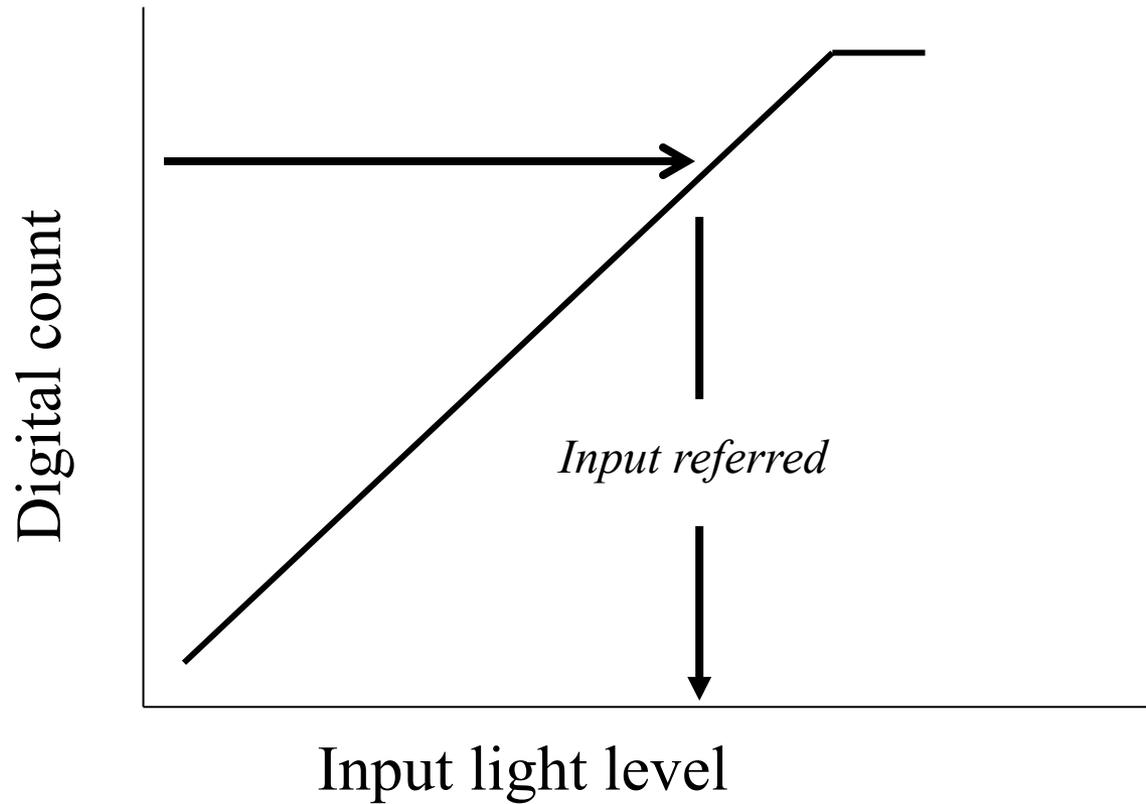
Compute Sensor Image

# Sensor dynamic range



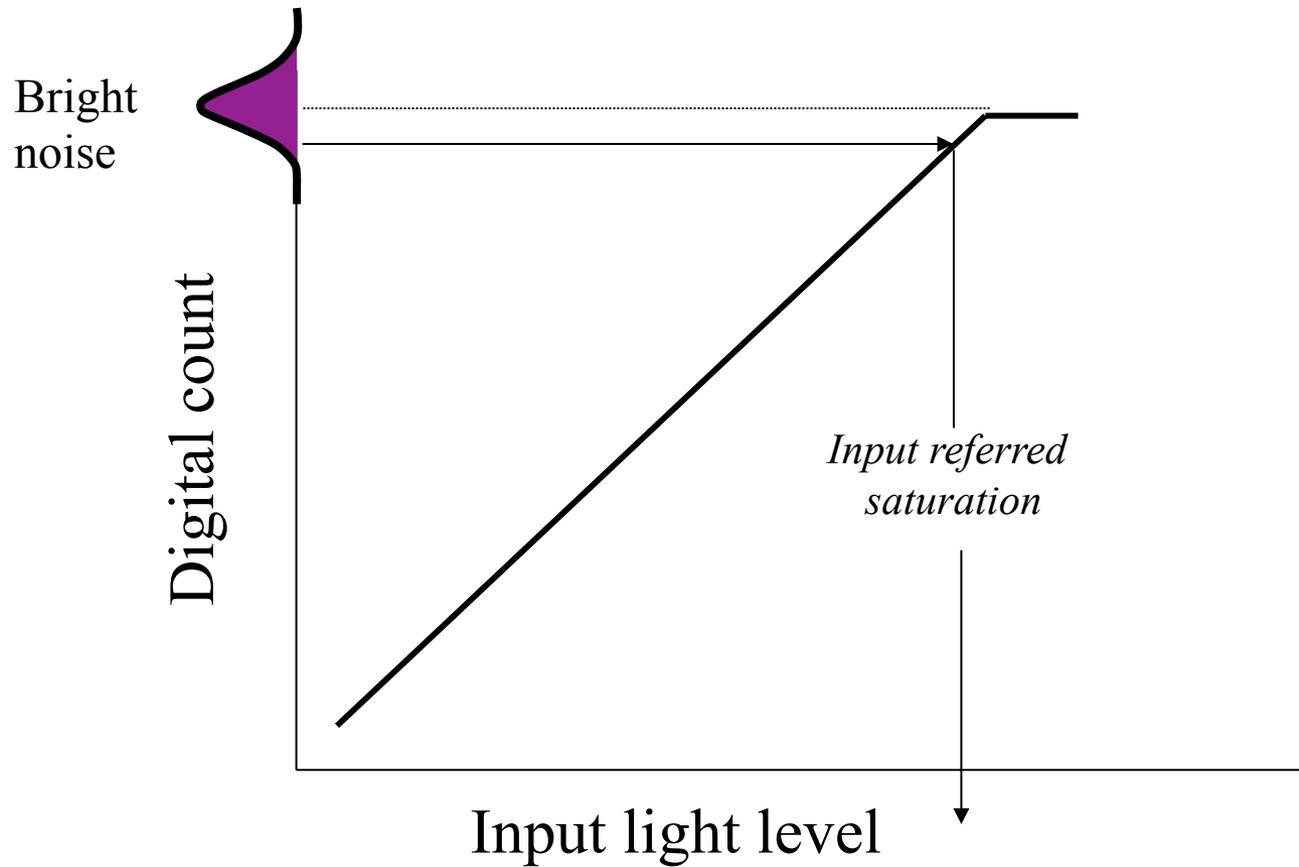
# Sensor dynamic range

*Input referred signals*



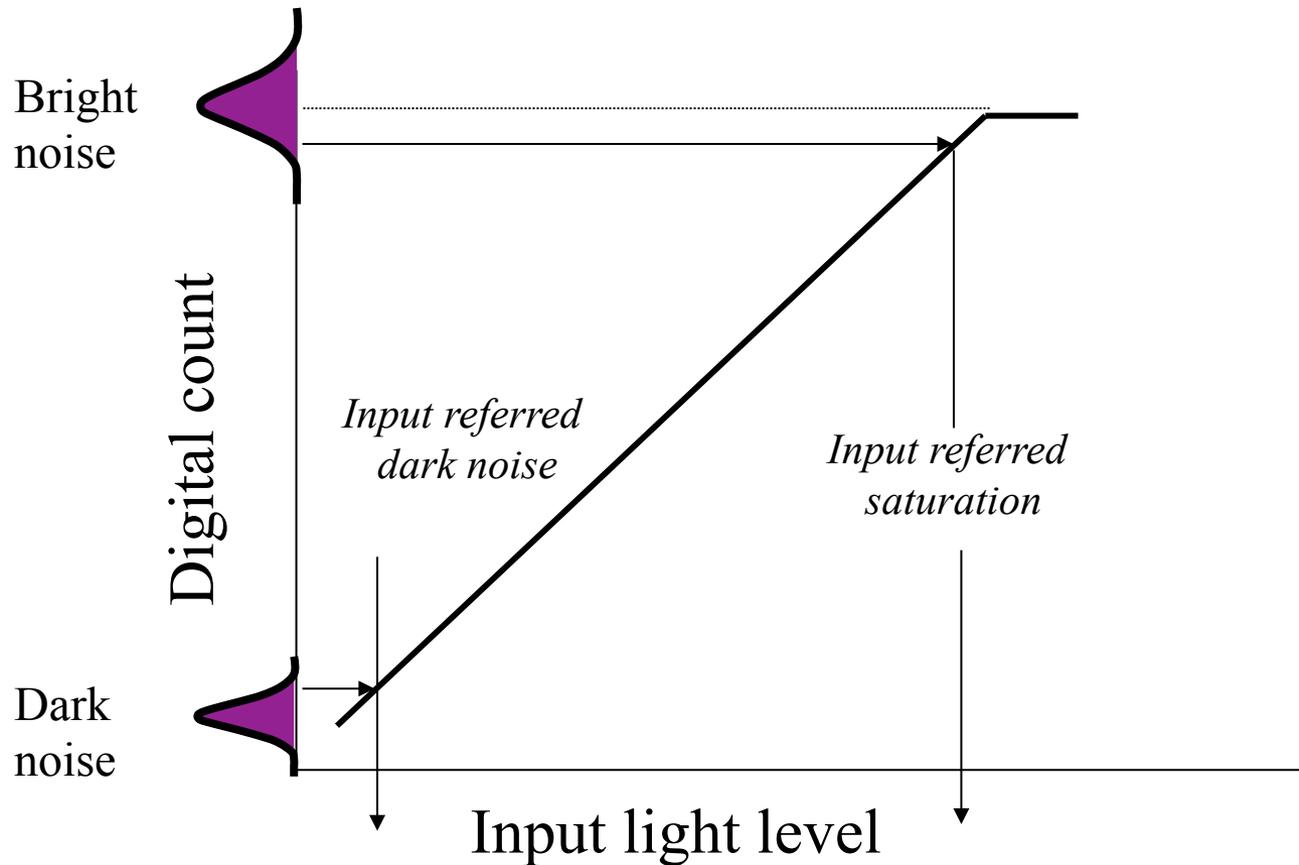
# Sensor dynamic range

*Saturation noise levels*



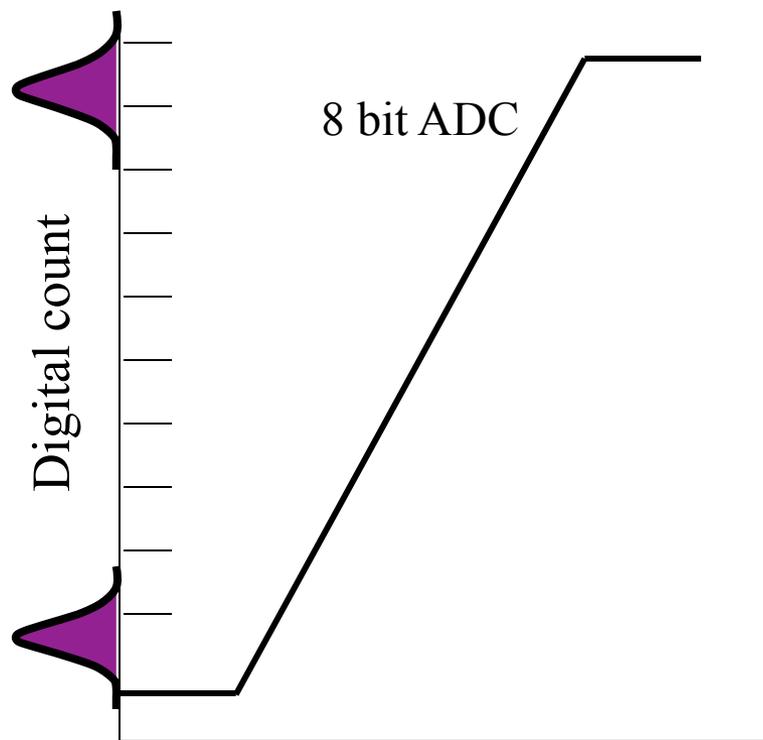
# Sensor dynamic range

*Ratio of saturation and dark noise levels*

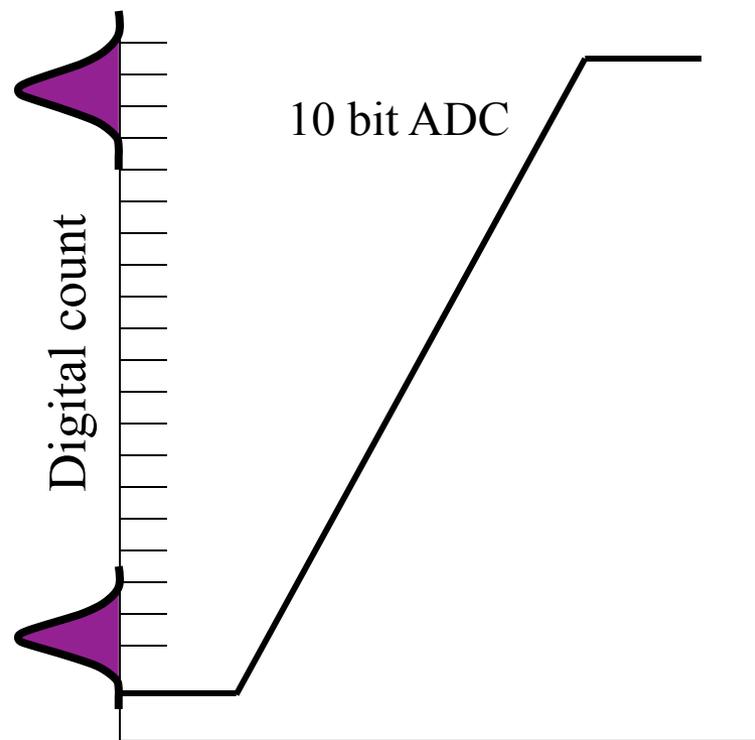


# Dynamic range and quantization

*Because dynamic range is stimulus-referred, quantization doesn't influence DR -- unless the bin size was set **very** badly (coarsely)*



Input light level



Input light level

# High Dynamic Range Imaging of Natural Scenes

*Volume 10/Nov. 2002/ Color Imaging Conference*

*Feng Xiao, Jeffrey M. DiCarlo, Peter B. Catrysse and Brian A. Wandell*

*Stanford University*

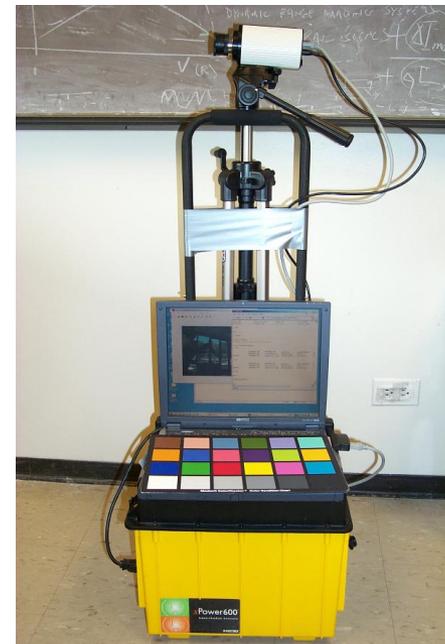
*Stanford, California*

## Rendering high dynamic range images

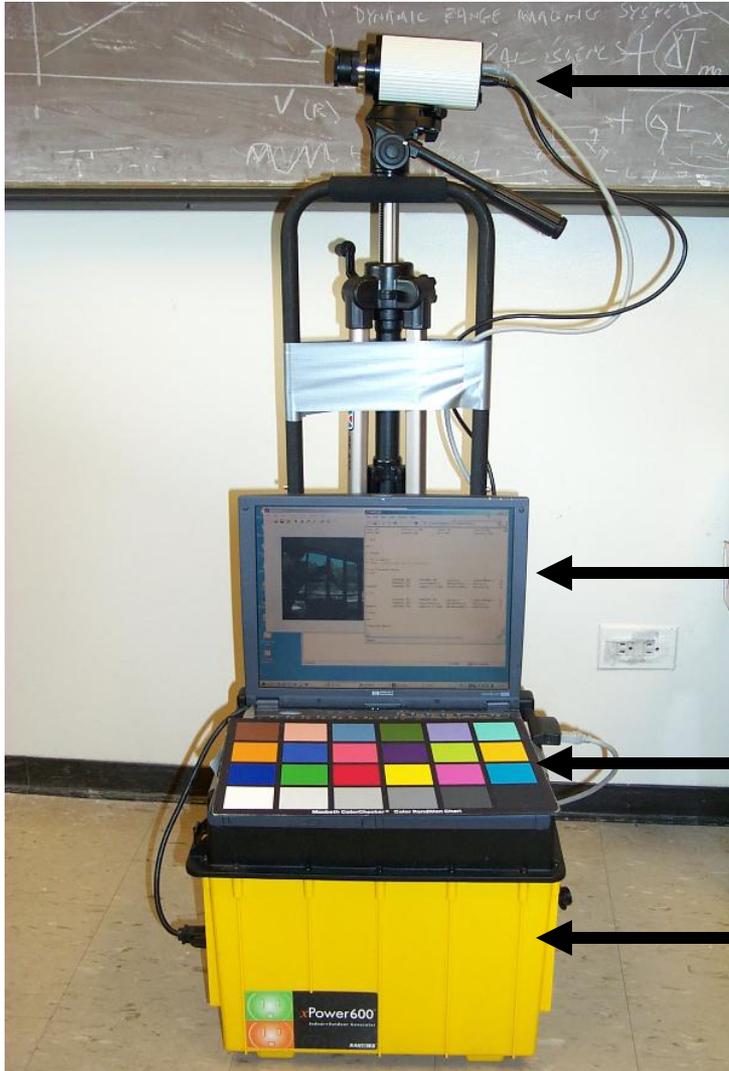
*Proceedings of the SPIE (2000), V. 3965, pp. 392-401*

Jeffrey M. DiCarlo<sup>\*a</sup> and Brian A. Wandell<sup>a,b</sup>

<sup>a</sup>Department of Electrical Engineering, Stanford University, CA 94305



# HDR: How High Is High?



*Camera*

*Laptop*

*Calibration target*

*Battery*

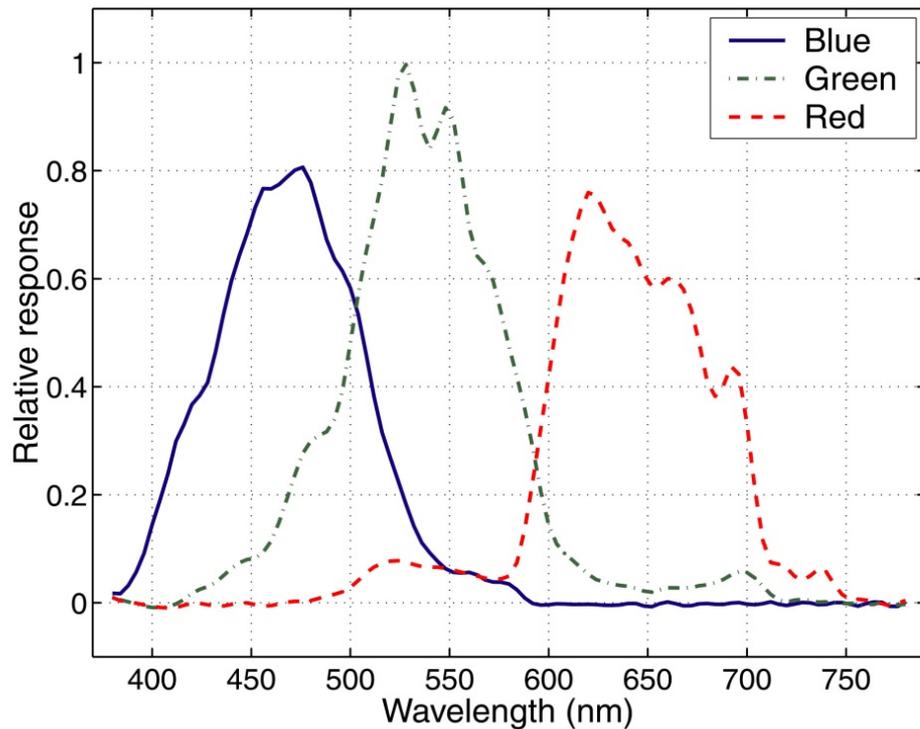


Sunlight

Shade



# System calibration



Dark current < 0.03 DV/sec  
Readout noise < 0.3 DV  
Exposure 40us ~ 15 minutes  
10-bit linear output  
1024x1280 Bayer pattern

# Multiple Exposures for HDR Capture



Increases DR by factor:

$$\frac{T_{long}}{T_{short}} \quad (\text{Yang et al. 99})$$

5-6 exposures at interval of 4 times

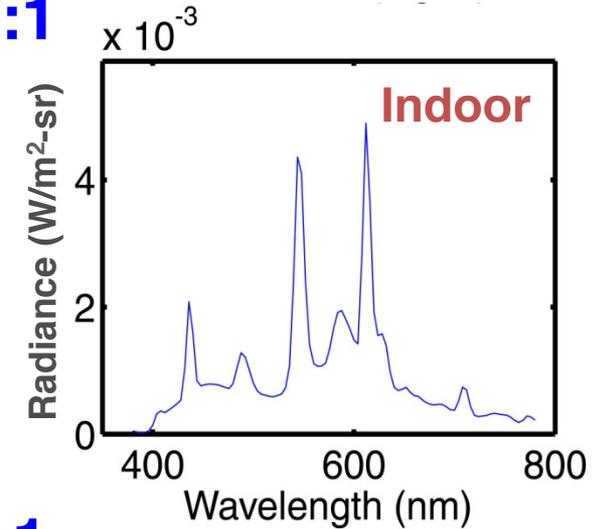
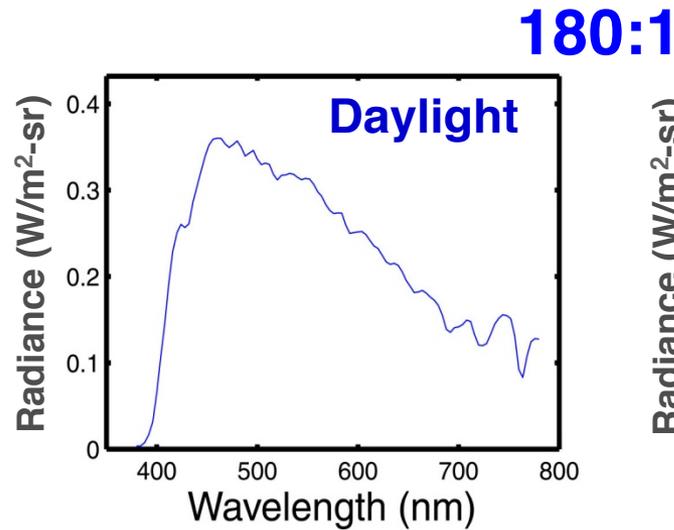
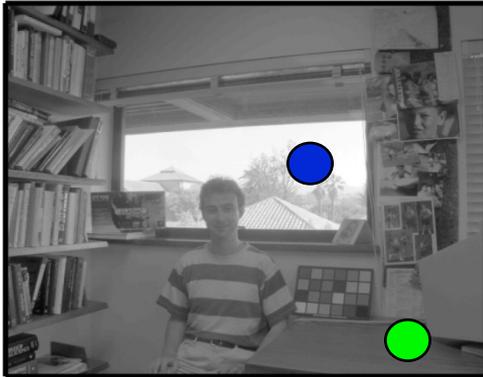
Measurable luminance range:

$[10^{-1} \sim 10^5 \text{ cd/m}^2]$

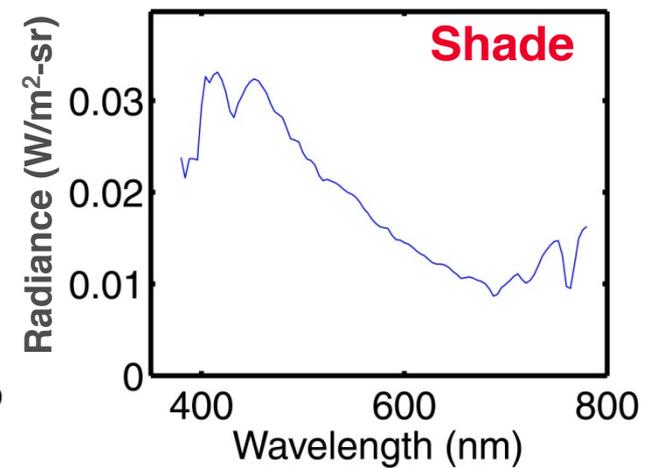
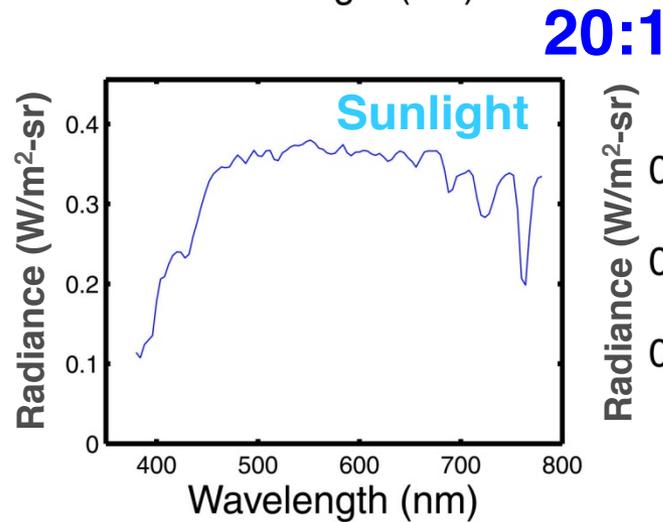
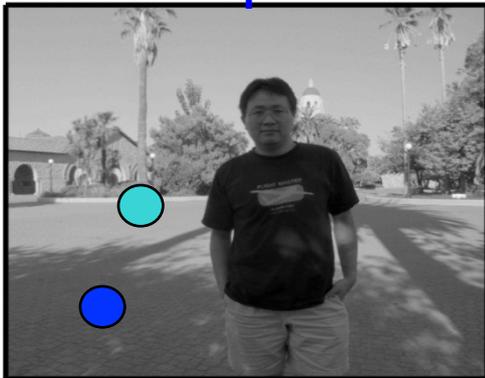
Dynamic range  $> 10^6:1$

# (1) HDR scenes have multiple illuminants

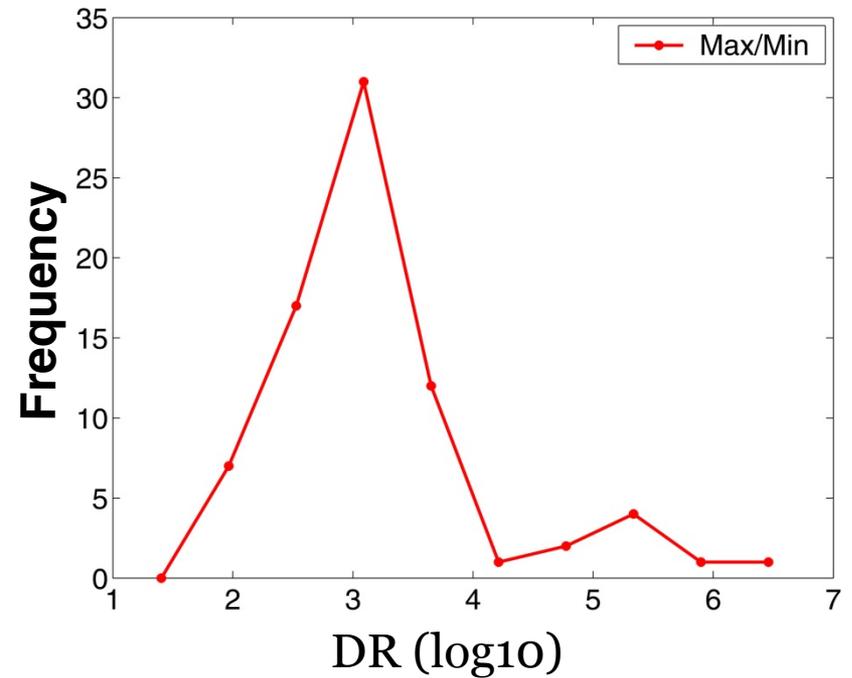
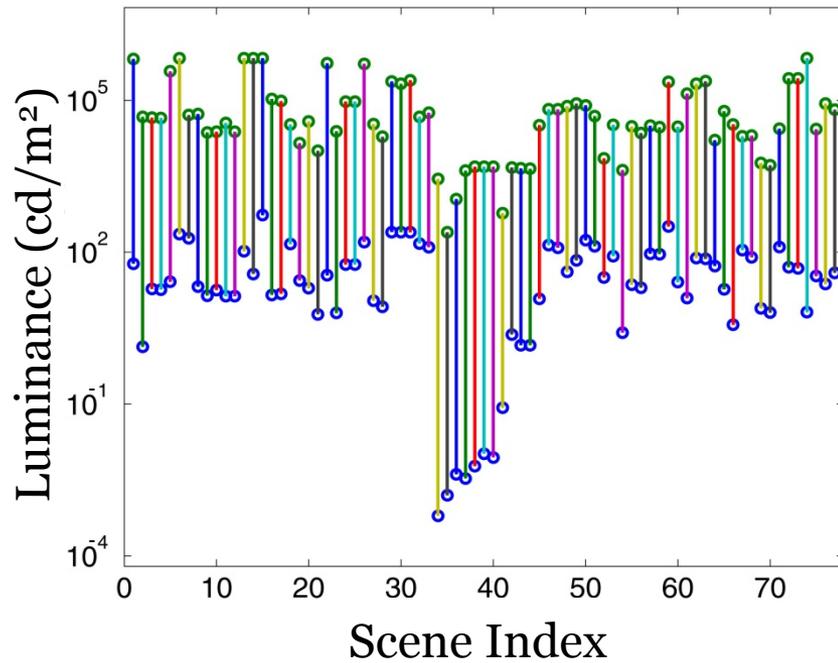
DR = 2000:1



DR = 400:1

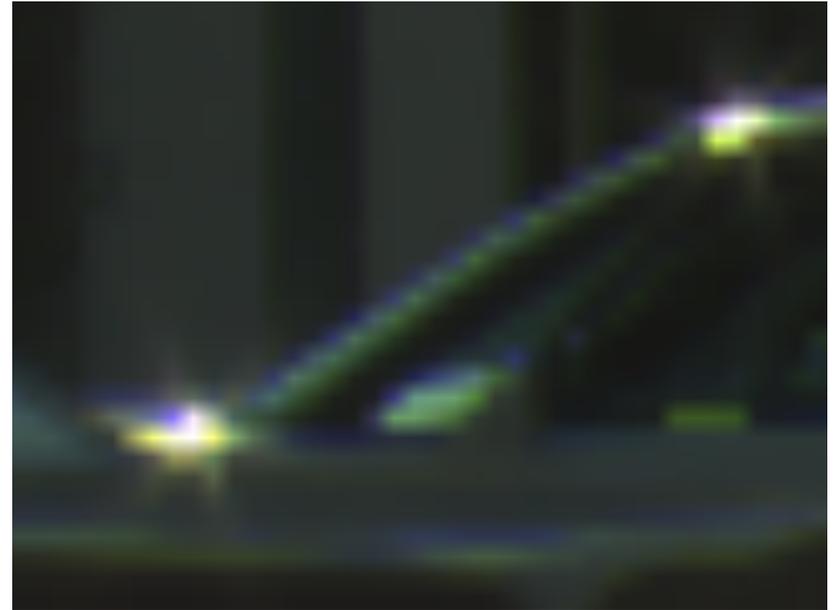


## (2) Image DR is often 3-5 Log units



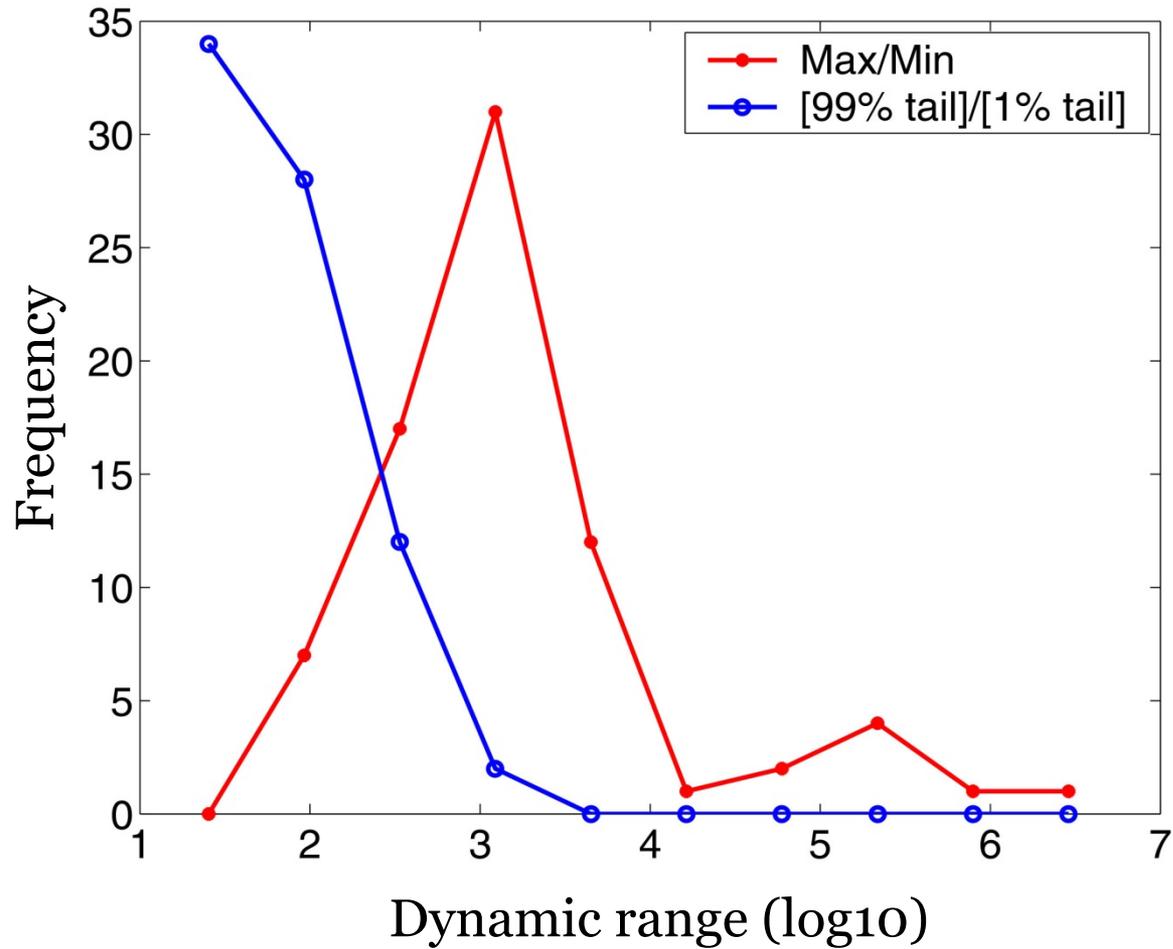
(3) The high range is often due to specular reflection or light

Original dynamic range = 6000:1



Effective dynamic range = [99% tail] / [1% tail]  
6000:1 reduced to 350:1

# Eliminating specular reflections and light sources reduces DR



# HDR image database (online)

<http://52.32.77.154/#browse~isetbio/resources.scenes.hdr>

Archiva

LOGIN REGISTER

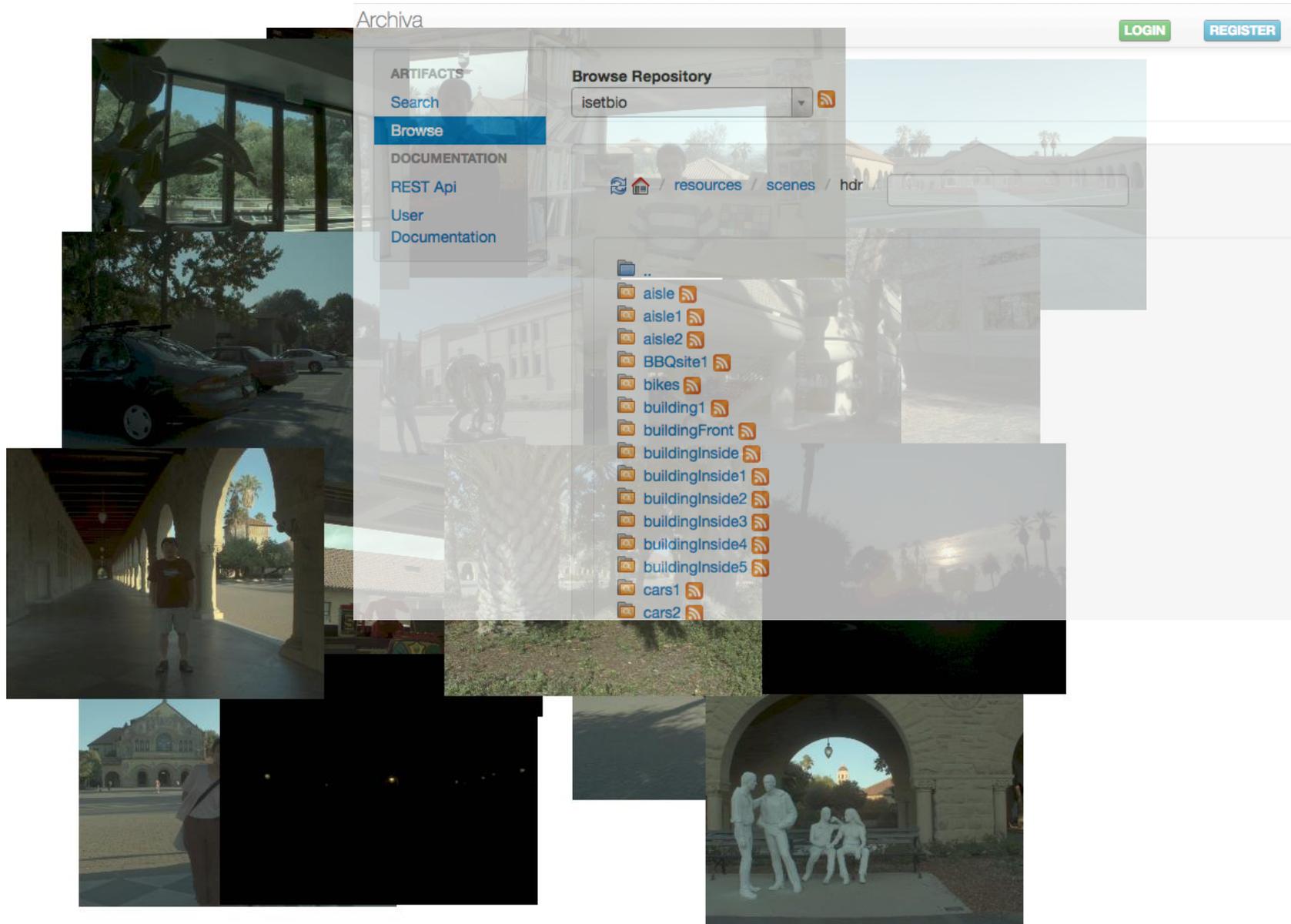
ARTIFACTS  
Search  
Browse  
DOCUMENTATION  
REST Api  
User  
Documentation

Browse Repository

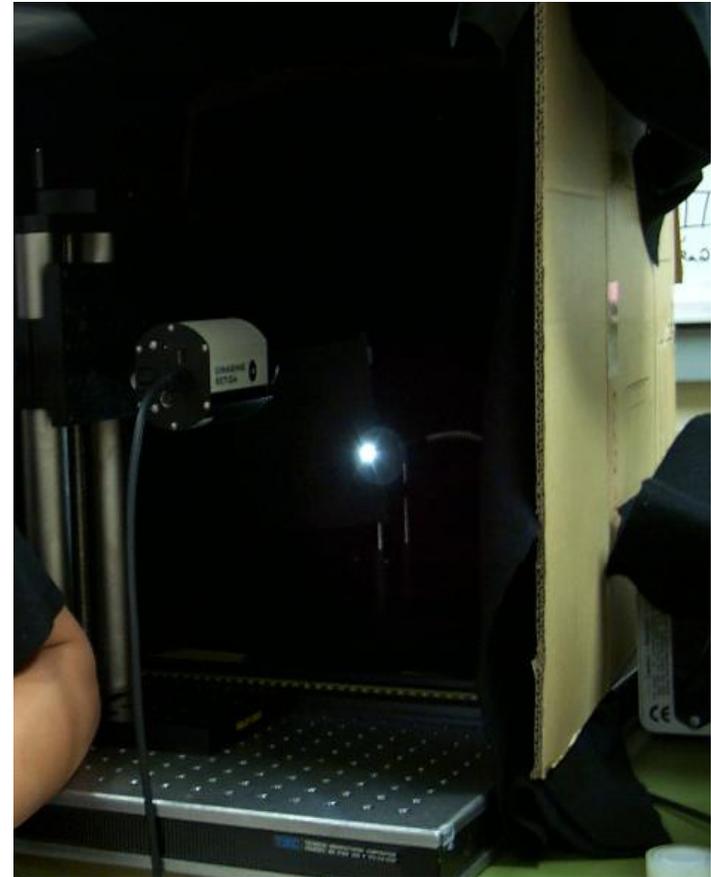
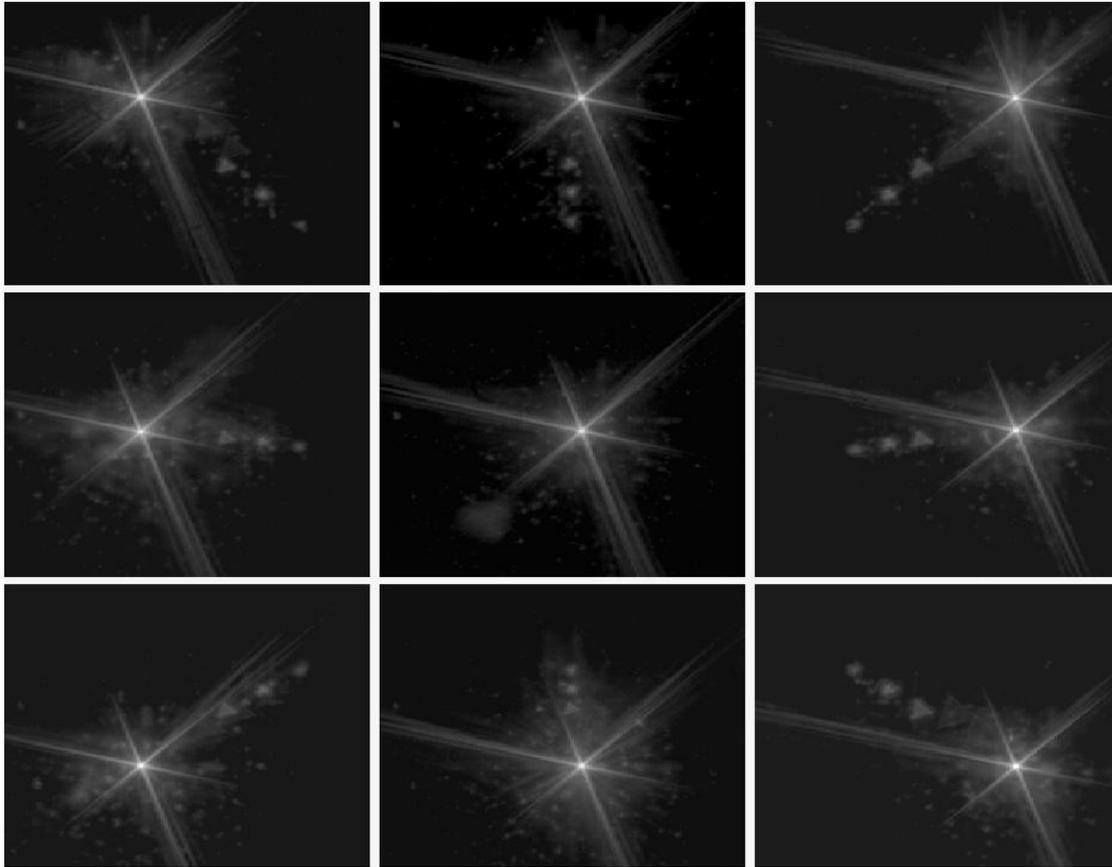
isetbio

resources / scenes / hdr

- ..
- aisle
- aisle1
- aisle2
- BBQsite1
- bikes
- building1
- buildingFront
- buildingInside
- buildingInside1
- buildingInside2
- buildingInside3
- buildingInside4
- buildingInside5
- cars1
- cars2

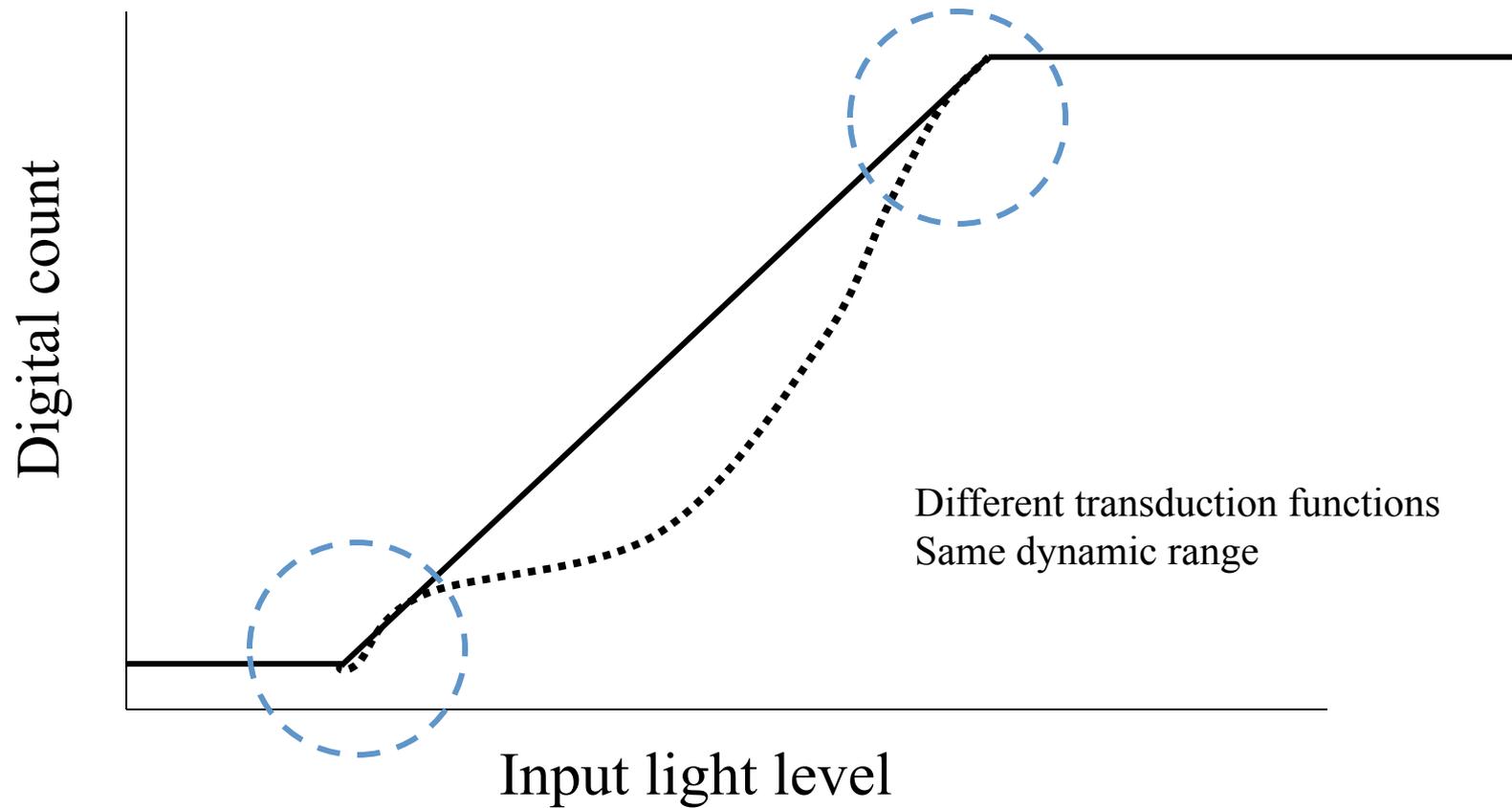


# Lens Calibration: Flare for HDR



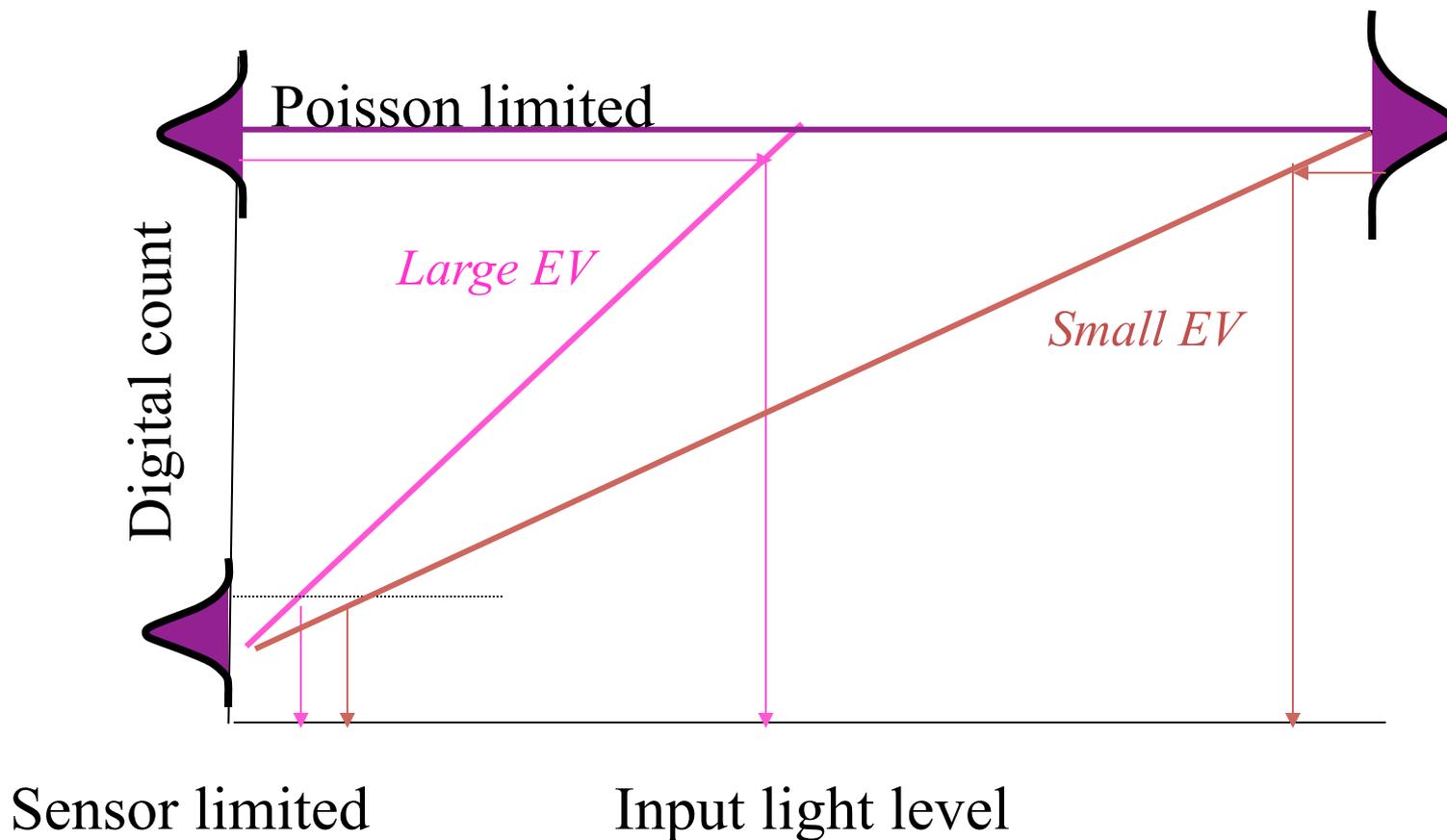
Shift-variant (but linear)

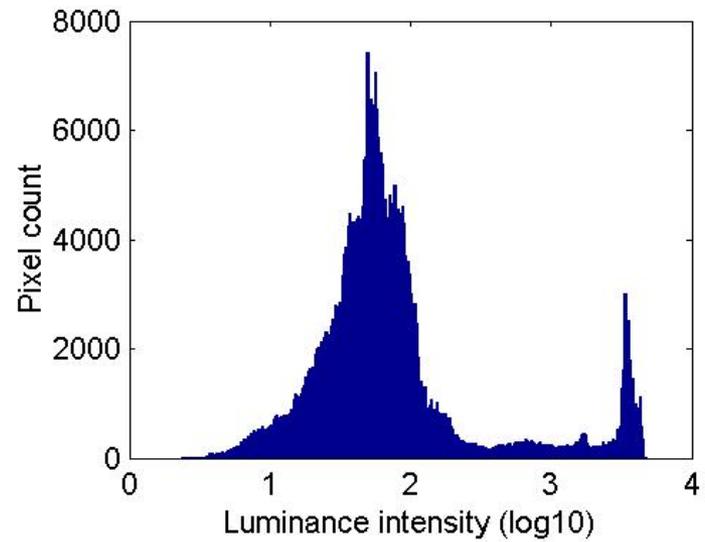
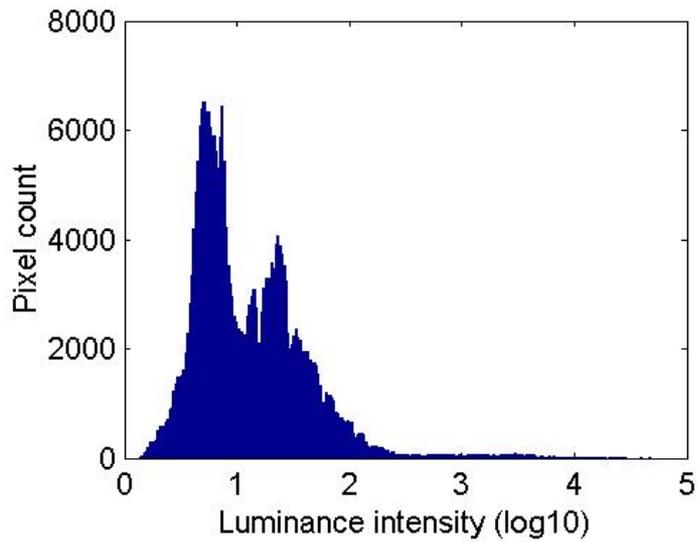
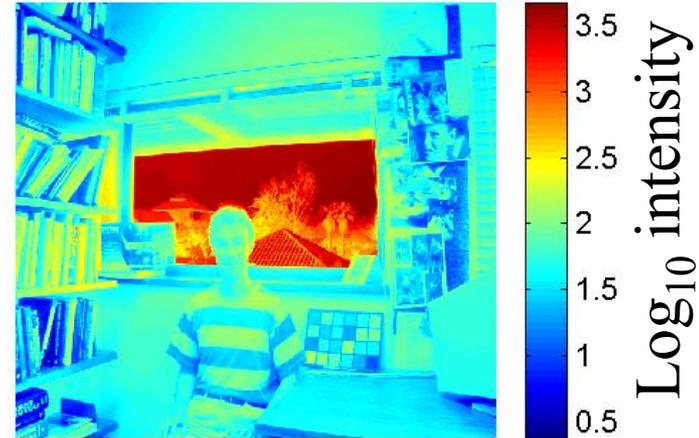
# Dynamic range Not the same as quantization



# Dynamic range and exposure value

Changing exposure value scales input-referred dark noise **and** input referred saturation. Hence, the dynamic range remains **roughly constant**





# High dynamic range image capture

- There are software and multi-capture approaches
- We attend to hardware ideas
- Limitation is pixel well-capacity







# 1<sup>st</sup> Generation Implementation (D. Yang et al., IEEE JSSC, 1999)



- *Imager: 640 x 512*
- *Pixel: 10.5 micron*
- *Technology: 0.35 micron*
- *ADC shared x 4*
- *Control signals FPGA*
- *Fill factor ~ 29%*
- *QE ~10%*
- *Really cool, though*

# Multicapture HDR Illustration



Charge



4T

# Pixim



Feng\_Office-hdrs

Name: Feng\_Office-hdrs  
(Row,Col): 506 by 759  
Hgt,Wdth (139.98, 209.97) mm  
Sample: 276.64 um  
Deg/samp: 0.01  
Wave: 400:10:700 nm  
DR: 81.23 dB (max 2053 cd/m2)



Adjust scene size

X 1

Interp

Luminance

100.0

cd/m2

FOV (width)

10.00

deg

Distance

1.2

m

1

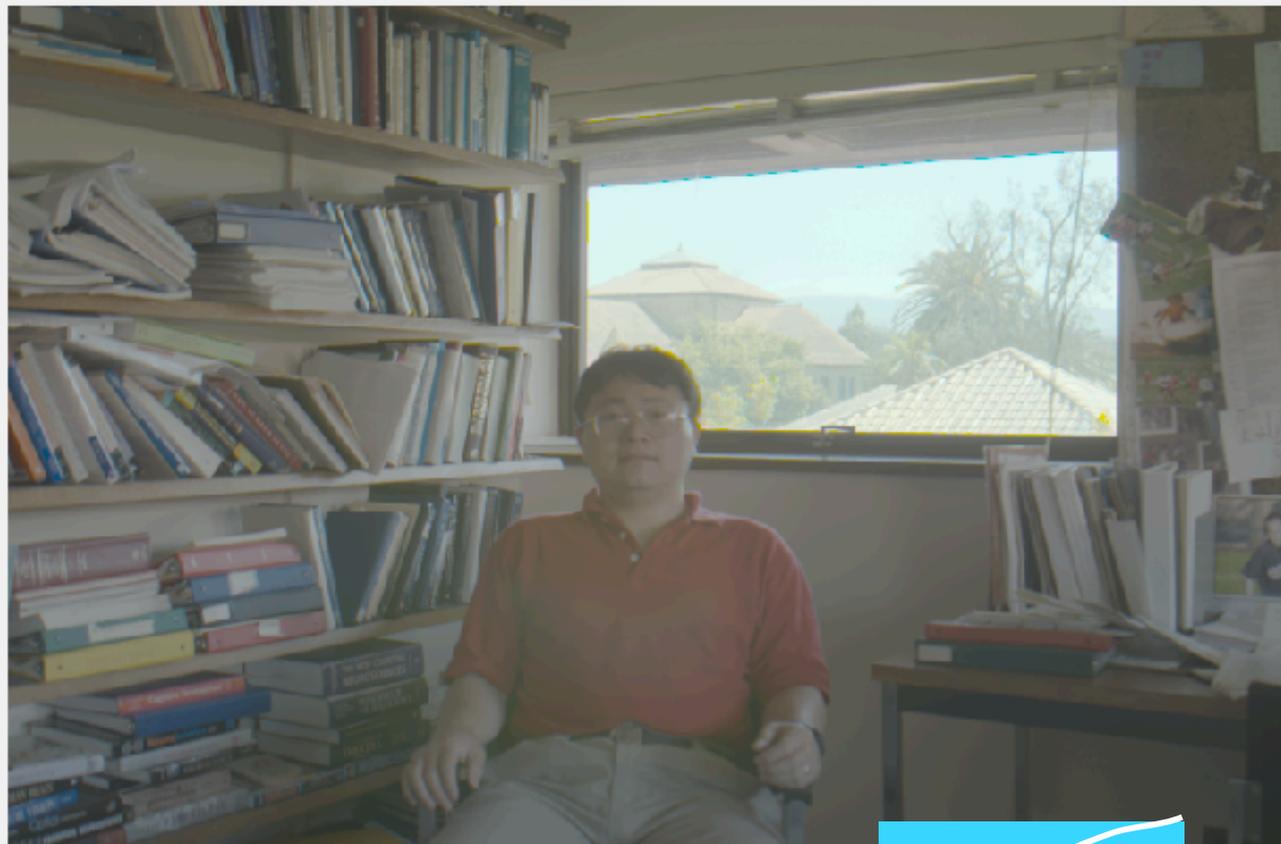
Standard RGB

Gamma

Display

Feng\_Office-hdrs

Name: Feng\_Office-hdrs  
(Row,Col): 506 by 759  
Hgt,Wdth (139.98, 209.97) mm  
Sample: 276.64 um  
Deg/samp: 0.01  
Wave: 400:10:700 nm  
DR: 81.23 dB (max 2053 cd/m2)



Adjust scene size

X 1

Interp

Luminance

100.0

cd/m2

FOV (width)

10.00

deg

Distance

1.2

m

.3

Gamma

Standard RGB

Display

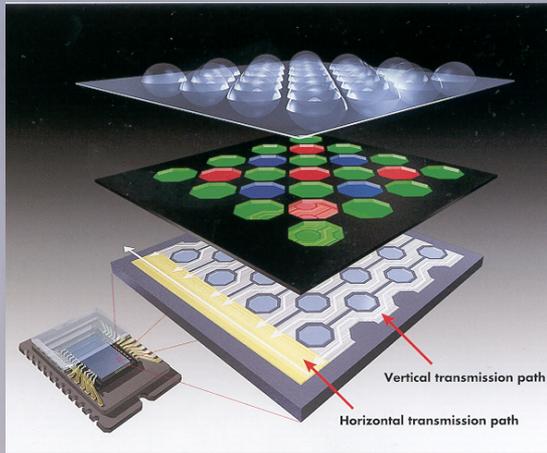
 $I^\gamma$

# HDR range compression code from MIT

[Li, Sharan, and Adelson](#)

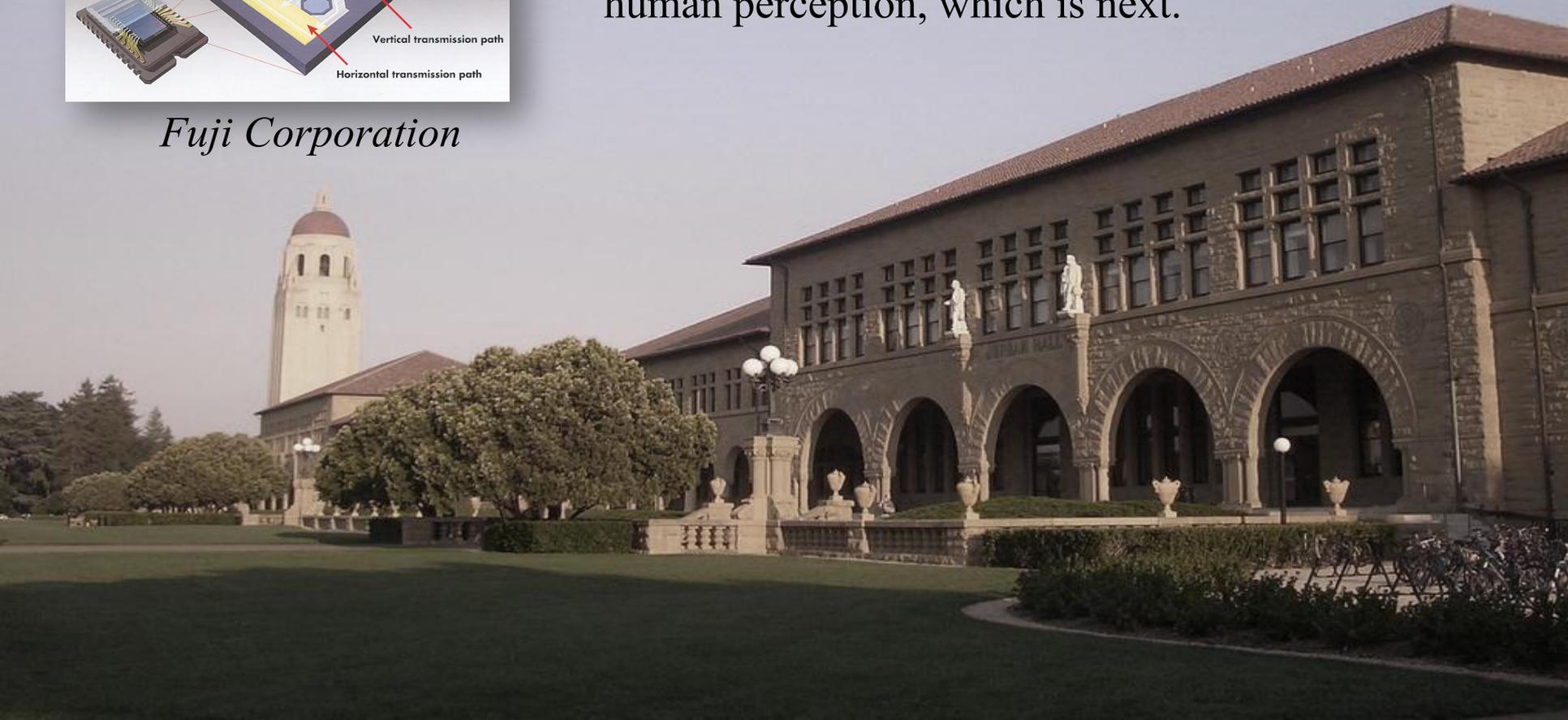


# Novel camera architectures



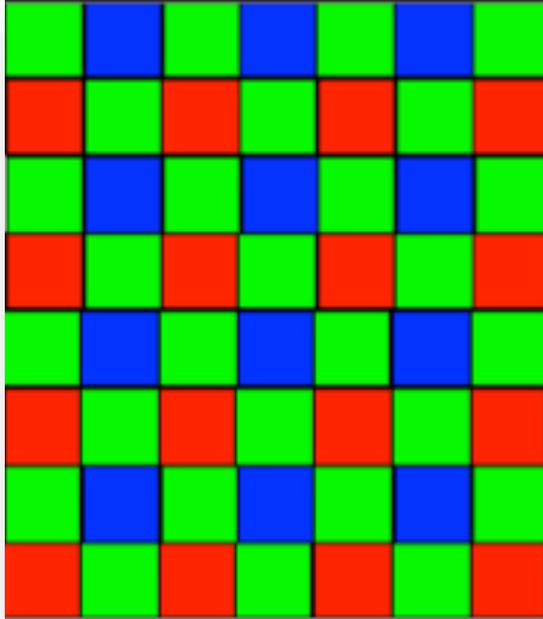
*Fuji Corporation*

This is an overview. When we get to the image processing lectures in 2.5 weeks, I will explain more about how the data are processed and evaluated. Before that we need to review some human perception, which is next.

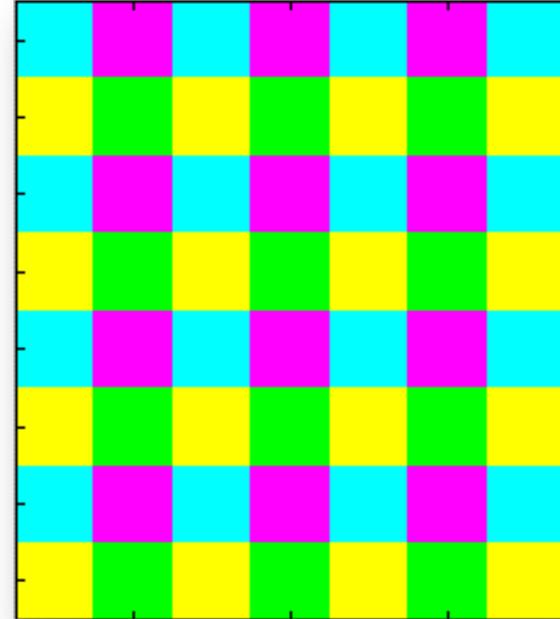


# Camera CFA architectures

- Bayer array RGB
- Most common
- Green double the sampling rate
- Requires filling in missing pixel values – (demosaicking)

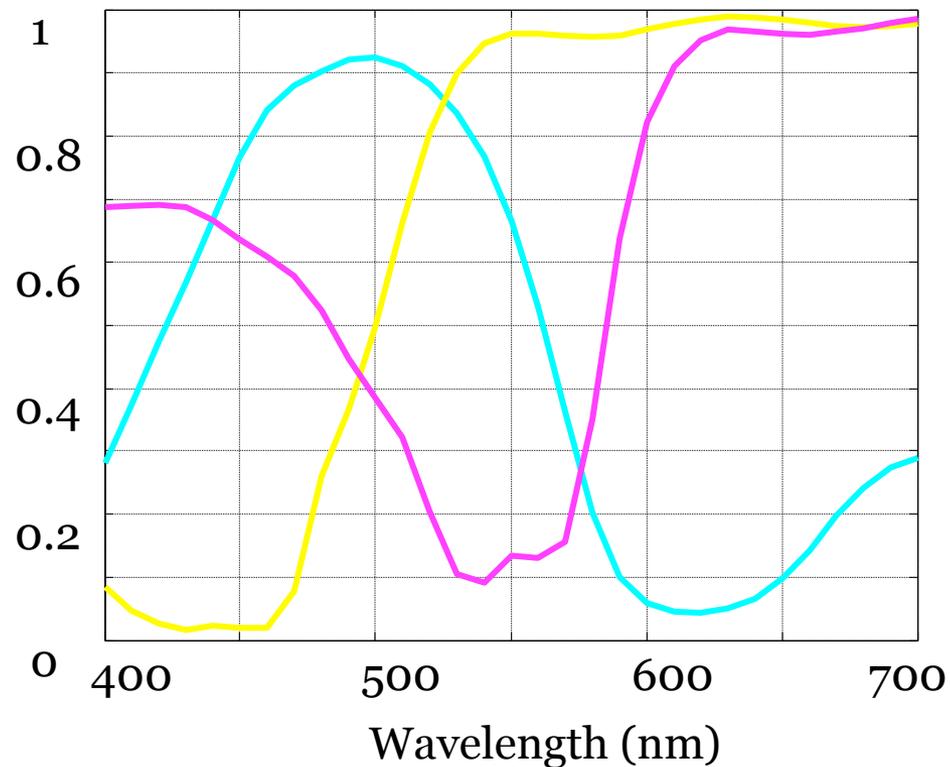
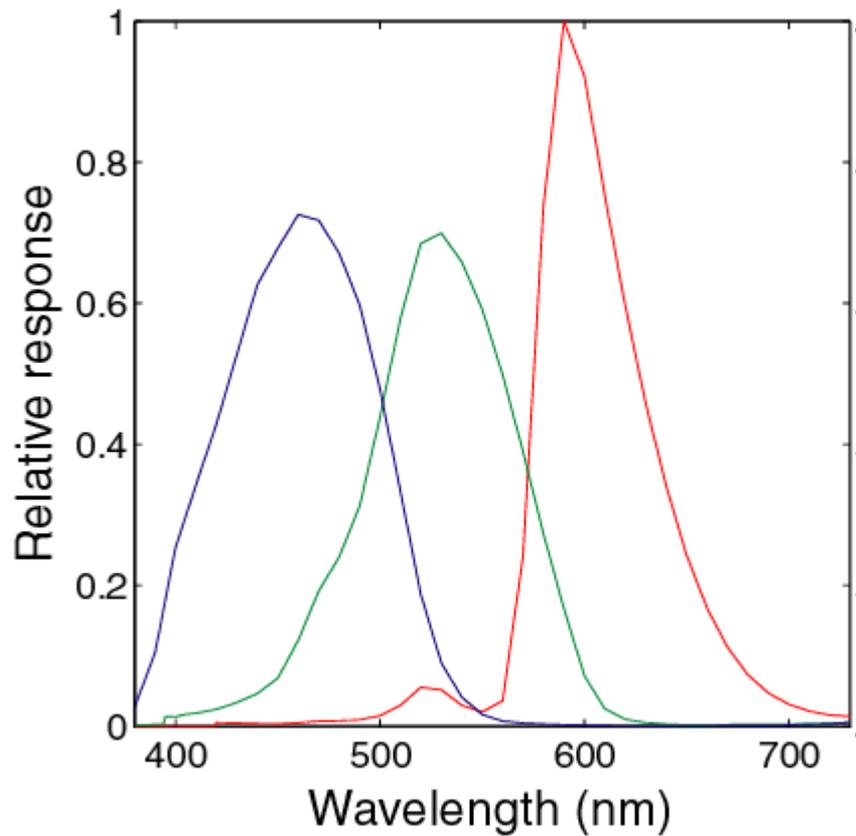


- CMYG – video cameras
- Fast demosaicking
- Broad filters, more photons
- Poor noise properties



# Example sensor responsivities differ

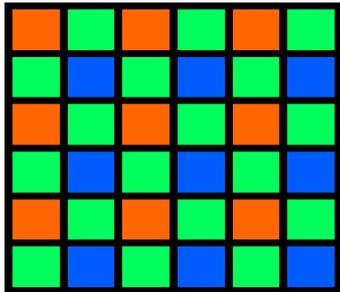
Nikon D1 camera



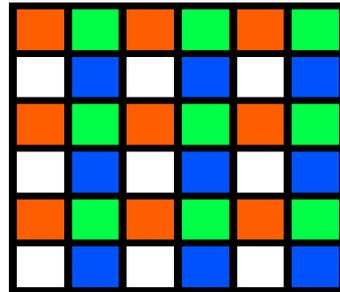
*(Xiao and Wandell, personal comm.)*

# Opportunity and challenge

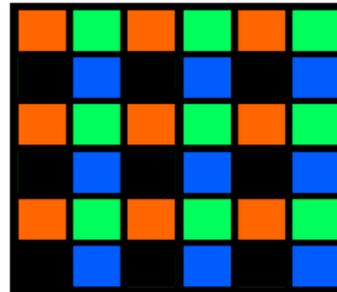
- High density (small size) and excellent electrical properties of modern pixels enable new sensors with new applications
- **Challenge:** design and deliver image processing pipelines that exploit the spatial spectral statistics of the target scenes, properly balancing noise



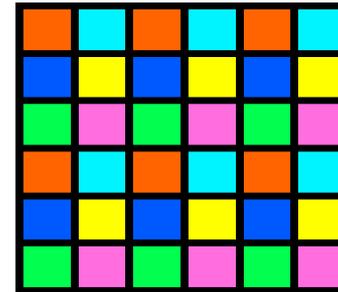
**Bayer**



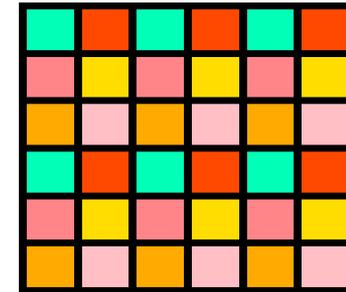
**RGBW**  
low-light sensitivity  
dynamic range



**RGBX**  
infrared  
light field



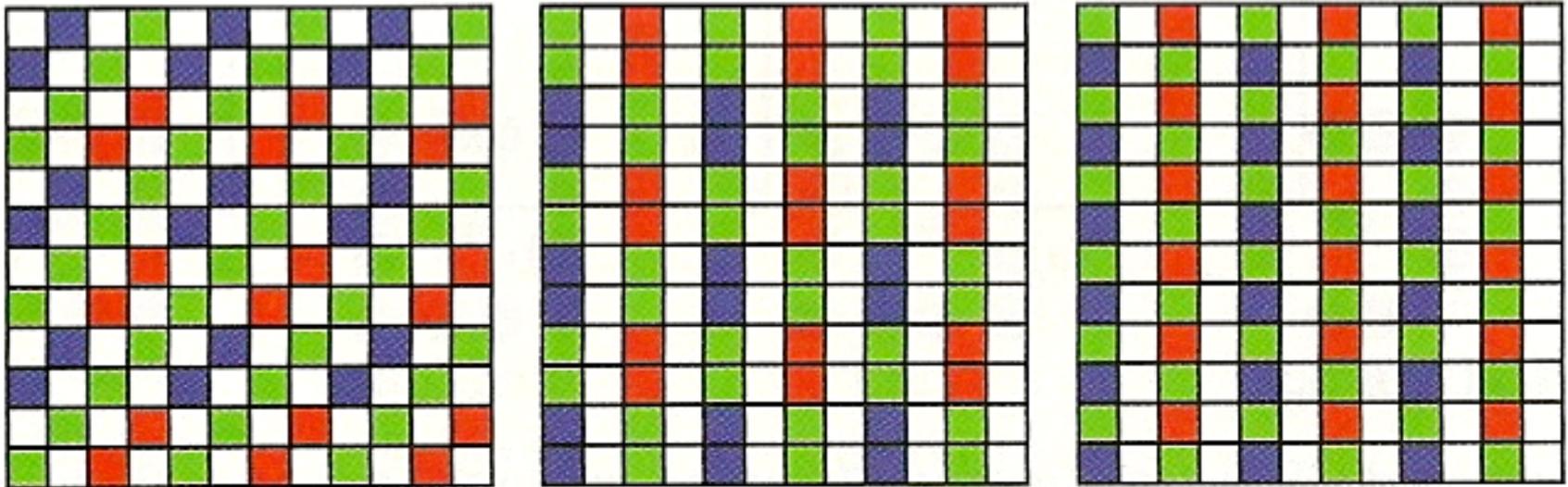
**RGBCMY**  
multispectral



**Medical**  
specialized  
application

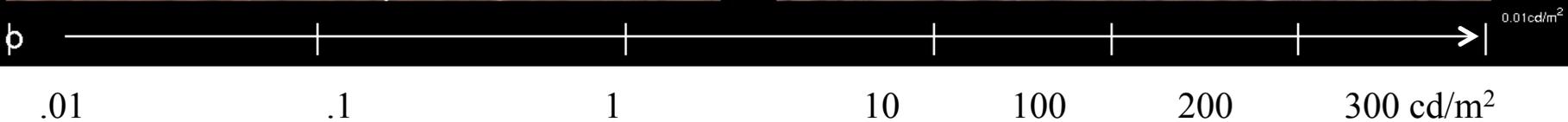
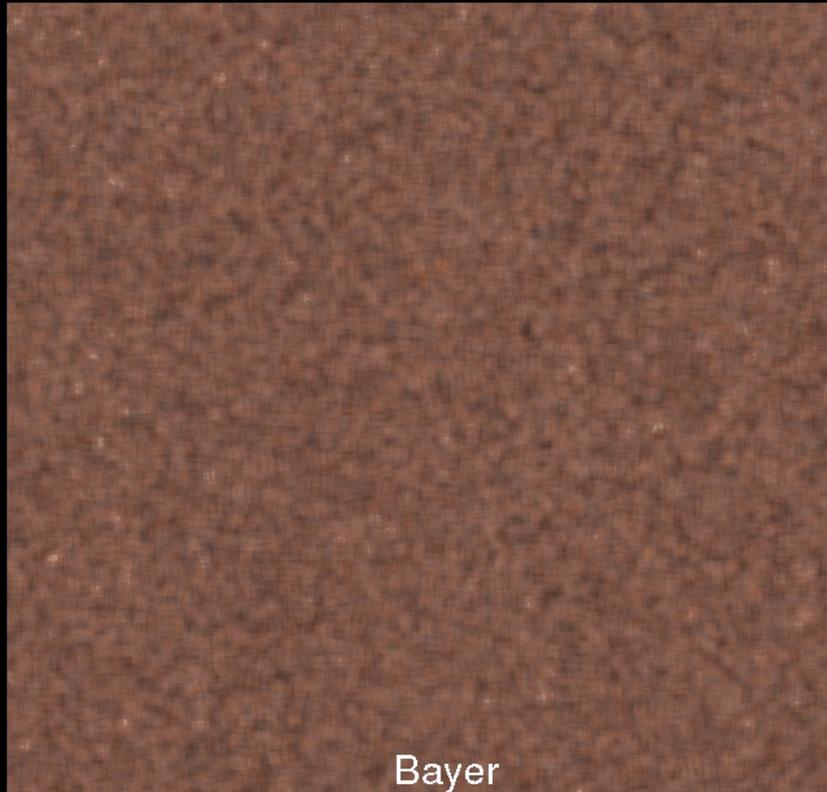
# Arrays with white pixels

Under low illumination conditions, the white pixel still gathers some information.  
The rendered scene, however, will not have good color reproduction



# RGBW compared to Bayer

RGBW: better in low light & same in high light



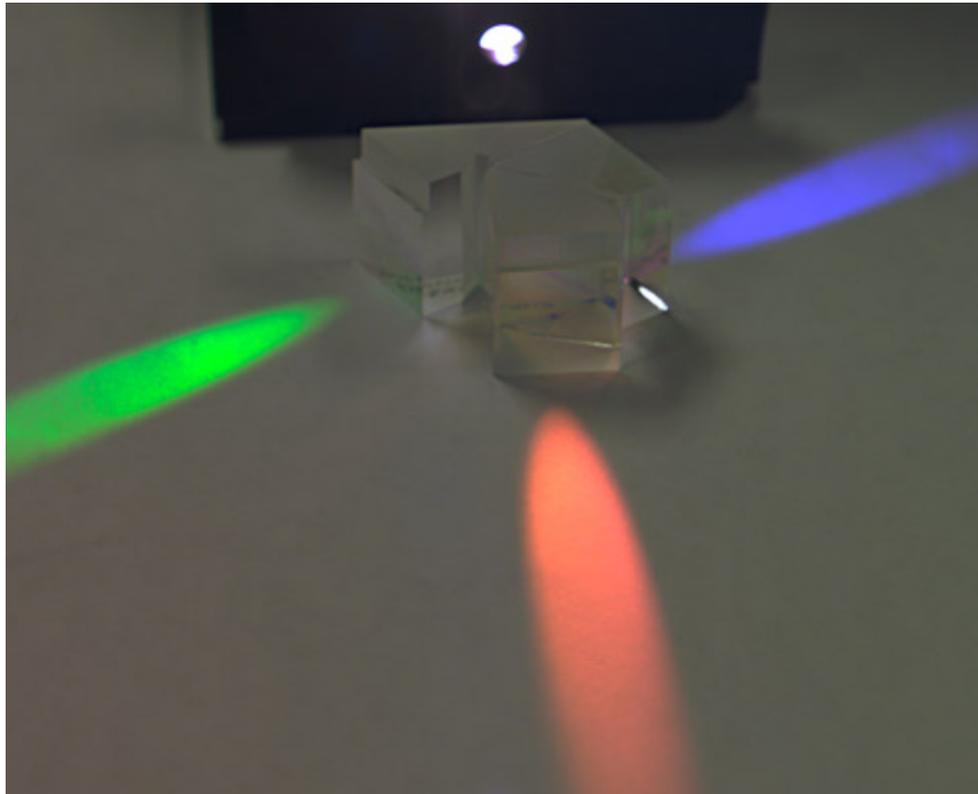
Scene luminance (cd/m<sup>2</sup>)

# Camera color architectures: 3-Sensor

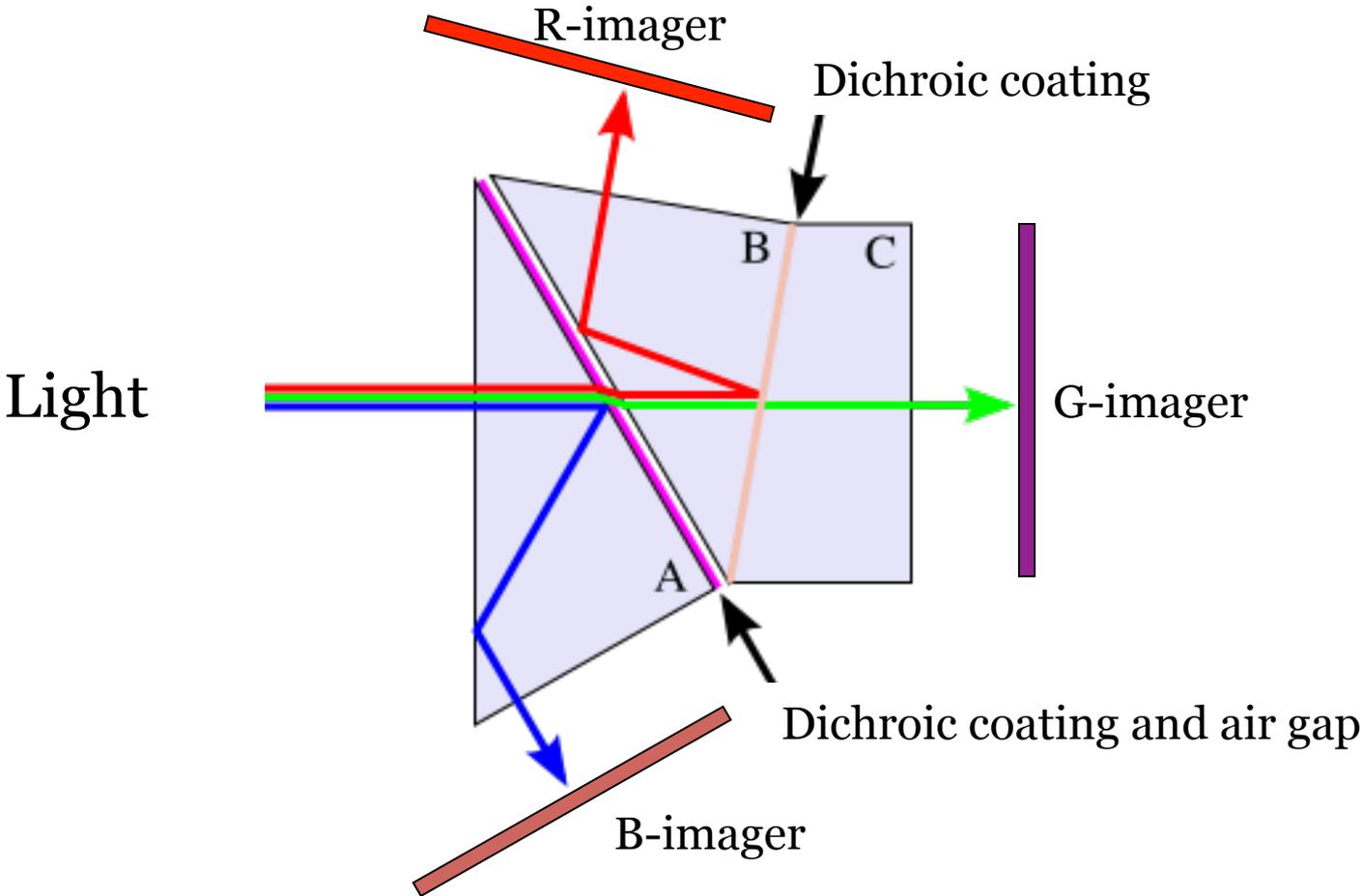
## Prismatic optics

No demosaicking

Three (smaller) sensors and optical alignment



# Philips total internal reflection dichroic prism



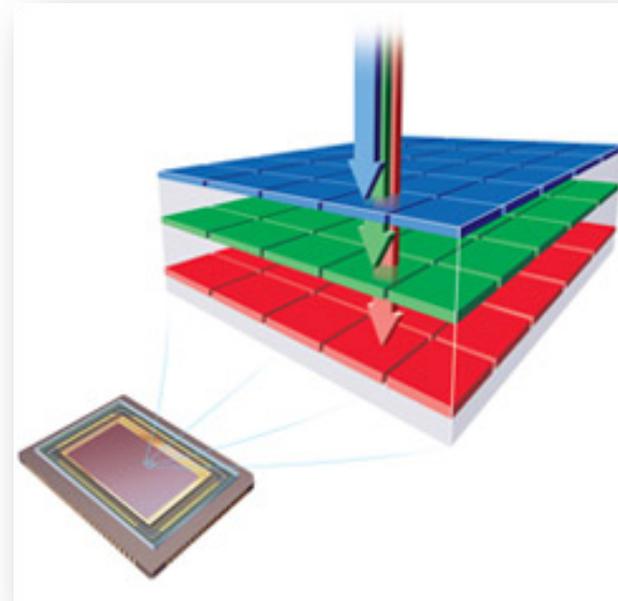
# Foveon and Sigma

<http://www.foveon.com/article.php?a=67>

s\_sensorStackedPixel.m



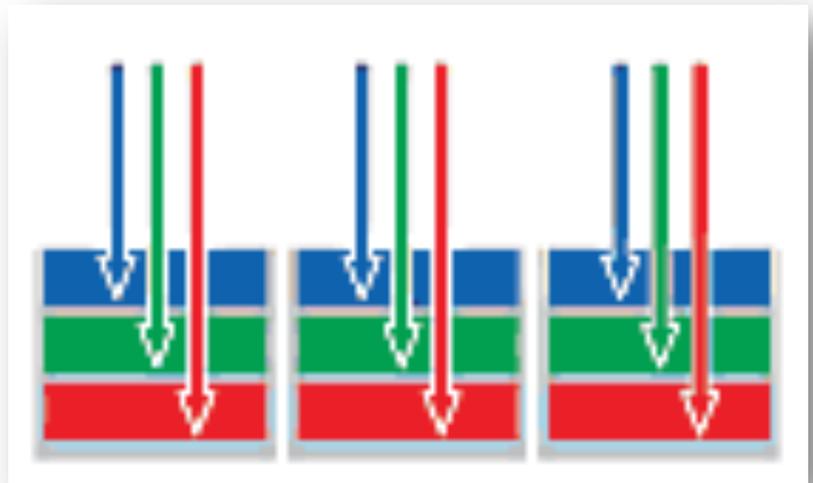
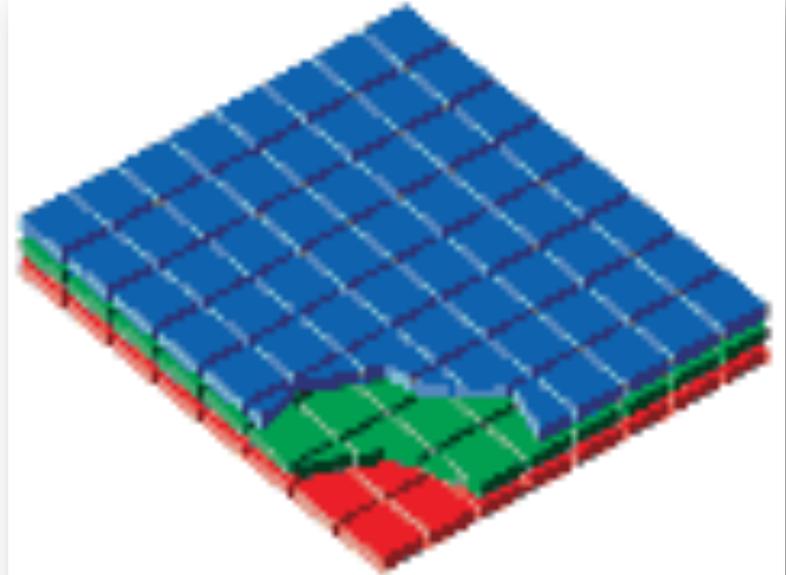
The Sigma SD9 was the first digital camera to use a full-color multi-layer sensor technology.



The sensor was called the Foveon X3.

# Wavelengths penetrate to different depths

Long-wavelength photons penetrate deeper than short. The spectral response of electrons at the surface differs from electrons deeper in the material



# Calculating absorption likelihoods

Probability of absorption in an infinitesimal slice

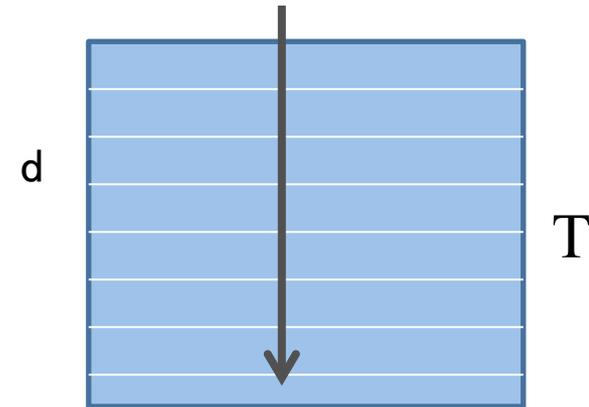
$$p(\lambda, \delta) = a(\lambda)\delta$$

Suppose that we calculate for a thickness,  $T$ , of  $N$  infinitesimal slices, each of thickness  $T/N = d$  the likelihood of **not** being absorbed up to that last slice

$$\lim_{N \rightarrow \infty} \left(1 - a(\lambda) \frac{T}{N}\right)^N = e^{-a(\lambda)T}$$

Probability of **being** absorbed in the next infinitesimal slice

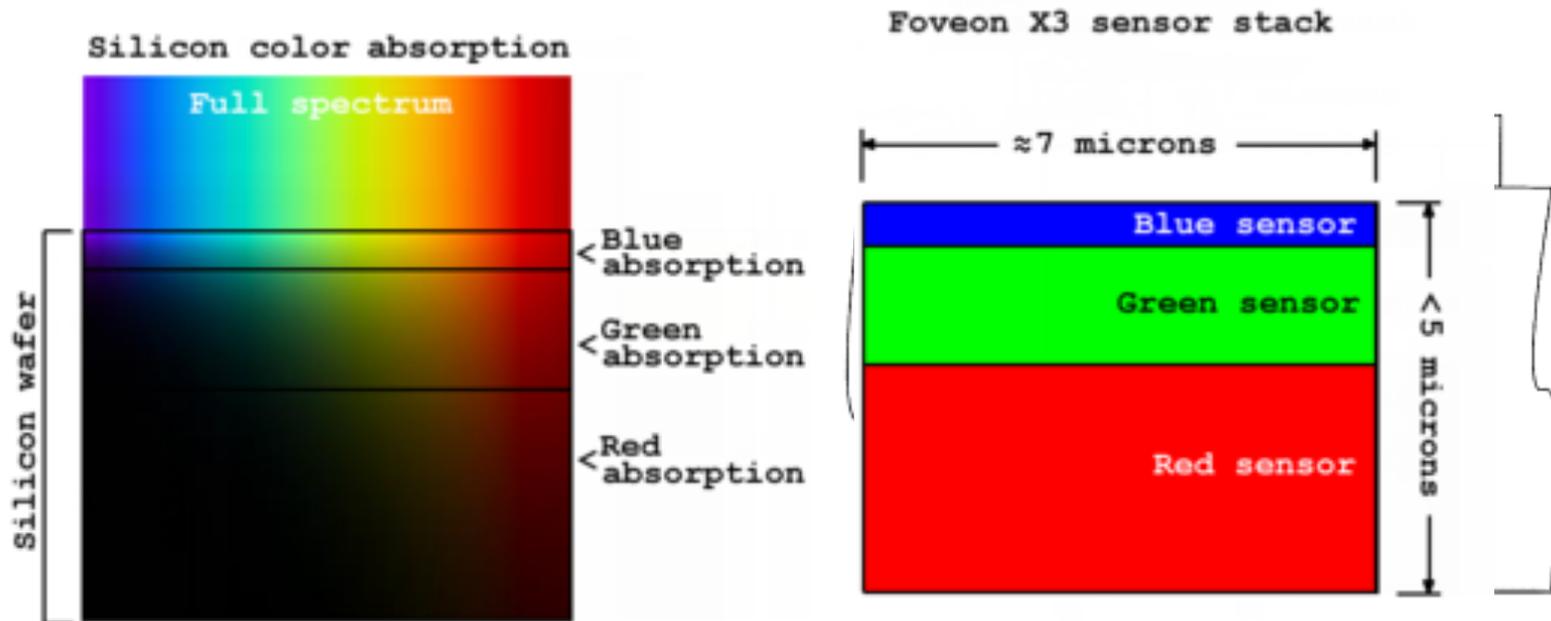
$$p(\lambda, \delta)e^{-a(\lambda)T} \sim a(\lambda)e^{-a(\lambda)T}$$



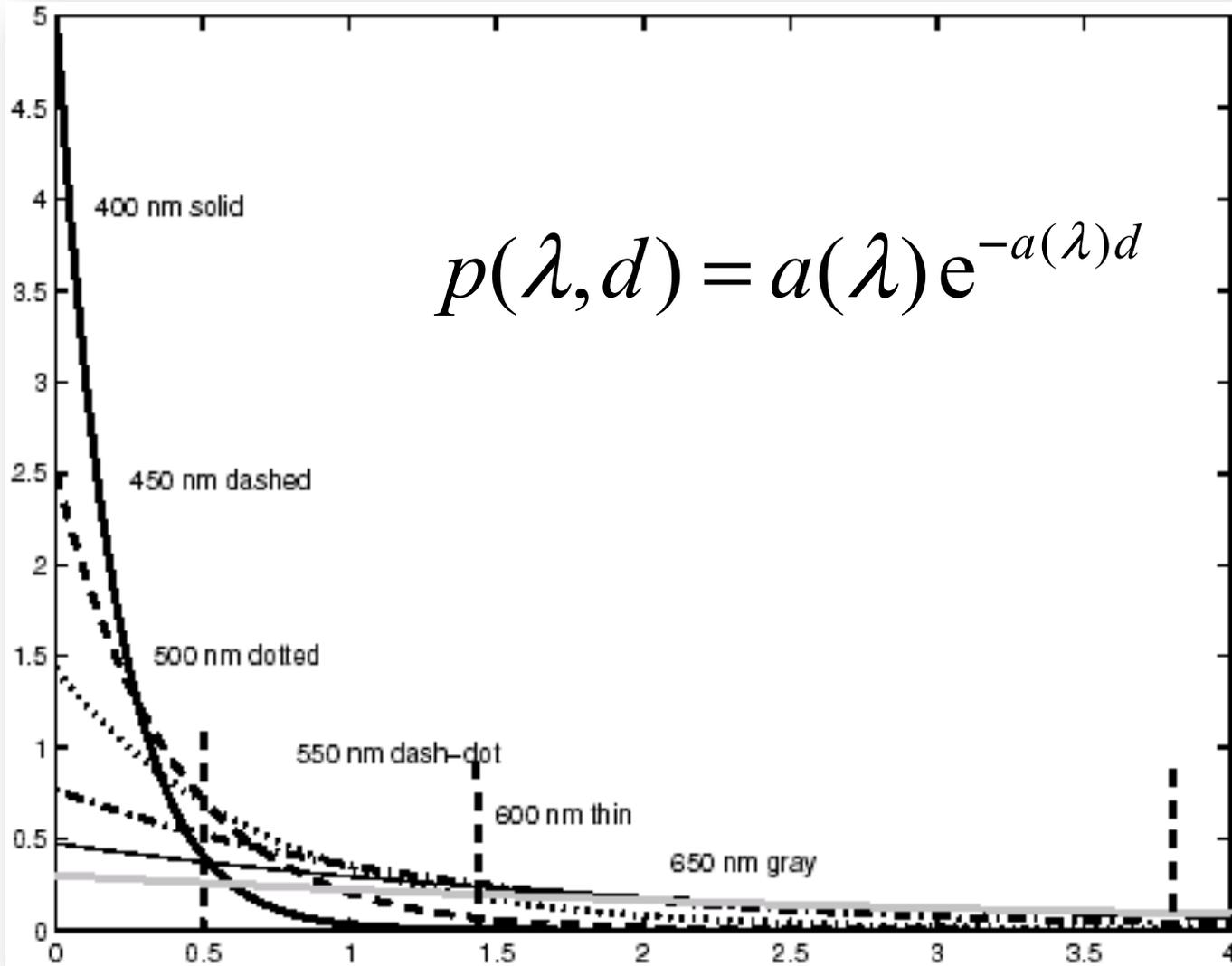
# Photon penetration into silicon

$$p(\lambda, d) = a(\lambda) e^{-a(\lambda)d}$$

*Each photon goes somewhere*



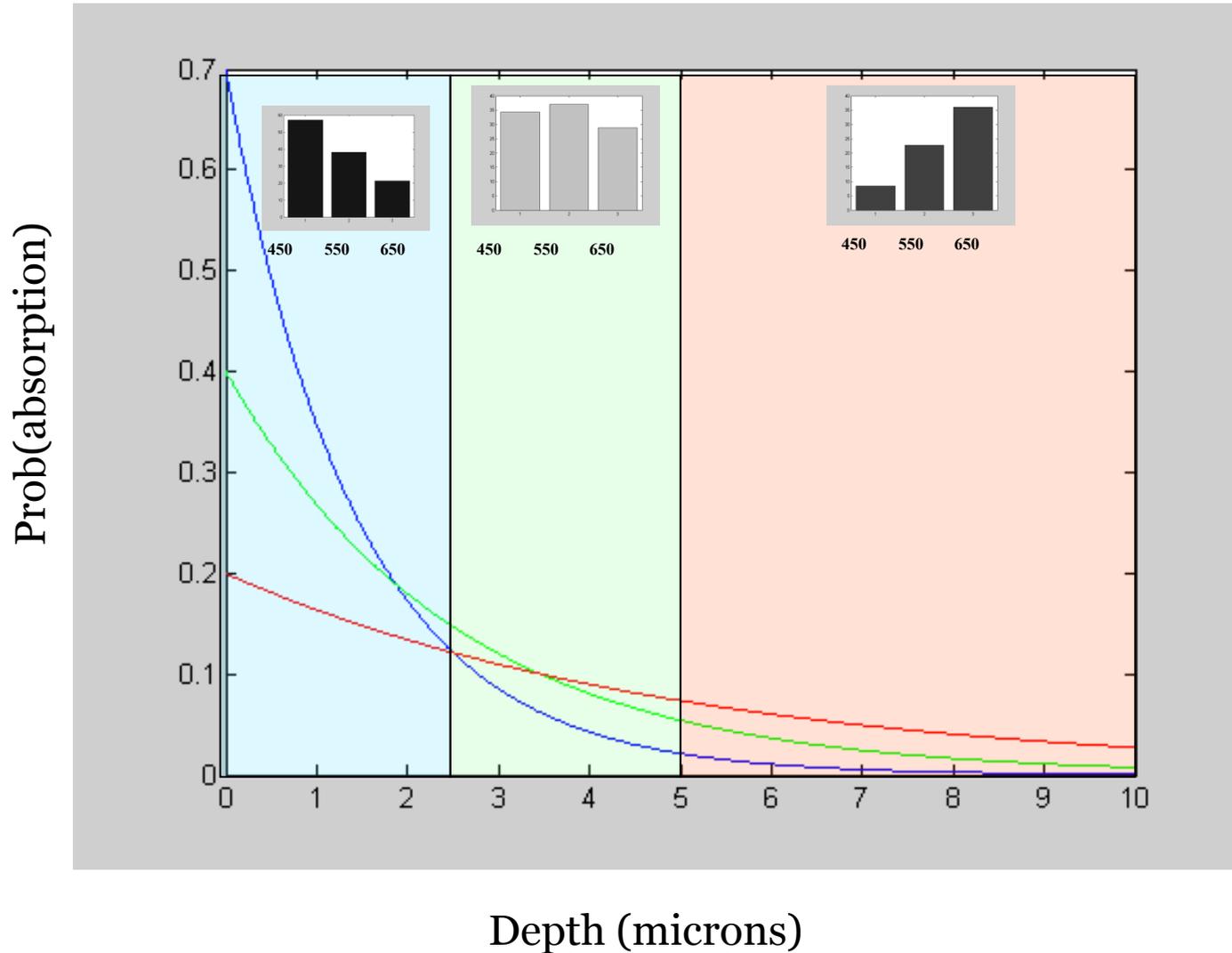
Absorption per unit depth



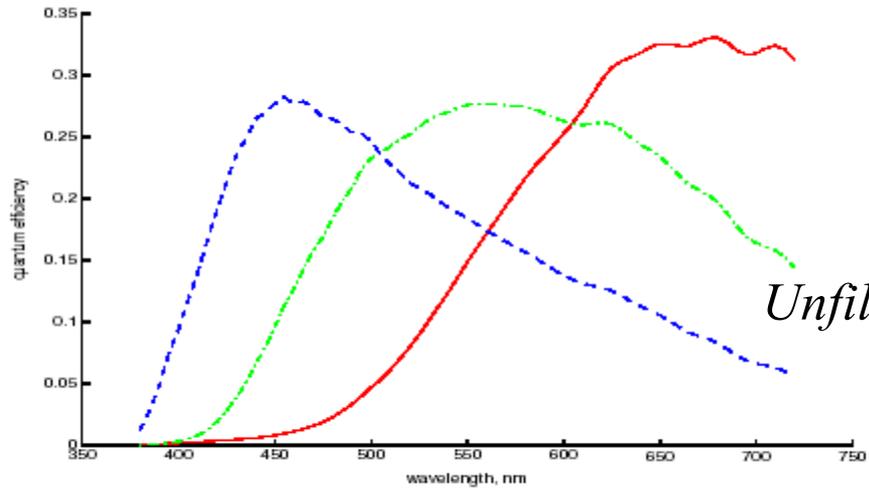
$$p(\lambda, d) = a(\lambda) e^{-a(\lambda)d}$$

Depth (microns)

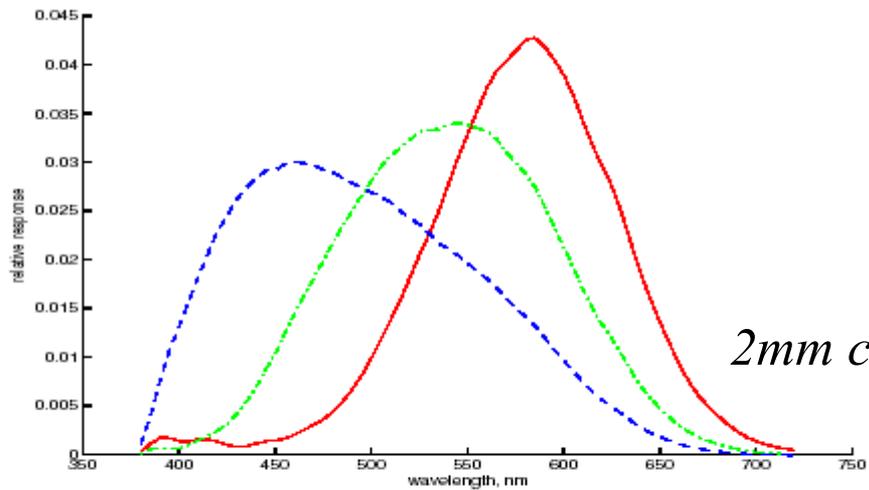
# Foveon X3 Pixel (Triple-Well)



# Quantum efficiencies of the three wells (Foveon)

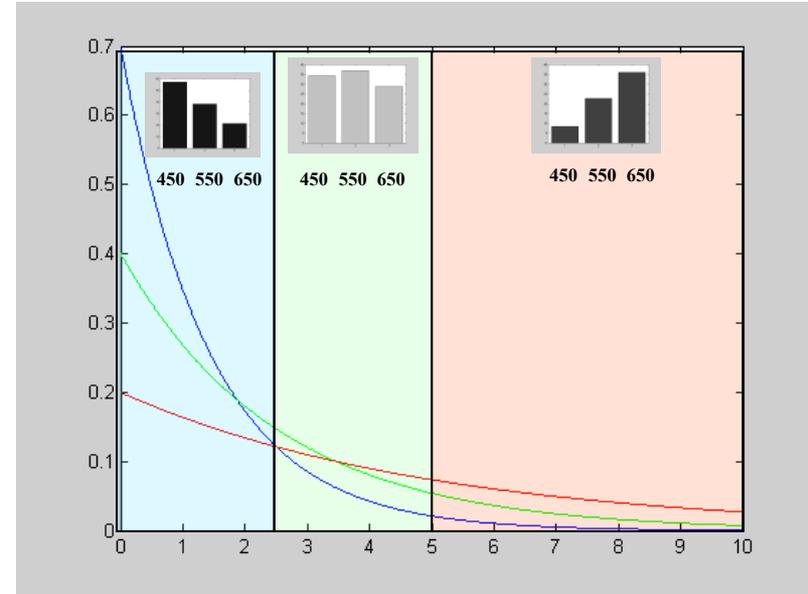


*Unfiltered*



*2mm cm500 IR filter*

**Prob(absorption)**



**Depth (microns)**

# Having more photosites makes the luminance image sharper

## Foveon marketing

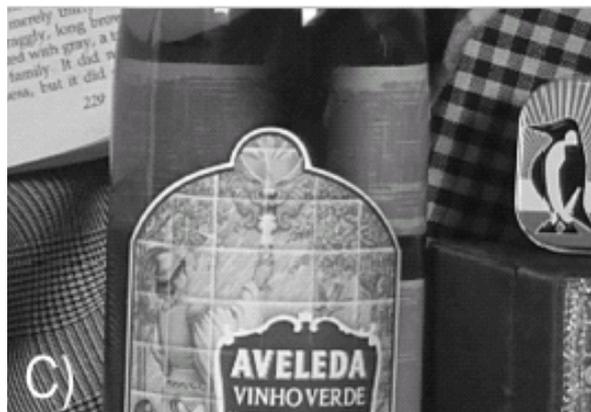
Is slightly higher resolution what people really wanted?



*Bayer*



*Bayer + blur*



*Foveon X3*

# New high-end camera designs: Light L16



# Choose 10 of 16

Multiple focal lengths, field of view, depth of field

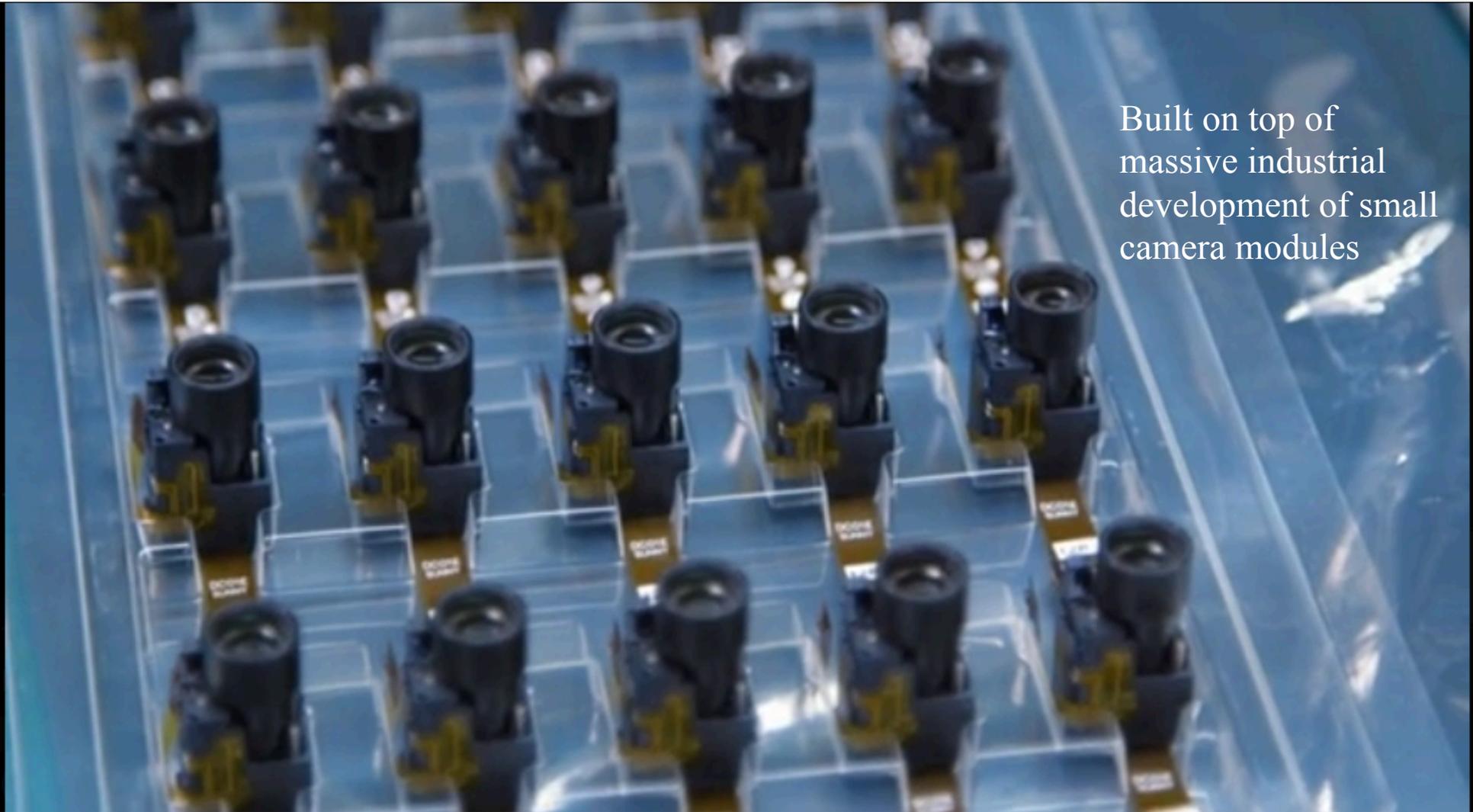
Computational imaging

Potential for multiple exposure durations



# Taking advantage of camera module scaling

Built on top of  
massive industrial  
development of small  
camera modules



Talk at SCIEN Oct.  
15<sup>th</sup>, 2015 by the CEO



## The Light L16 Camera

\$1699

The L16 is a compact camera that uses multiple lens systems to shoot photos at the same time, then computationally fuses them into a DSLR-quality image.

The Light L16 is sold out until 2017.

Join our email list for updates and to get notified when we begin taking new orders.



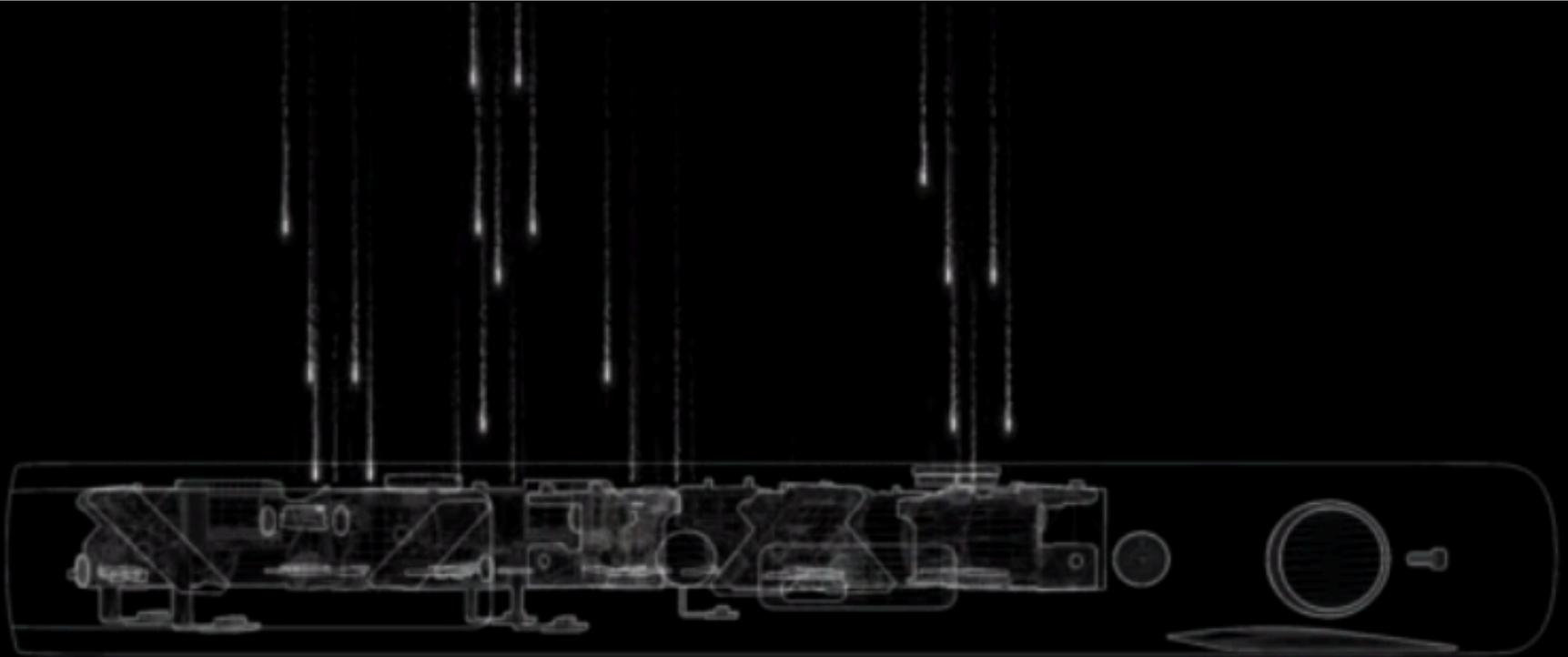
Enter your email address

Join our list

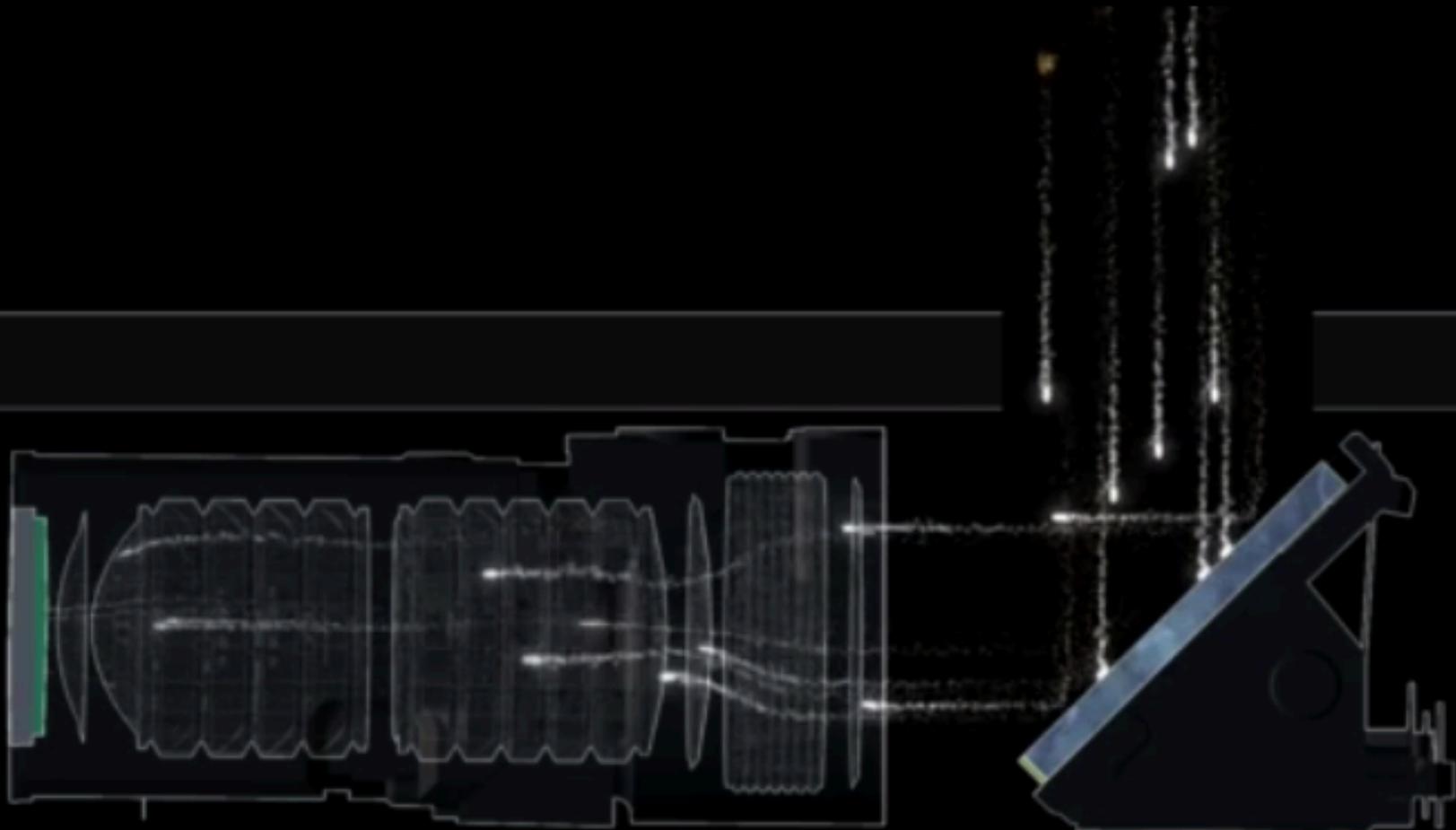
# Innovative design using movable mirrors



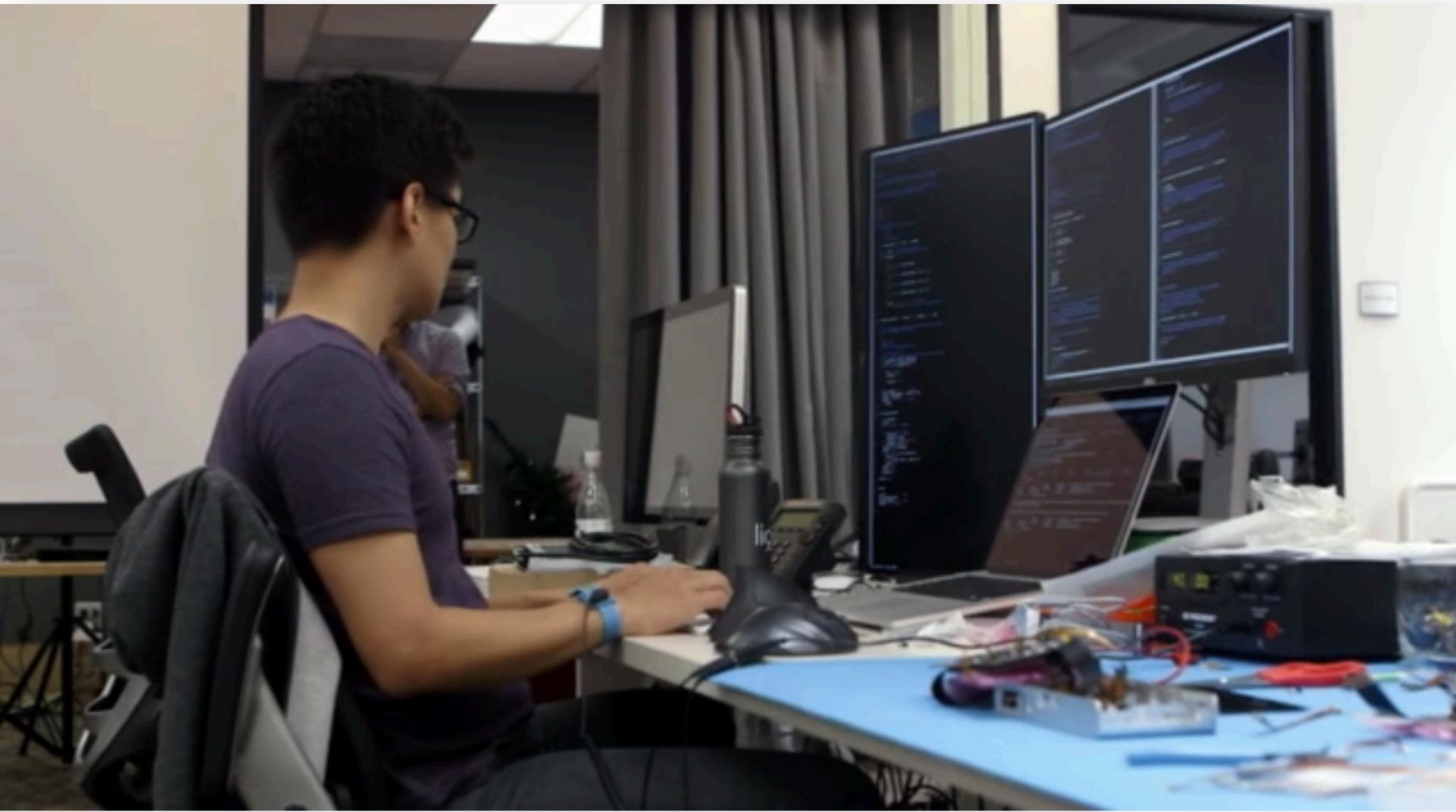
# Innovative design using movable mirrors



# Innovative design using movable mirrors



Put together by computational imaging ideas

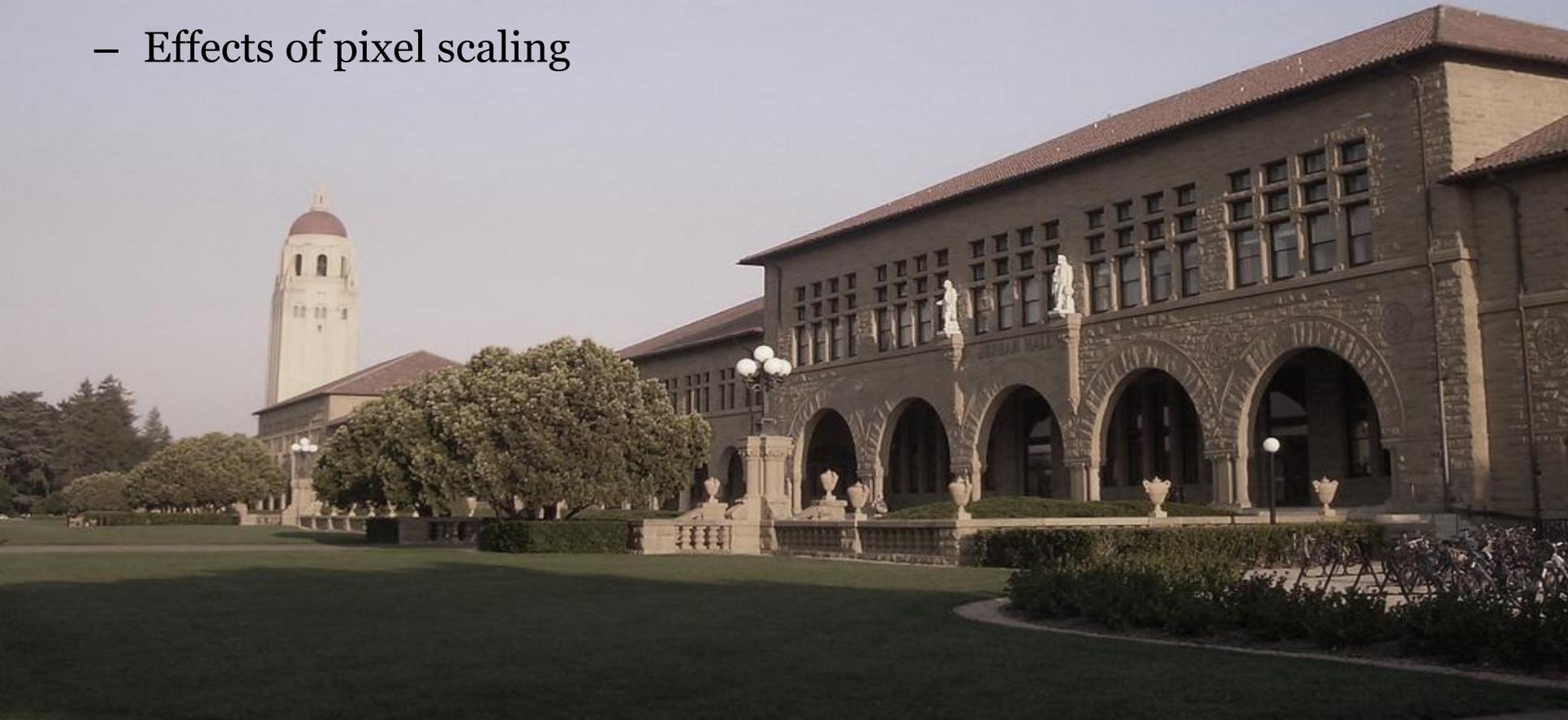


Is higher resolution and controlled properties of depth of field and bokeh<sup>1</sup> features in a cell phone form factor what people really want?

1. Bokeh: The visual quality of the out-of-focus areas of a photographic image, especially as rendered by a particular lens (pronounced both ways, in practice).

# Pixel optics

- Light inside imagers
  - # photons at the pixel is finite
  - Light collecting and guiding in pixels
  - Effects of pixel scaling



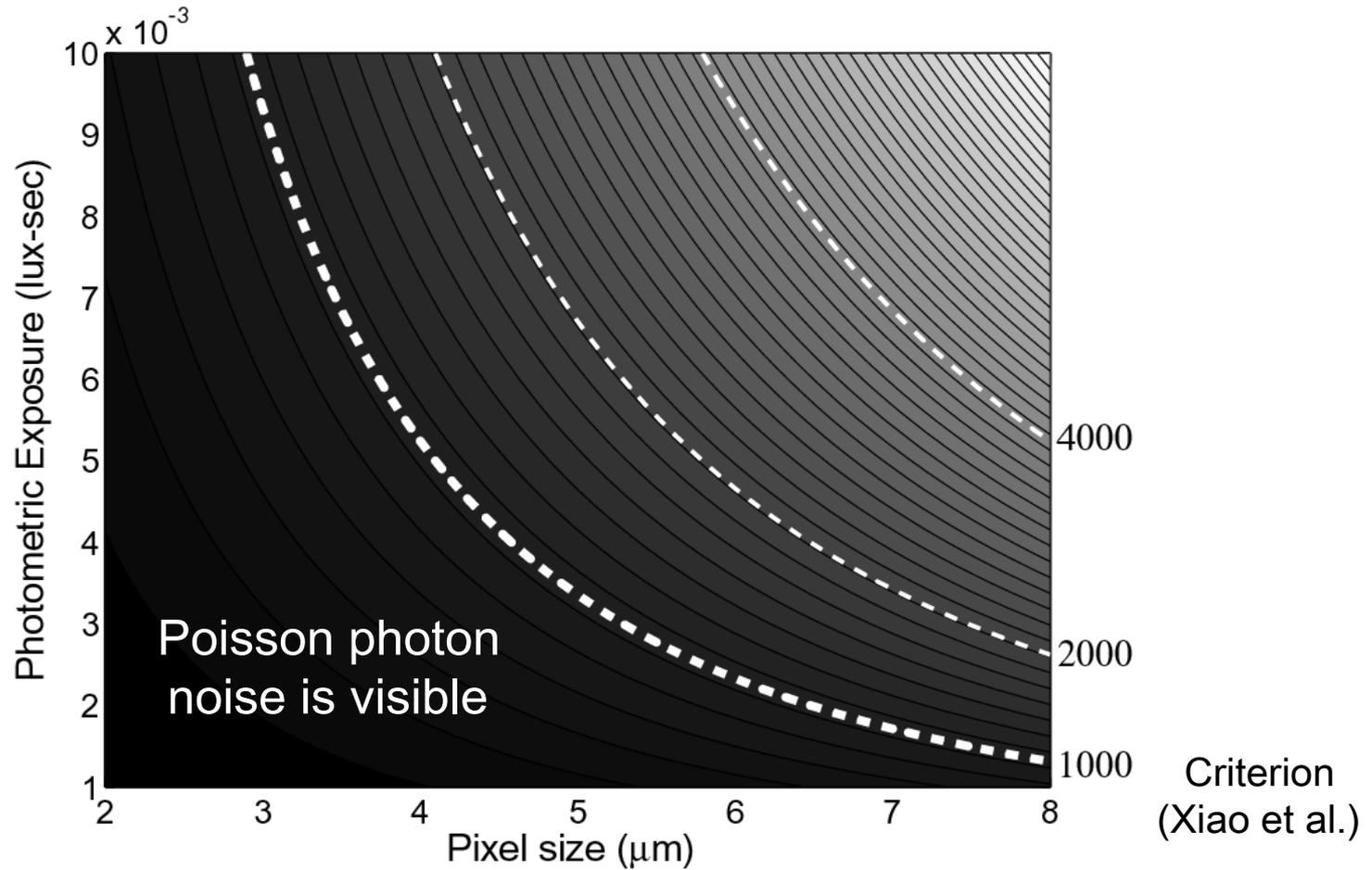
# 1,000 photon criterion (Xiao et al.)

3% contrast-threshold for spatially uniform photon noise  
Photon noise becomes visible at 1,000 photons  
( $\text{SNR} = 1000/\sqrt{1000} = 33:1$ )

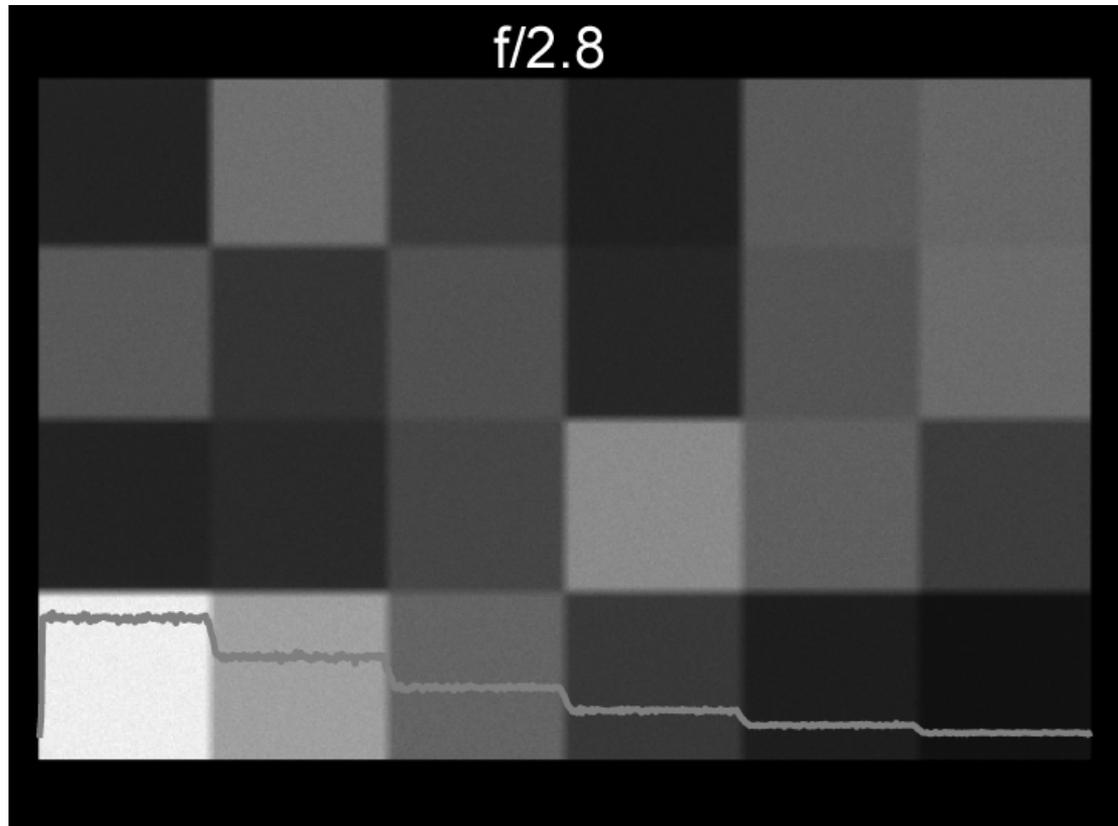


Figure 3: A pair of stimuli was displayed side by side: one was a uniform disk and the other one with noise superimposed.

# Photon noise: Photons per pixel

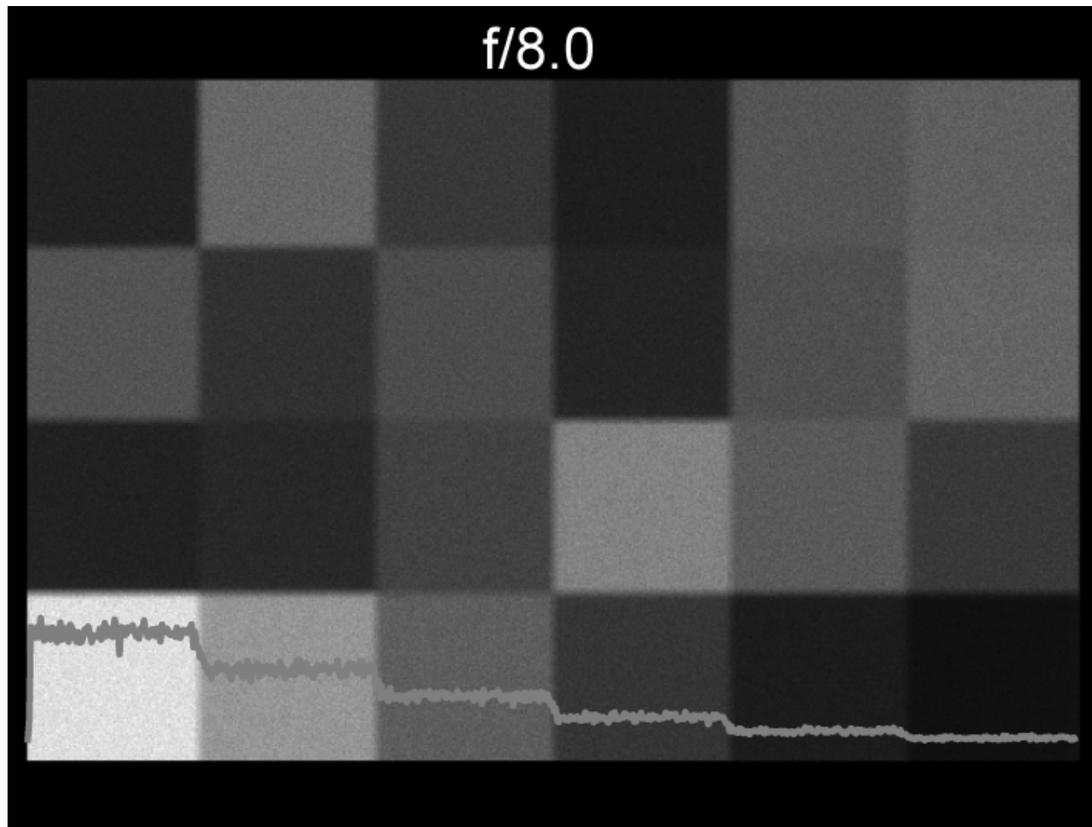


# Photon noise: Visibility (monochrome)



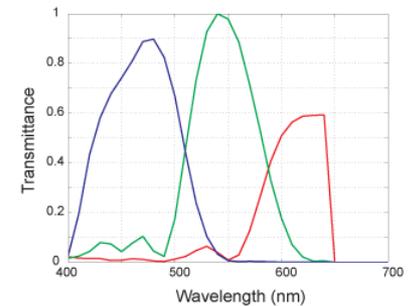
Luminance range: 12 - 1.25 cd/m<sup>2</sup>  
Exposure time: 10 ms

# Photon noise: Visibility (monochrome)



Luminance range: 12 - 1.25 cd/m<sup>2</sup>  
Exposure time: 10 ms

# Photon noise: Visibility (color)



Additional processing steps usually amplify noise in color images

Mean luminance:  $100 \text{ cd/m}^2$   
Exposure time: 10 ms  
Imaging lens: f/2.8

# Photon noise: Visibility (color)

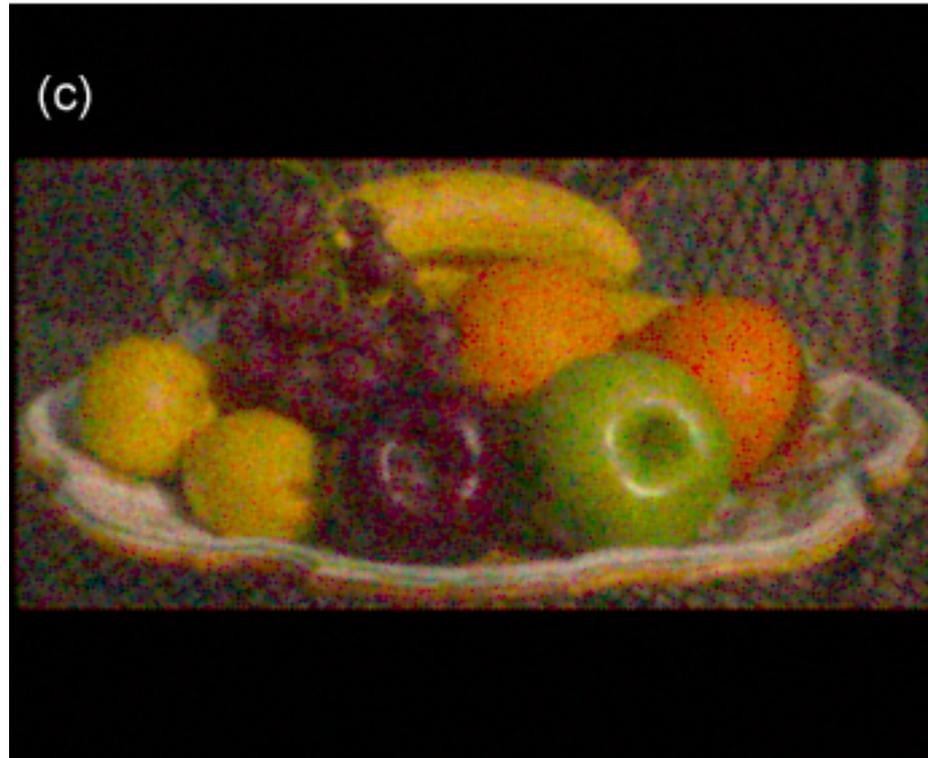


Mean luminance:  $10 \text{ cd/m}^2$

Exposure time: 10 ms

Imaging lens: f/2.8

# Photon noise: Visibility (color)

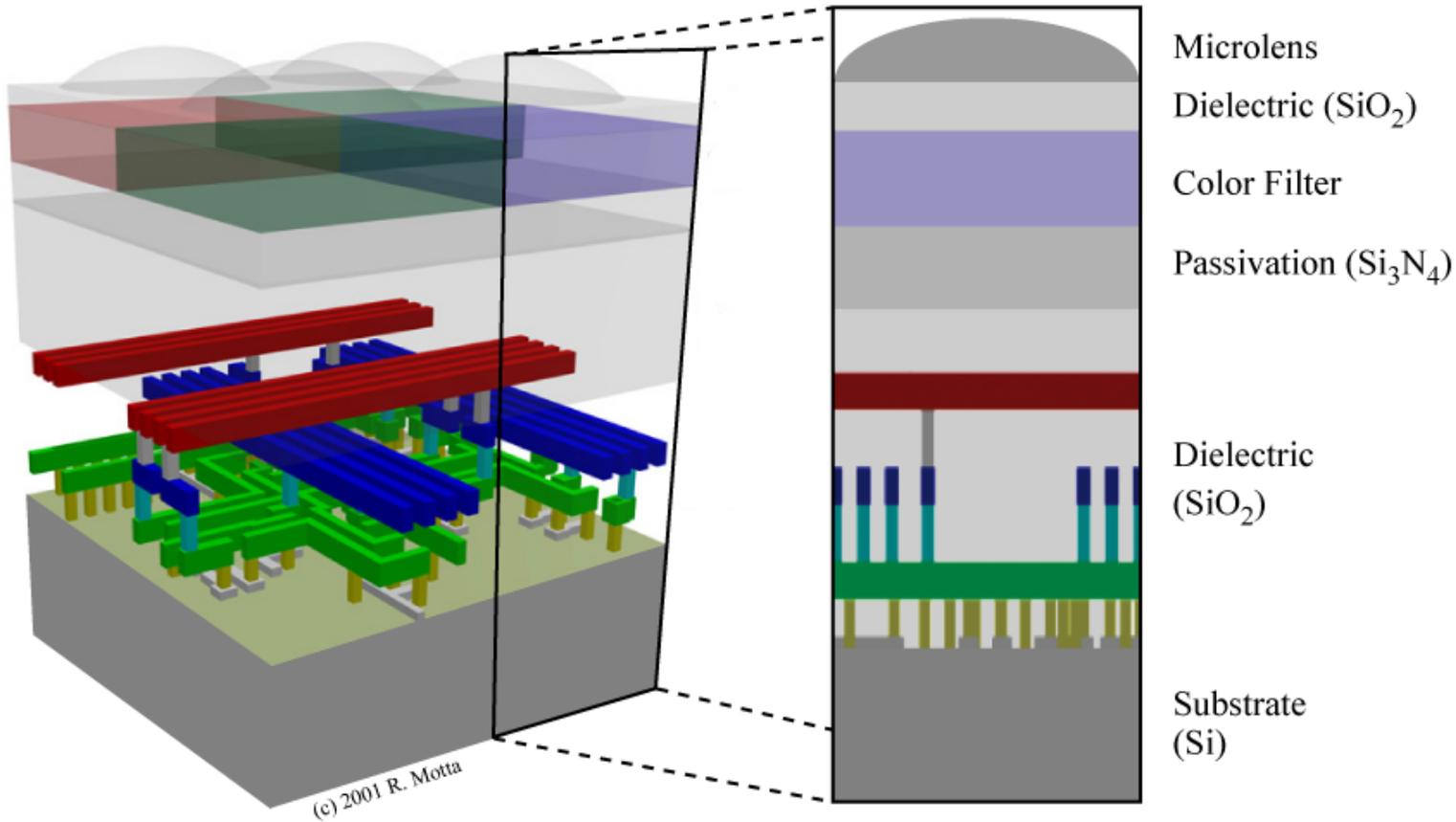


Mean luminance:  $10 \text{ cd/m}^2$

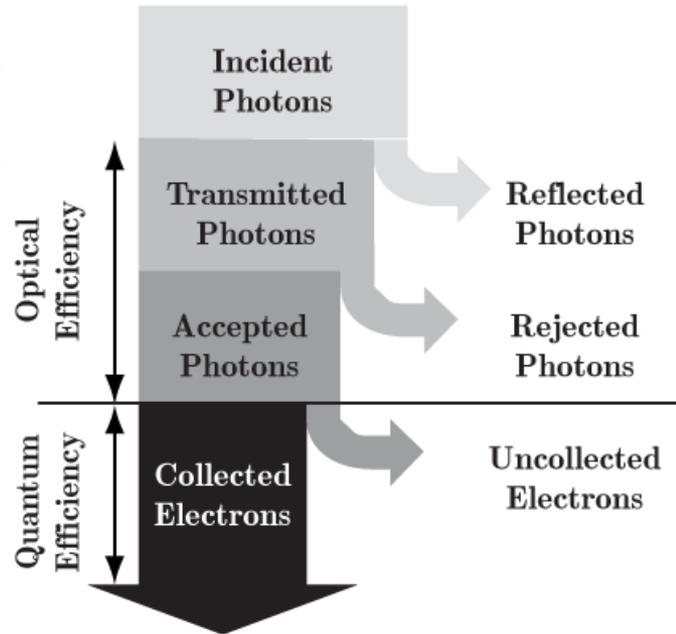
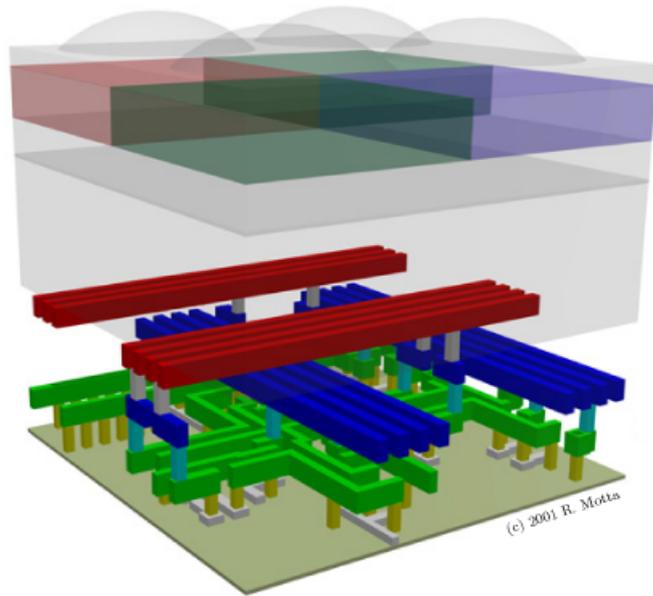
Exposure time: 10 ms

Imaging lens: f/8.0

# Typical image sensor pixel



# Pixel optics: Capture every photon!



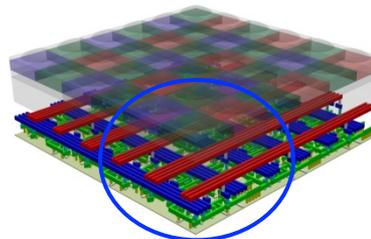
- Pixel QE = Optical Efficiency (OE) + internal QE
- Optical X-talk (OX) (in addition to electrical X-talk)
- Collecting and guiding: maximize OE & minimize OX

# Optics of digital camera systems

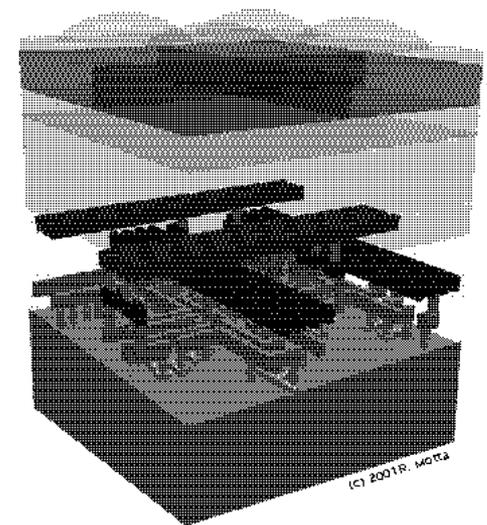
Imaging optics  
( $\gg \lambda$ )



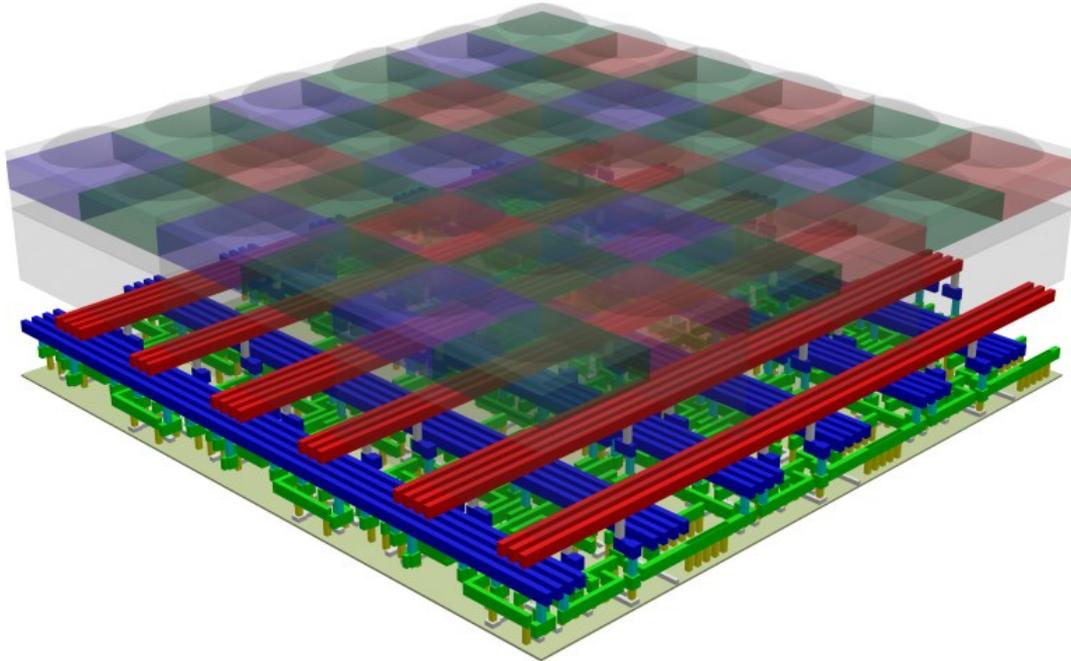
Collecting optics  
( $> \lambda$ )



Guiding optics  
( $< \lambda$ )



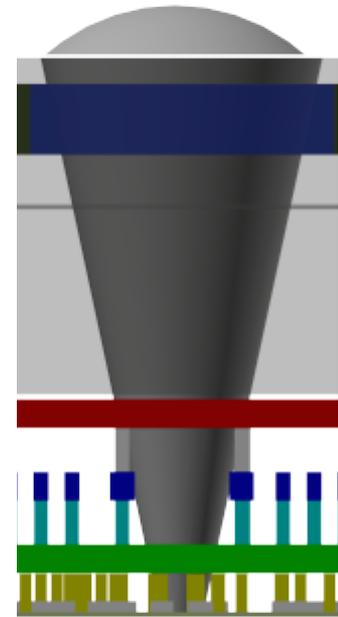
# Collecting optics: The basics



- Etendue  $G$ , Concentration  $C$

$$C = \frac{NA_{\mu Lens}}{NA_{Lens}} \approx \frac{n_{\mu Lens}}{n_{Lens}} \frac{f / \#_{Lens}}{f / \#_{\mu Lens}}$$

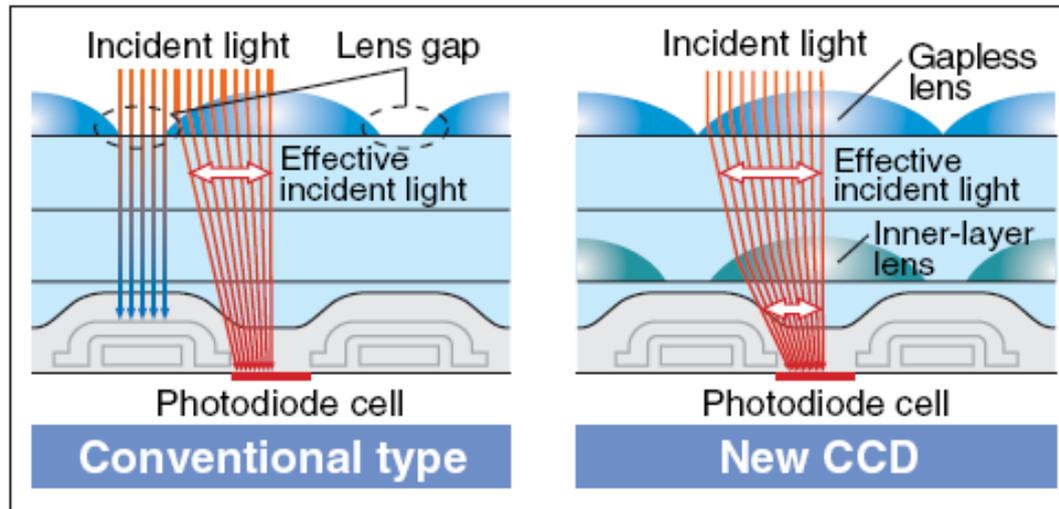
$$G = 2NA_{Lens} w$$



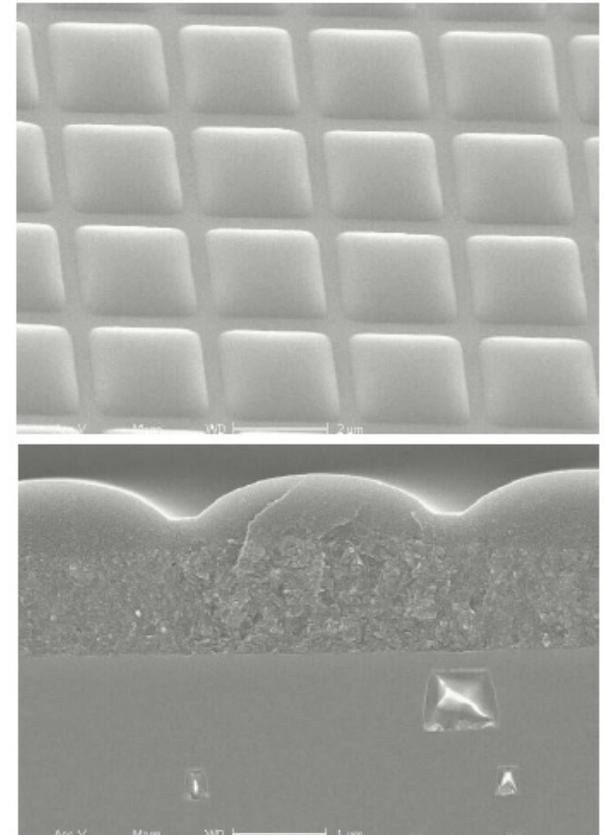
$$G = 2NA_{\mu Lens} w_{Diode}$$

# Collecting optics: Examples

- Micro-lens arrays
  - Single → double
  - Circular → gapless
  - Refractive → diffractive/Fresnel



Panasonic CCD technology



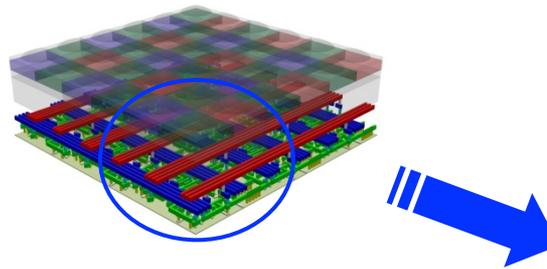
H. Rhodes *et al.*, IEEE (2004)

# Optics of digital camera systems

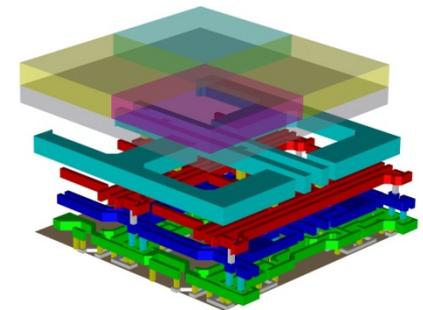
Imaging optics  
( $\gg 1$ )



Collecting optics  
( $> 1$ )

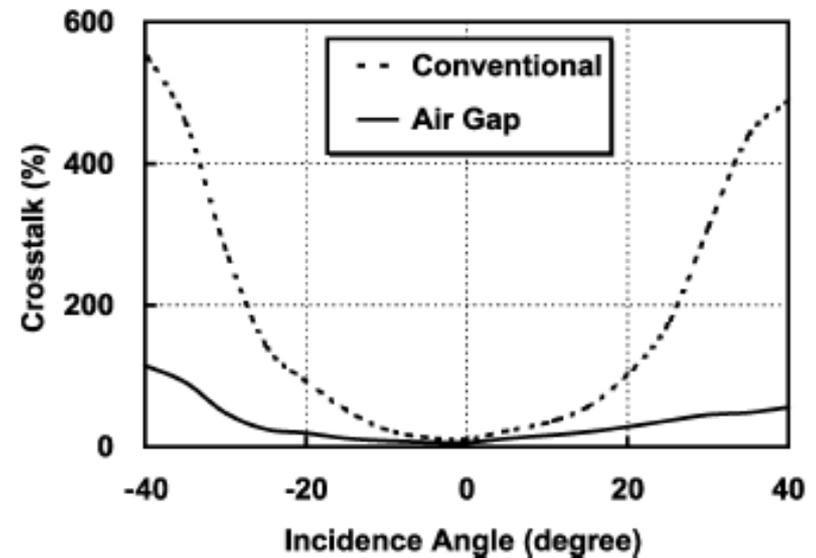
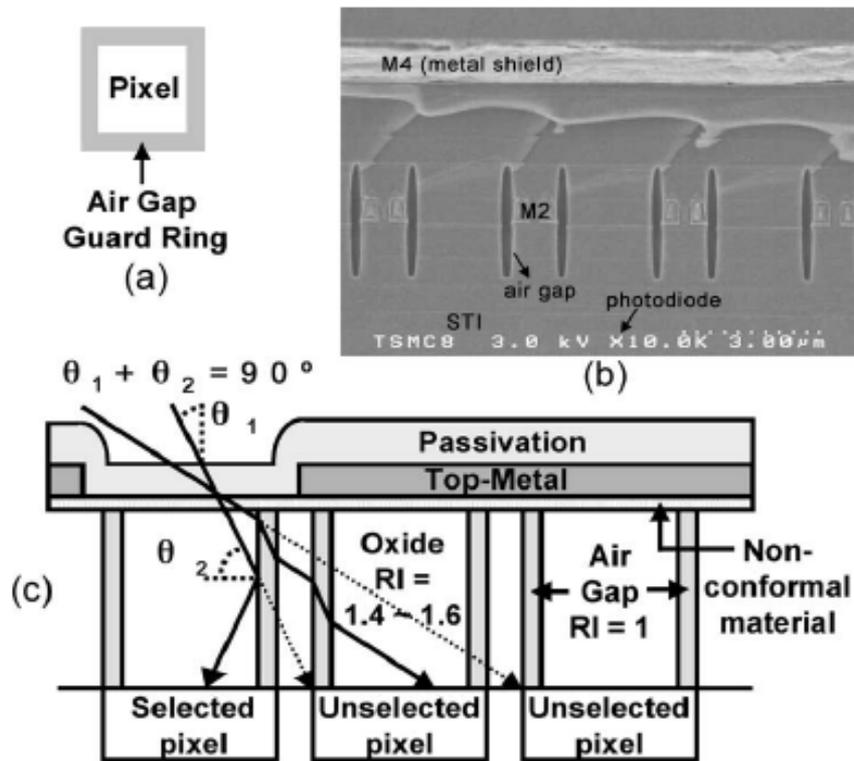


Guiding optics  
( $< 1$ )



# Guiding optics: Examples

- Air gap “Guard ring”: TIR waveguide



# Pixel scaling = Optical problems

- Motivations for reducing pixel size
  - Decrease cost per sensor
  - Increase number of pixels per area (spatial resolution)
- Reducing pixel size leads to:
  - Less light incident on each pixel
    - Noise visible when less than 1000 photons
  - More diffraction, spreading out light
    - Decrease in Optical Efficiency (OE)
    - Increase in Optical Crosstalk (OX)

Catrysse, P.B. and Wandell, B.A., Proc. SPIE 5678, 1-13 (2005)

Xiao, F. *et al.*, Proc. SPIE 5678, 75-84 (2005)



# Definitions (Fuji, and others)

**Photodiode:** A single, light-sensing element on a sensor.

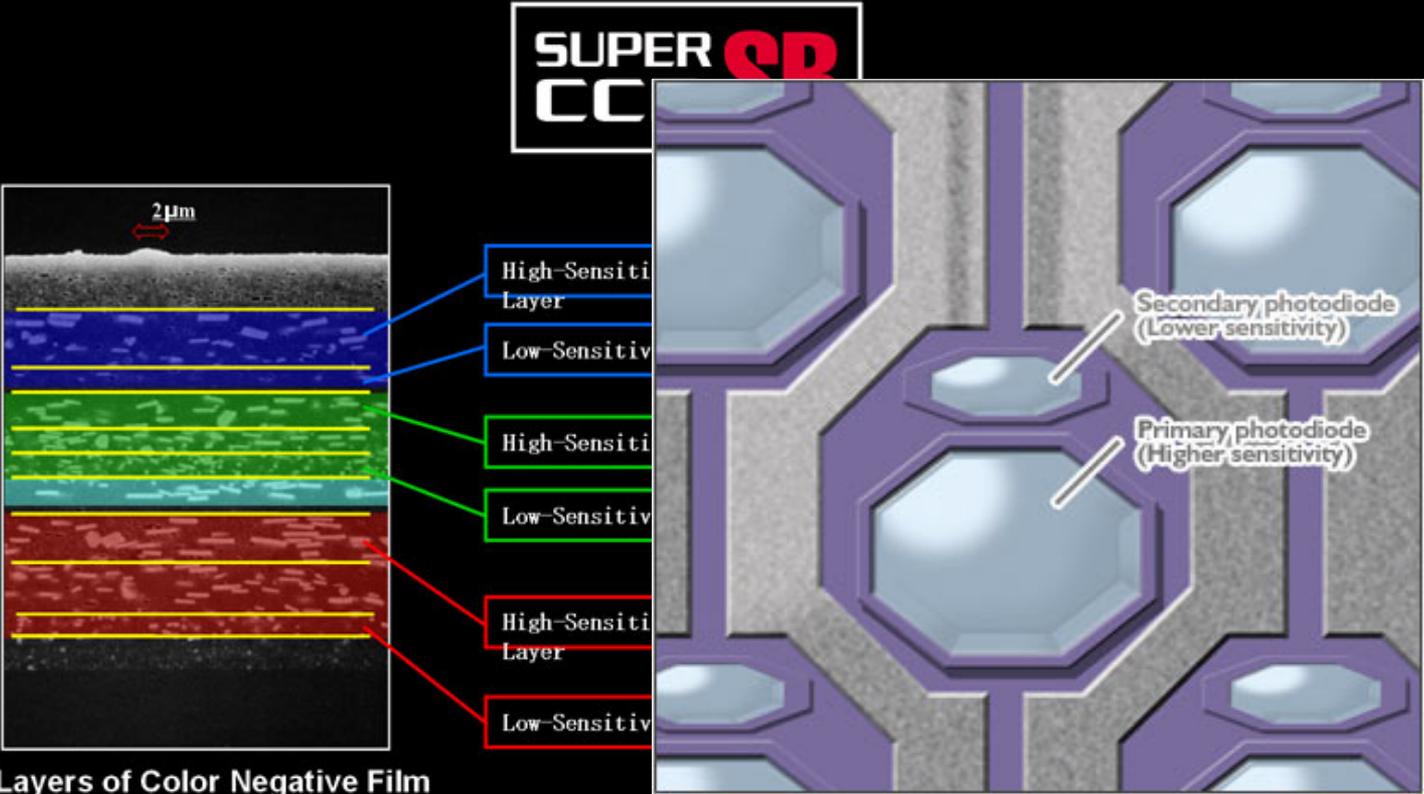
**Photosite:** The area on a sensor where the light from one point of the image is received. The light entering the photosite passes through one microlens and one color filter. With a traditional sensor, there is one photodiode beneath the microlens, whereas with Double Honeycomb Super CCD, there are two photodiodes: a primary and a secondary photodiode.

**Pixel:** A final point of picture information in the outputted image. This normally equates to one printed 'dot', or a square of information on the image when displayed on a monitor.

**An explanation of Dynamic Range:** Unlike the human eye, which can rapidly adjust to differing intensities of light inherent within a contrasty scene, photographic media (film and digital sensors) are constrained by having to align themselves to expose correctly for a given intensity of light. If the camera exposes bright areas correctly, the shadow areas darken out, and detail is lost. Conversely, if the camera exposes shadow areas correctly, the bright areas will appear as burnt-out whites. A camera with good dynamic range will possess the exposure flexibility to accommodate these extremes and expose both bright and shadow areas correctly.

# High dynamic range CCD imager (Fuji)

**SUPER CCD**



The diagram illustrates the structure of the Super CCD SR. On the left, a cross-section of color negative film is shown with a 2 μm scale bar. It consists of alternating layers of high-sensitivity and low-sensitivity emulsion. On the right, a top-down view of the Super CCD SR shows two types of photodiodes: a primary photodiode with higher sensitivity and a secondary photodiode with lower sensitivity, arranged in a grid pattern.

Layers of Color Negative Film

- High-Sensitivity Layer
- Low-Sensitivity Layer
- High-Sensitivity Layer
- Low-Sensitivity Layer
- High-Sensitivity Layer
- Low-Sensitivity Layer

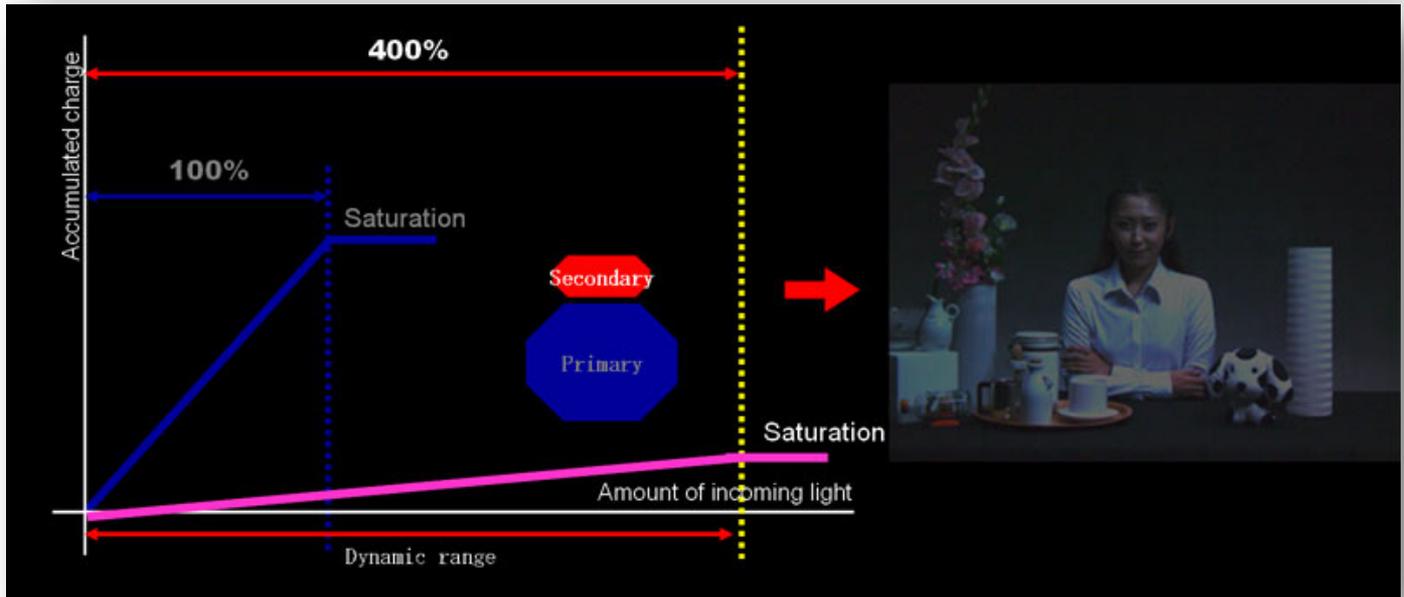
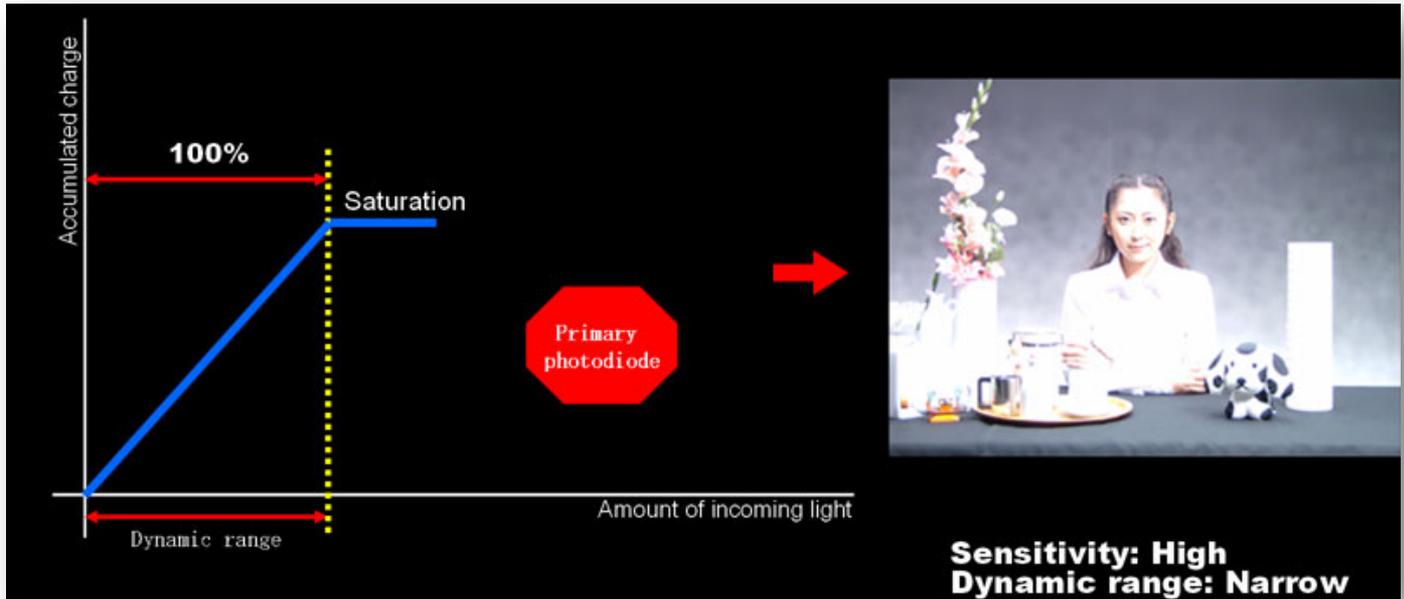
Secondary photodiode (Lower sensitivity)

Primary photodiode (Higher sensitivity)

- The Super CCD SR was developed specially to simulate the extended tonal range characteristics of color negative film.
- The Super CCD SR mimics the structure of negative film by using two photodiodes at two different sensitivities.

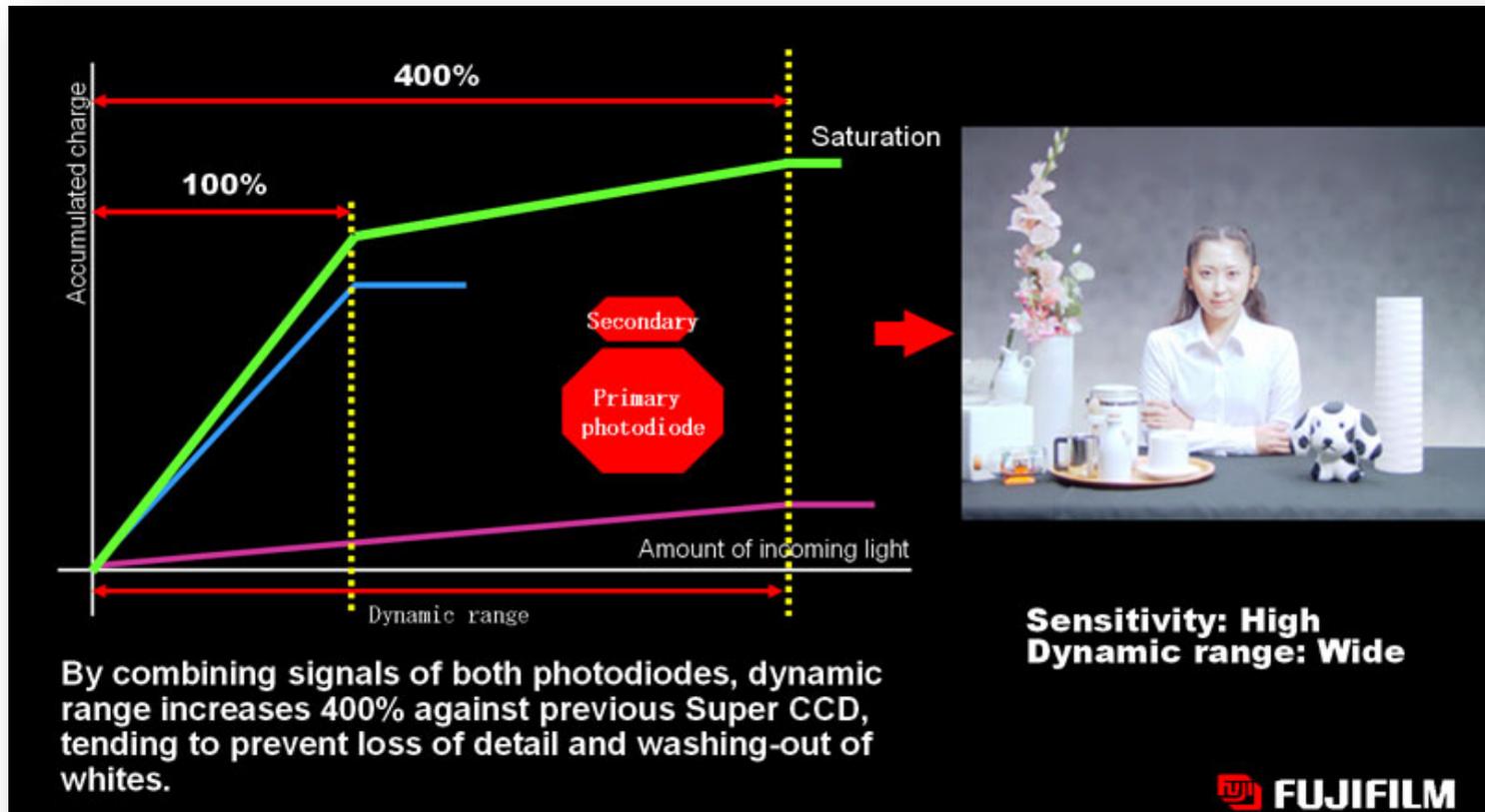
**FUJIFILM**

The secondary detector continues to accumulate charge after the primary saturates.

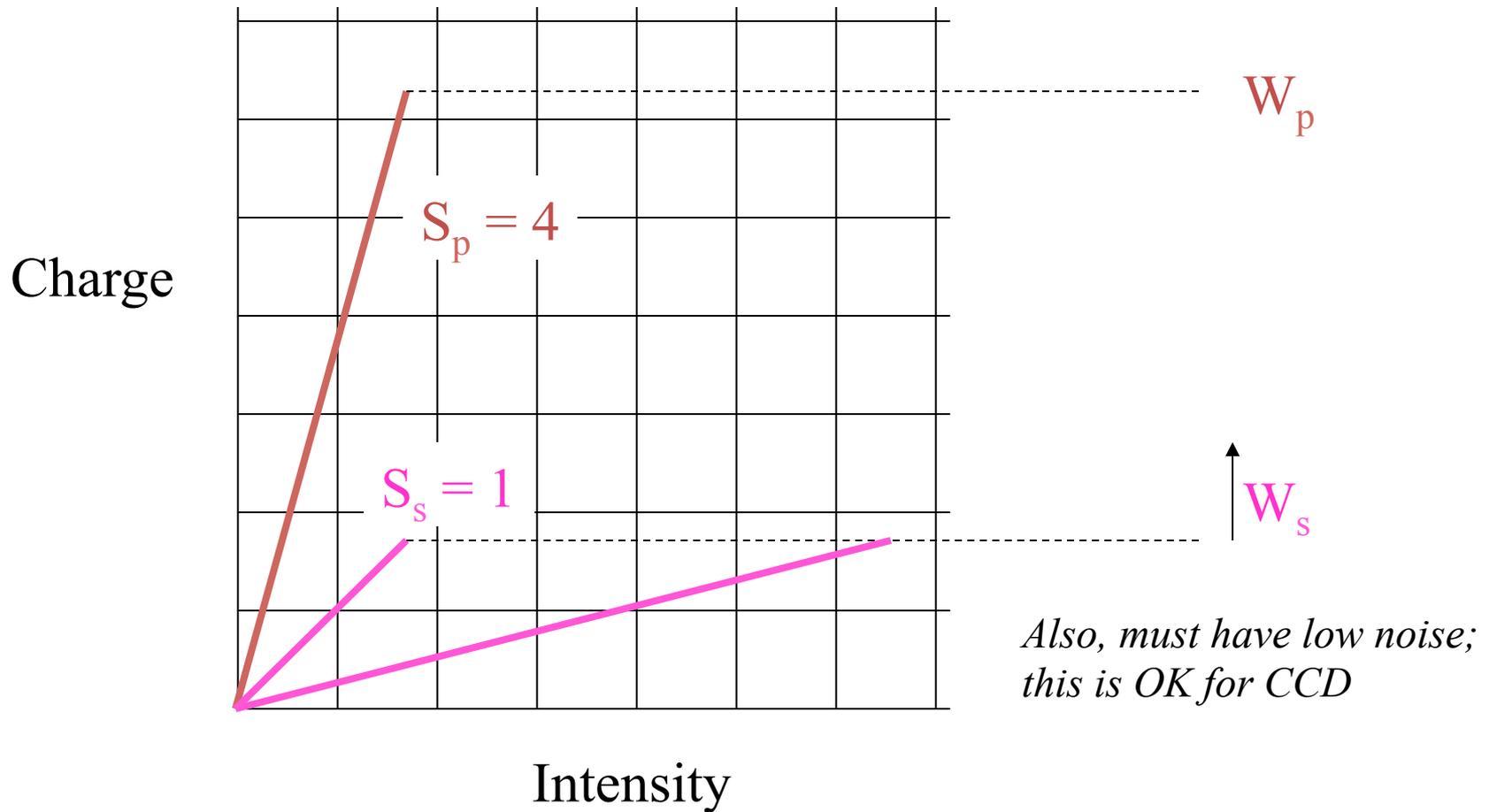


# Dynamic range enhancement combines the two captures

*Transduction function range is increased*

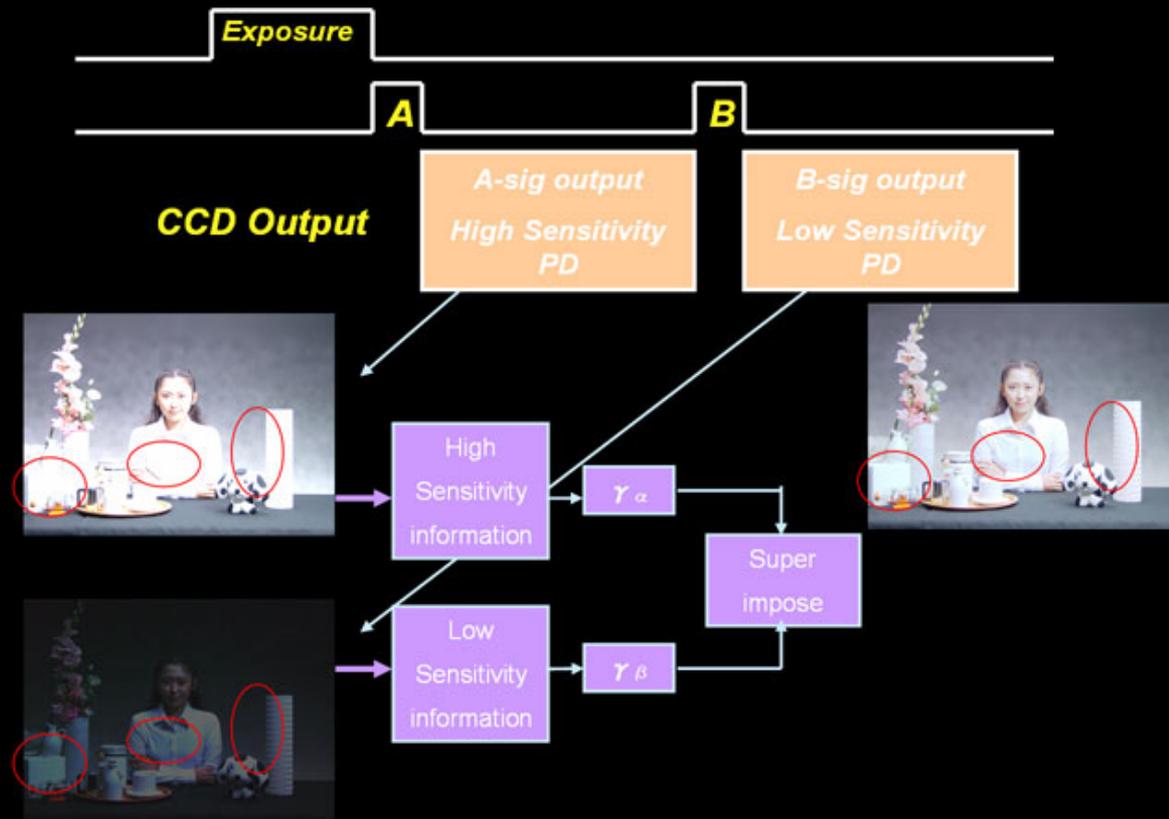


$$W_s/W_p > S_s/S_p$$



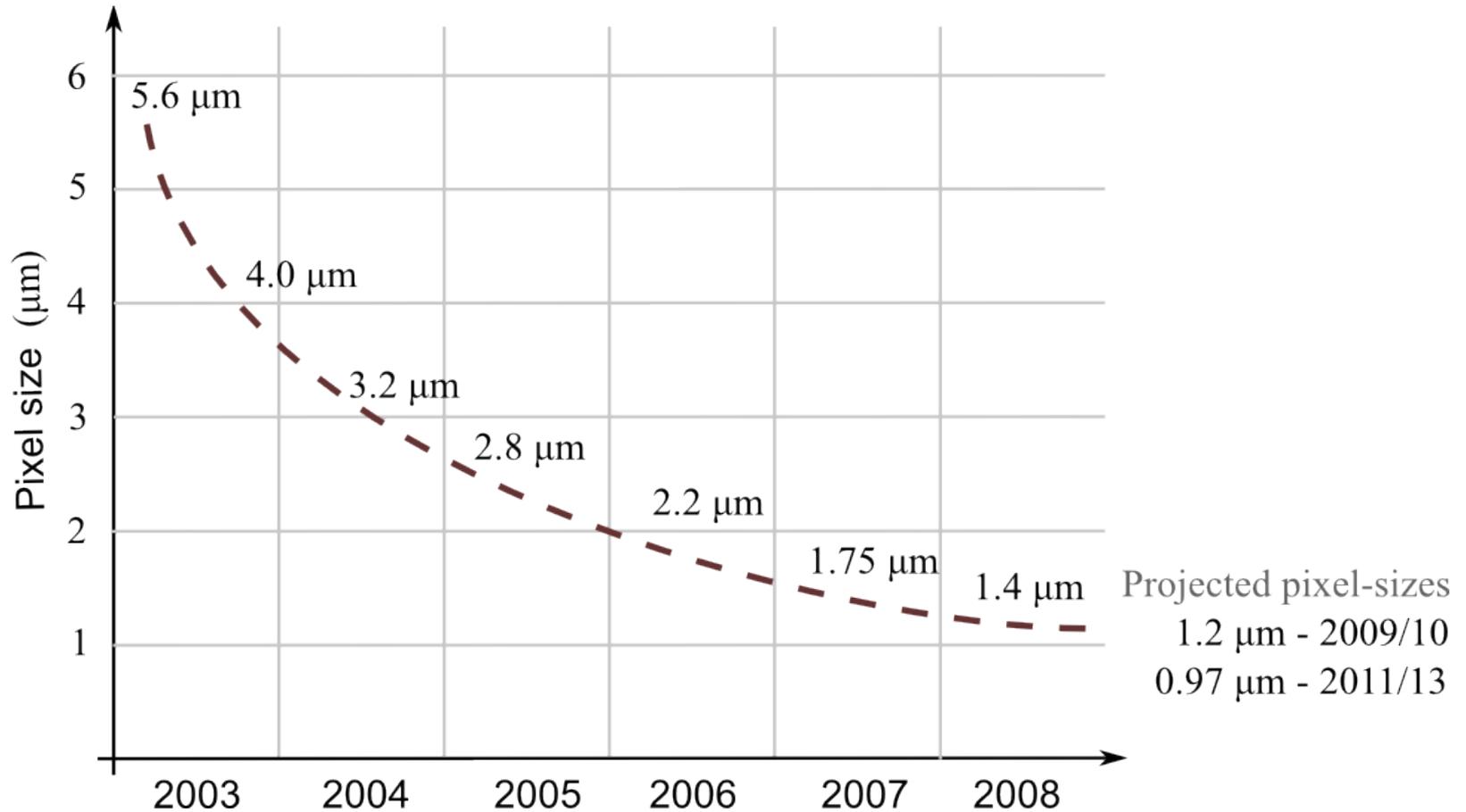
# Dynamic range

## Time Flow



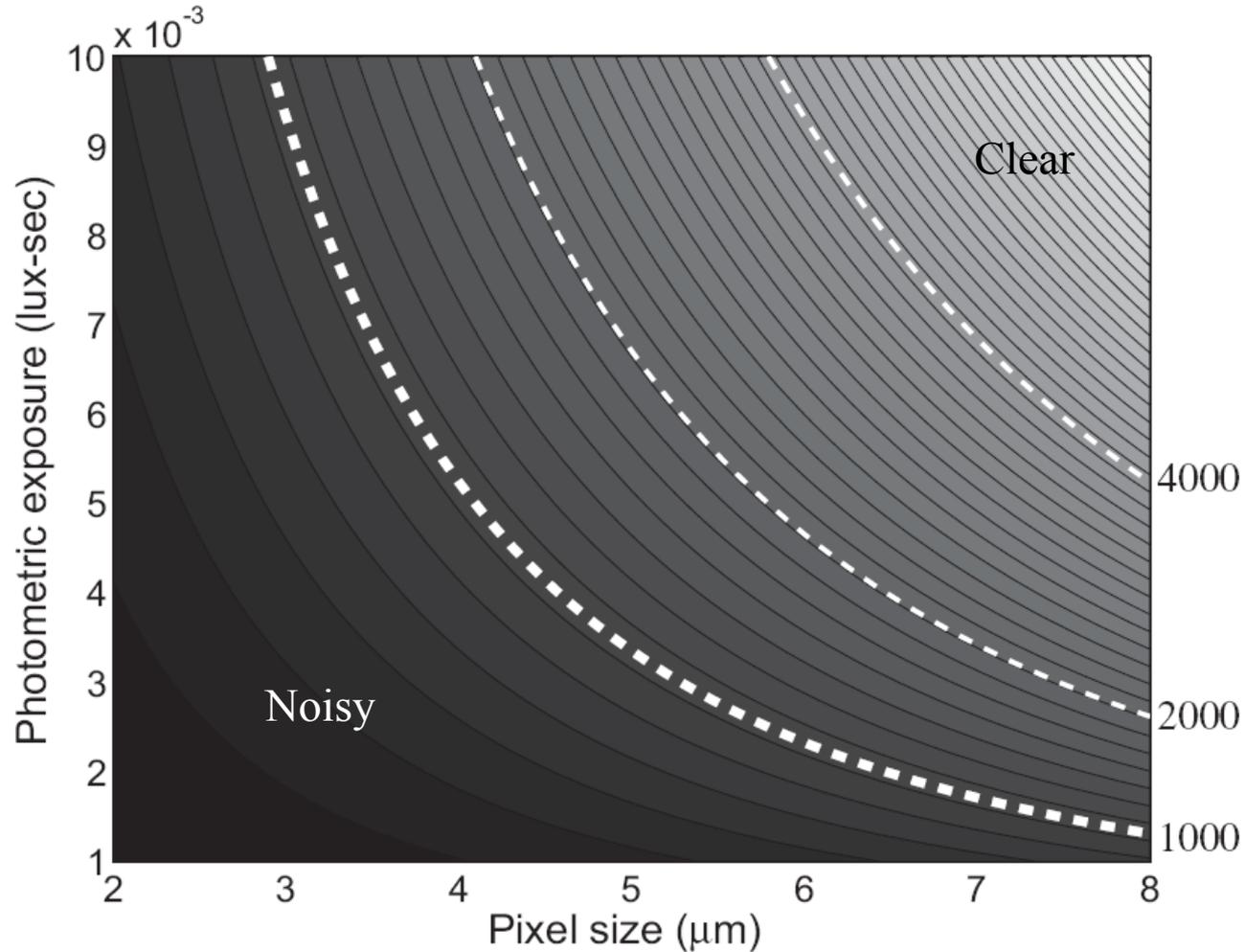
The problem is only getting worse

## Pixel-size trends in 1/4" Image sensors (cell phone cameras)

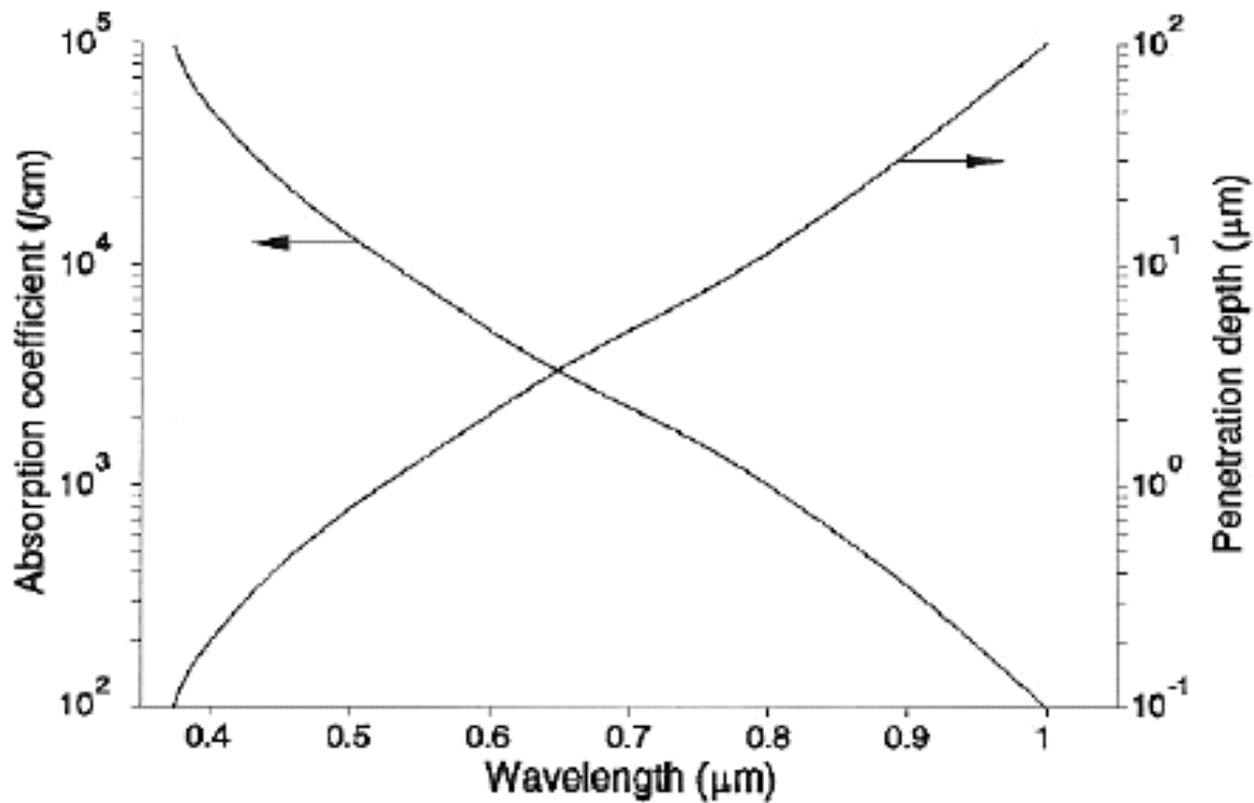


# The problem is only getting worse

Pixel-size trends in 1/4" Image sensors (cell phone cameras)



# Mean photon absorption or penetration depth in silicon



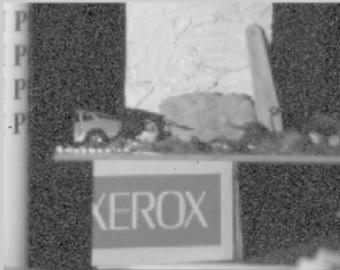
# 1<sup>st</sup> Generation Implementation (D. Yang et al., IEEE JSSC, 1999)



- *Imager: 640 x 512*
- *Pixel: 10.5 micron*
- *Technology: 0.35 micron*
- *ADC shared x 4*
- *Control signals FPGA*
- *Fill factor ~ 29%*
- *QE ~10%*
- *Really cool, though*

# MCSI: HDR Example

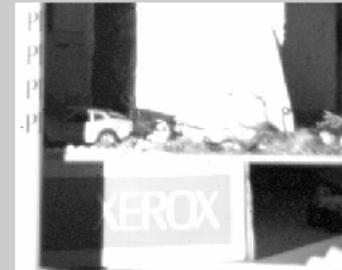
Exposure 1



Exposure 2



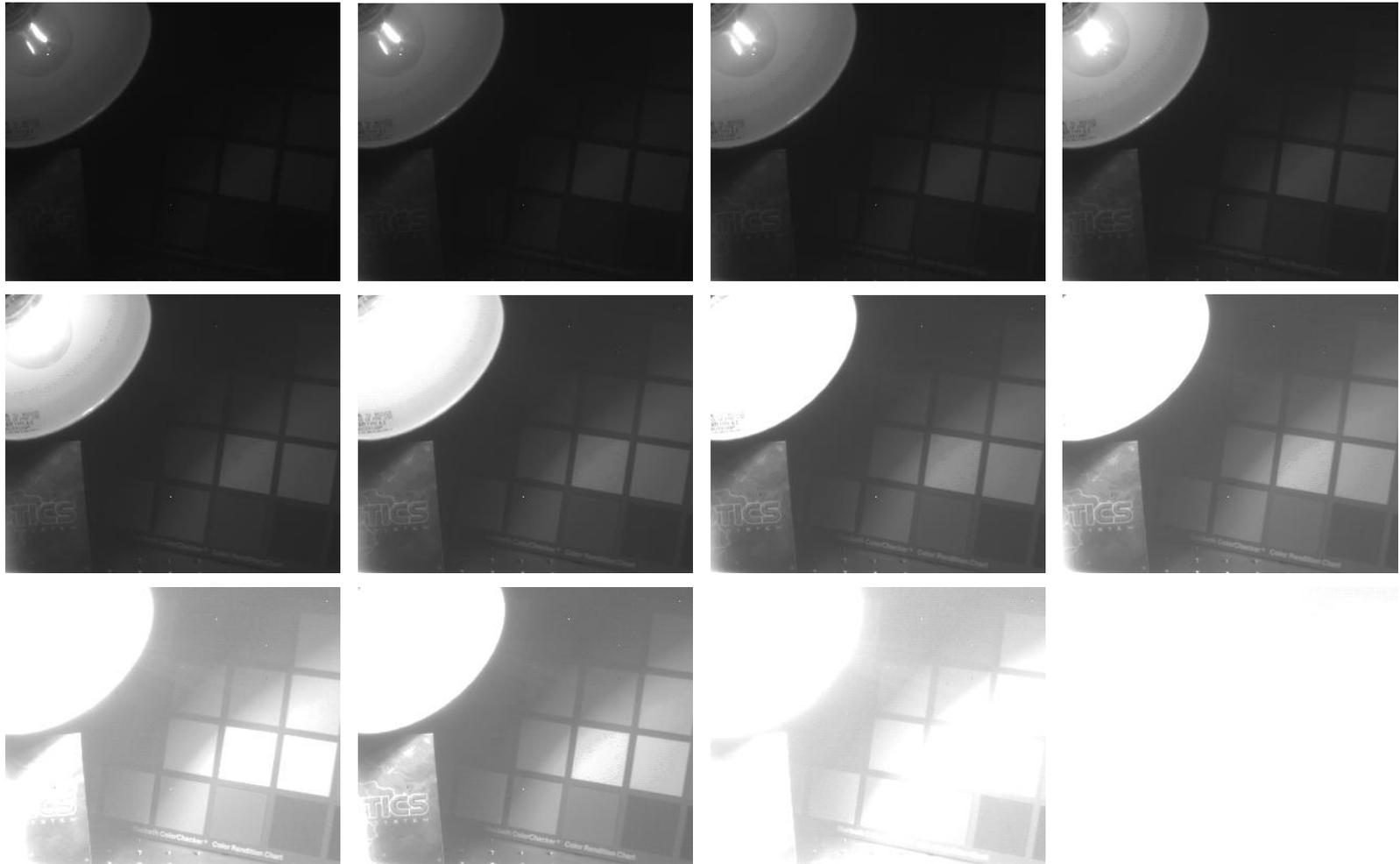
Exposure 3



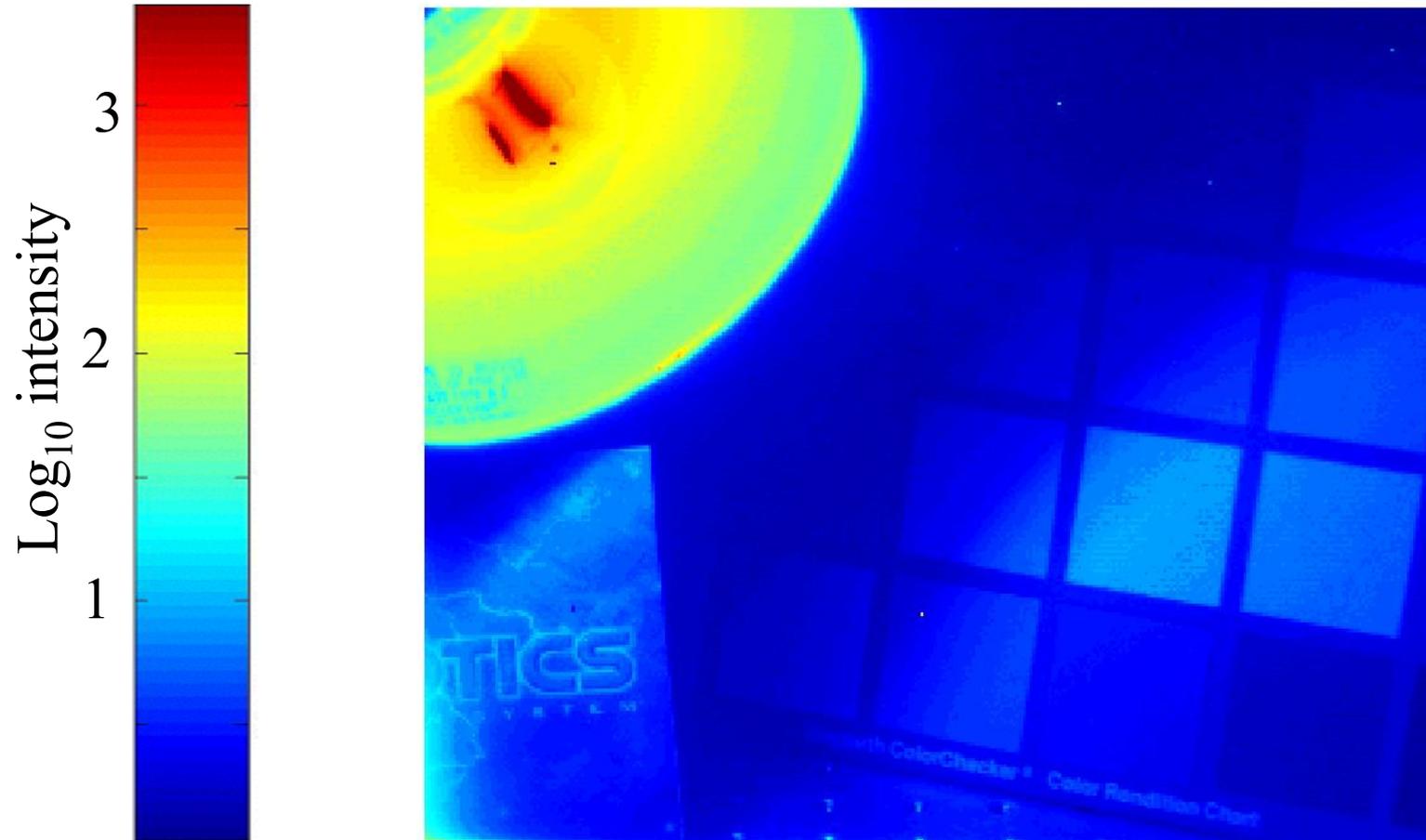
Combined HDR image



# MCSI: HDR Example

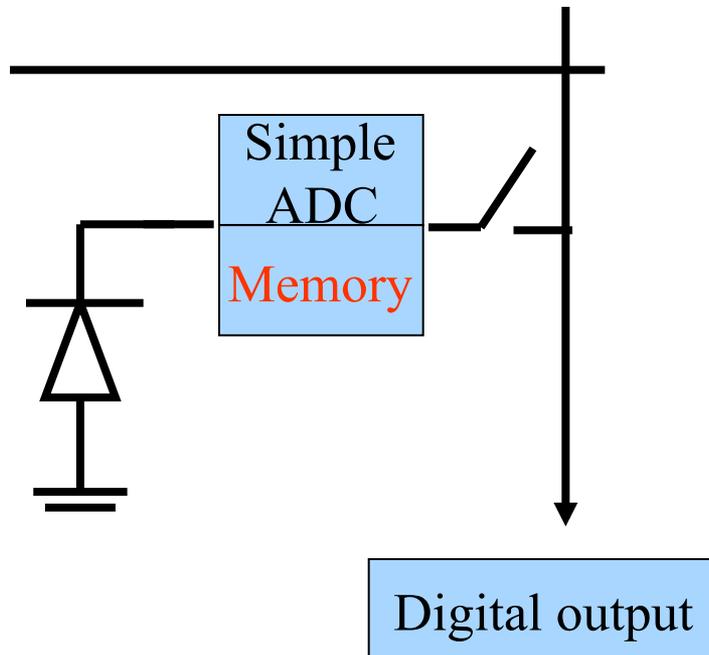


# MCSI: HDR Example



# 2nd Generation: 10,000 Frames/Sec DPS Chip

(S. Kleinfelder et al., IEEE JSSC, 2001)

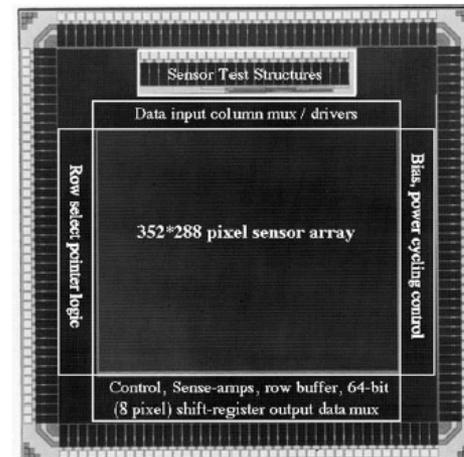
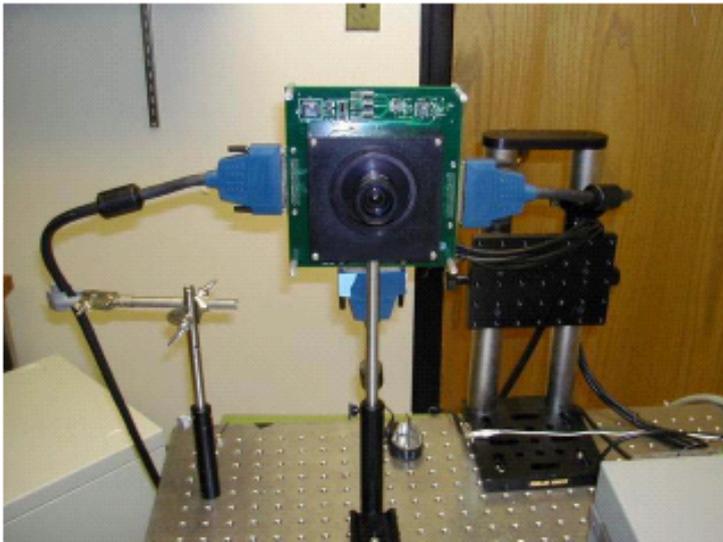


- *Imager: 352 x 288*
- *Pixel: 9.4 micron*
- *Technology: 0.18 micron*
- *ADC and 8bit memory per pixel*
- *Integrated*
- *QE ~14%*
- *Fill factor ~ 15%*
- *Significant dark noise*
- *Really cool, though*

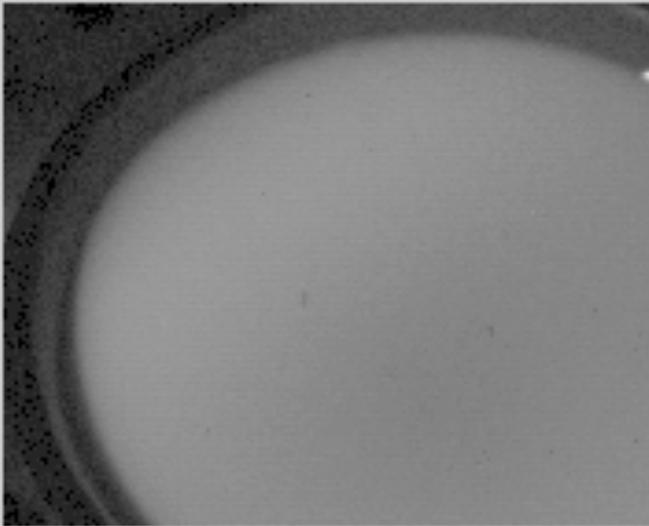
# 2<sup>nd</sup> Generation System

(Kleinfelder, Lim, Liu)

- *Based on CMOS-DPS (ADC, Memory)*
- *Interfaced via 3 NI cards to PC*
- *Programmable via Matlab interface*
- *Runs up to 1400 frames per sec*

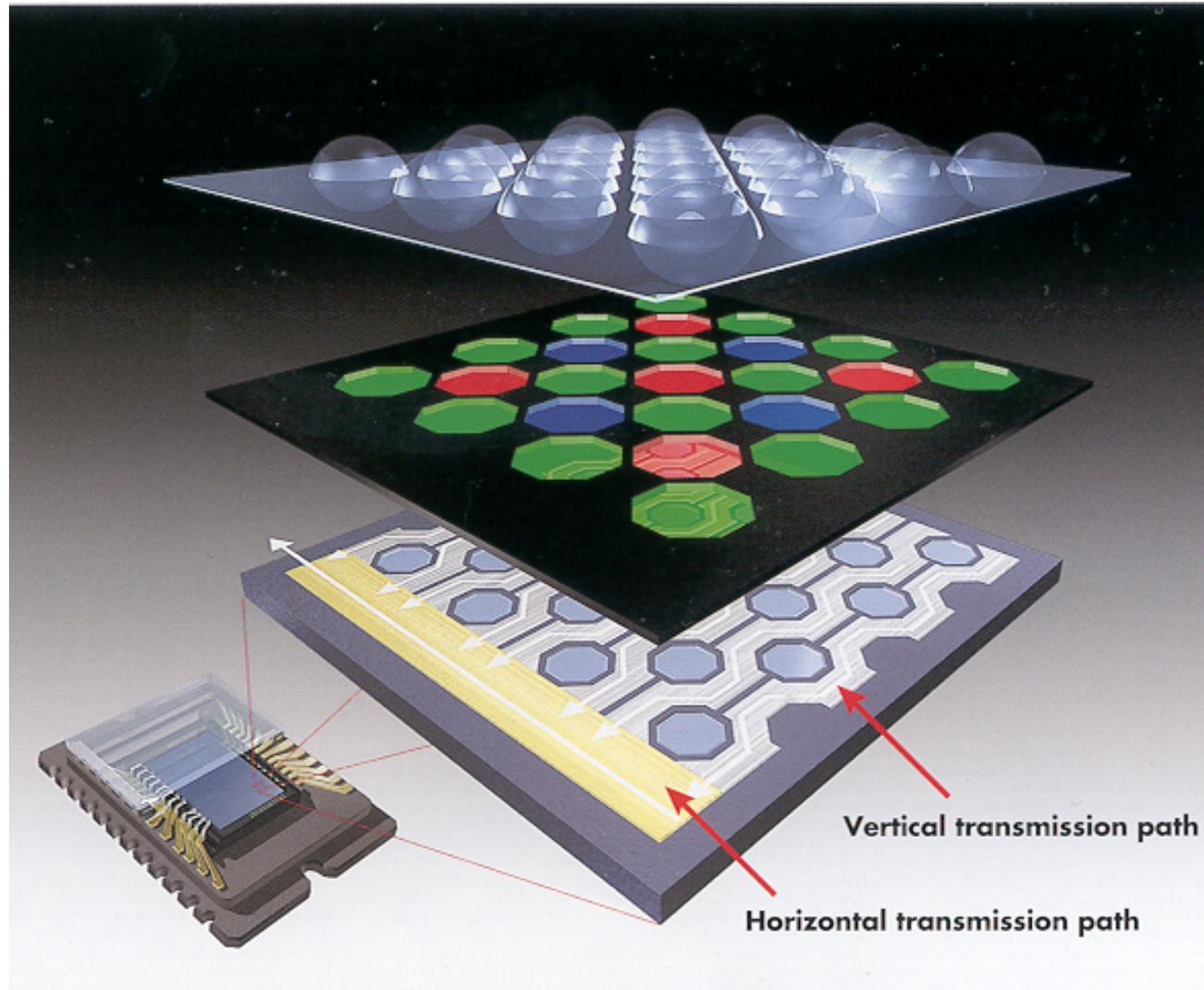


# System Example: Milk Drop



*Correlated double sampling*  
*1400 fps*  
*Play back at 30 fps*

# Image sensors: Structures and Capture

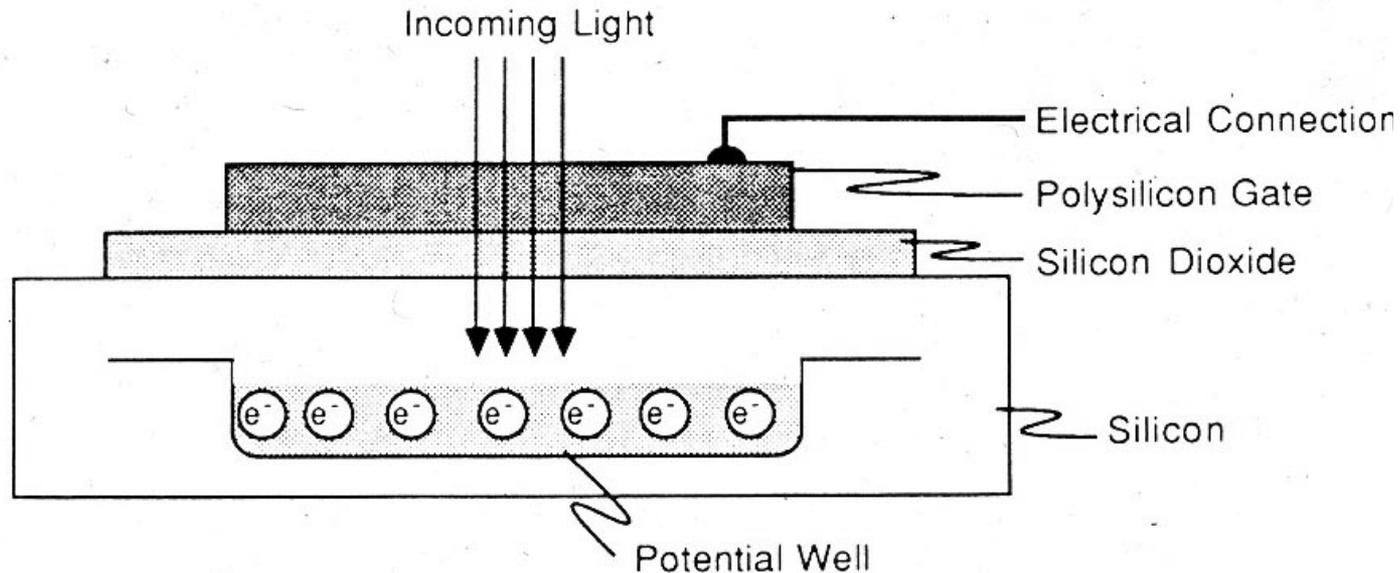


# CCD pixel structure

(Simon Tulloch [smt@ing.iac.es](mailto:smt@ing.iac.es))

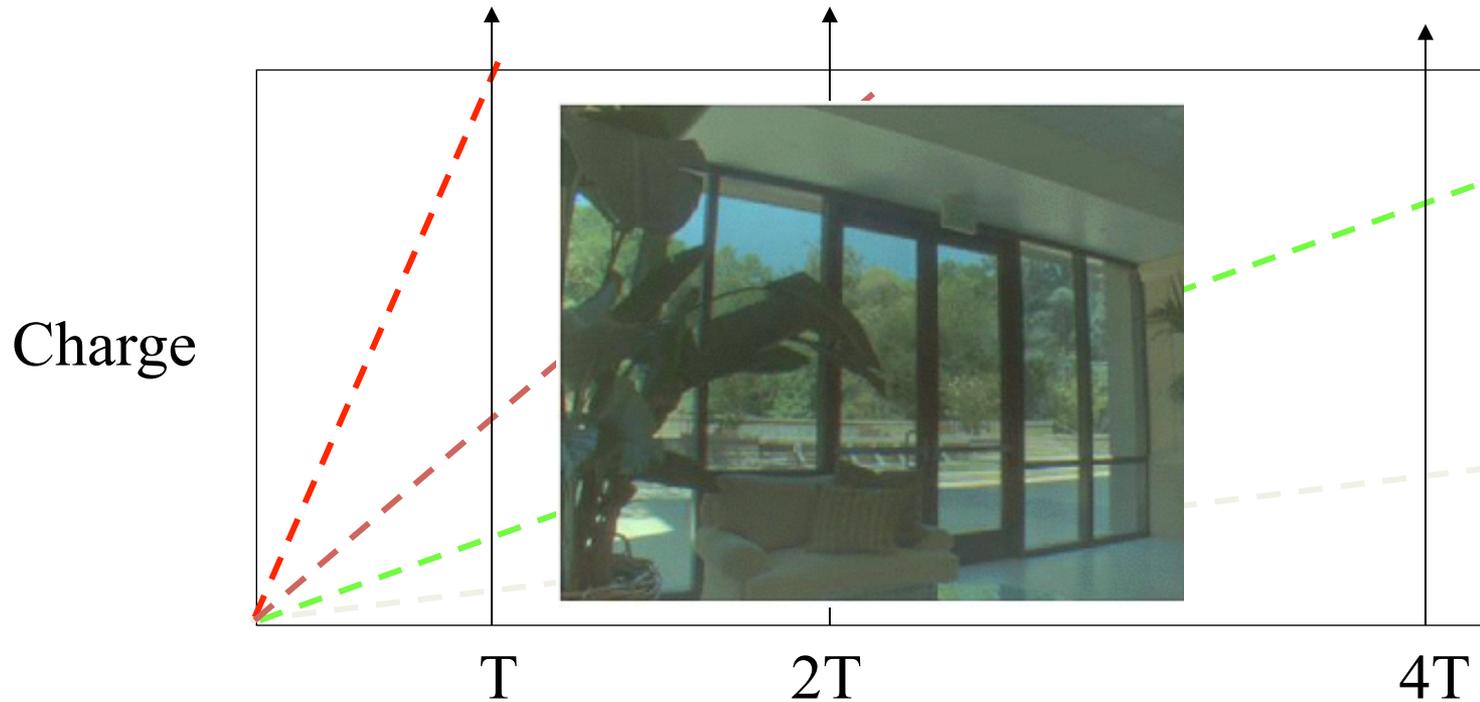
Invented in the 1970s as memory devices; light sensitive properties were exploited for imaging applications; a major revolution in Astronomy.

They improved the light gathering power of telescopes by almost two orders of magnitude. In 2001 an amateur astronomer with a CCD camera and a 15 cm telescope collects as much light as an astronomer of the 1960s equipped with a photographic plate and a 1m telescope.



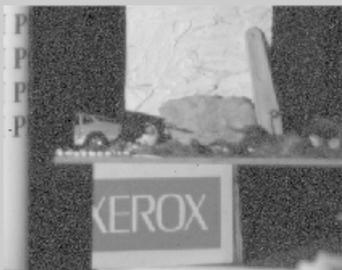
Stores as many as  $10^5$  electrons, though  $10^4$  more typical

# Multiple Capture Single Image



# Multiple Capture Single Image: High Dynamic Range Application

Exposure 1



Exposure 2



Exposure 3



Combined HDR image



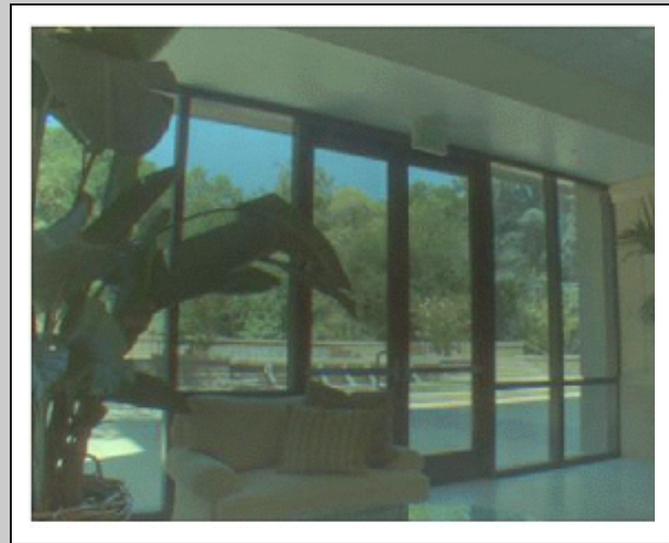
# MCSI: High Dynamic Range (HDR)

## Multiple captures



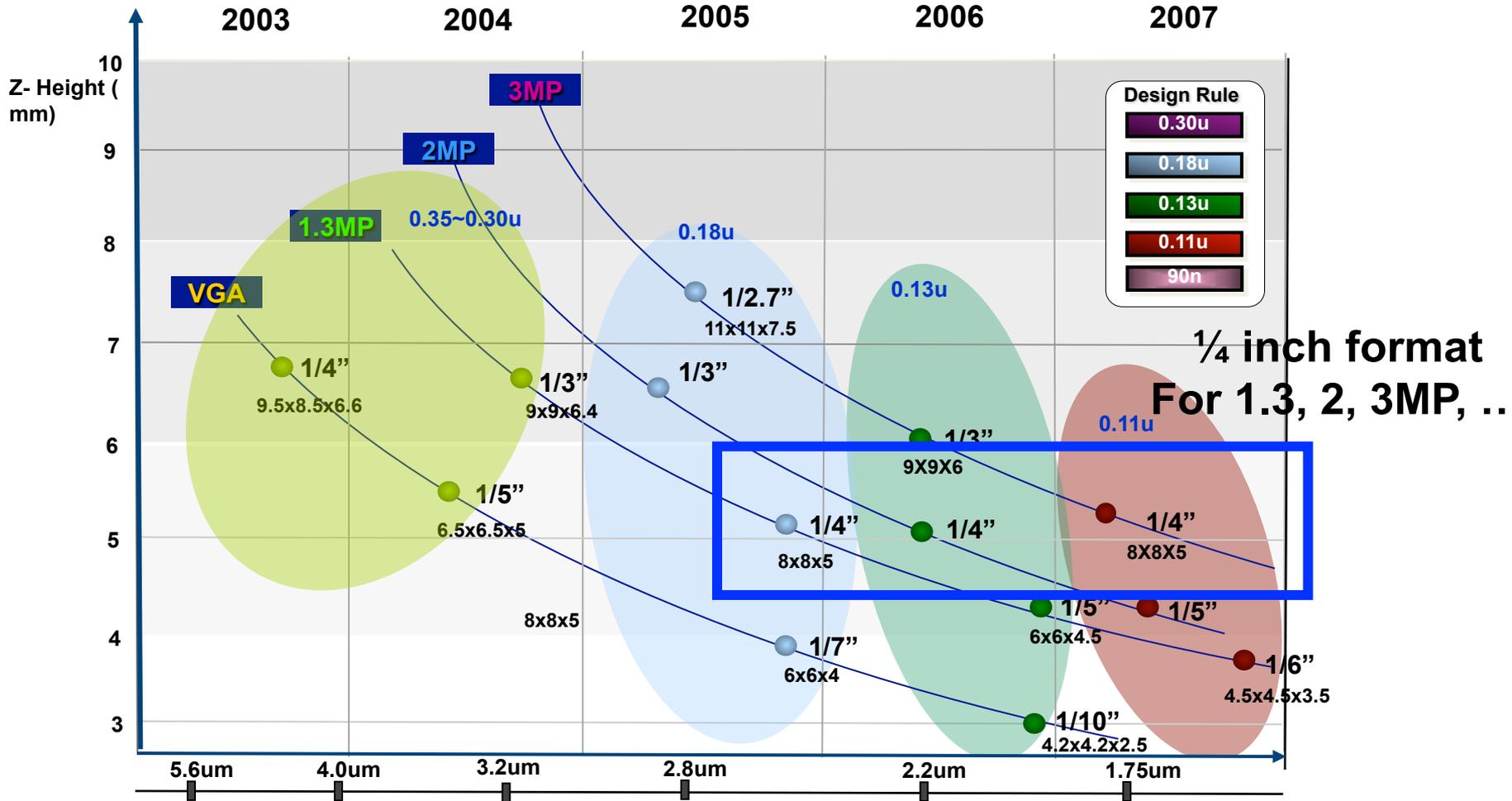
*Exposure bracketing*

## Single image



*High dynamic range  
image*

# Camera Module – Trend by Optical format & form factor



This is from a public talk given by Magnachip. Use the information freely, but please do not use this slide directly in your presentation!

# CMOS sensor characterization



- Goal:
  - Develop a noise model to analyze sensor performance
  - Use sensor model for system-level simulations
- Review sensor noise modeling terminology
  - Temporal
  - Spatial
- Sample characterization results

## ■ Temporal noise components

- $Q_{\text{shot}}$  : shot noise during integration (photo and dark currents)
- $Q_{\text{reset}}$  : reset noise
- $Q_{\text{read}}$  : readout noise (including A/D quantization noise)

## ■ Spatial noise components

- Fixed pattern noise due to mismatches across the sensor
- Offset and gain components
  - Offset: Canceled out by correlated double sampling, except DSNU
  - Gain: Pixel response non-uniformity (PRNU) not canceled

- Total input-referred noise charge

- $Q_n = Q_{\text{shot}} + Q_{\text{reset}} + Q_{\text{read}} + Q_{\text{fpn}}$

- After CDS,  $Q_n = Q_{\text{shot}} + Q_{\text{read}} + Q_{\text{prnu}} + Q_{\text{dsnu}}$

- SNR

- $$SNR = \frac{\left( \frac{i_{ph} t_{int}}{q} \right)^2}{\frac{(i_{ph} + i_{dc}) t_{int}}{q} + \frac{\sigma_{idc}^2 t_{int}^2}{q^2} + \sigma_{read}^2}$$

- Neglecting PRNU for now

## ■ Setup

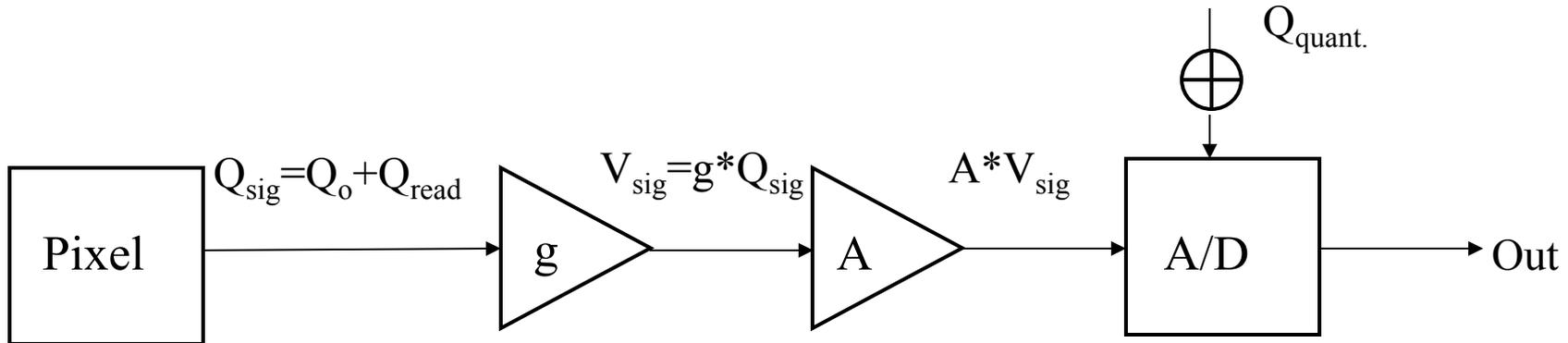
- Dark conditions
- Short integration time (0.1ms)
- Analog gain (A) is 1
- $\sigma_{read}$  is std. deviation of temporal variations over 1000 frames
- Only assumption is that  $i_{dc}/\text{pixel}$  is constant for 100ms

## ■ Sample results

- $\sigma_{read} = 0.86$  digital counts (full signal range = 1023)
- But this is A/D quantization noise-limited
- Also, need to convert to electrons (conversion gain)

# Read Noise Model

- This clarifies read noise characterization



$$\sigma_{Out}^2 = \left( \frac{2^n - 1}{V_{max}} \right)^2 \left[ g^2 A^2 \sigma_{read}^2 + \sigma_{quant.}^2 \right]$$

- For  $A=1$ , dominated by  $Q_{quant.}$
- Want to increase  $A$  to the point where  $Q_{read}$  dominates

# Conversion Gain

THIS IS A  
MESS. FIX  
IT OR  
DELETE IT.

## ■ Setup

- Sensor is in shot-noise limited regime

- Since

- Conversion gain,  $g = \frac{V_s}{SNR}$

- In general, for 10-bit A/D with FSR of

- So,

- Since we don't know  $g$ , can define  $V_{\max}$  as follows

$$g = \frac{I_{sig\ dig}}{SNR} \quad (\text{counts/electron})$$

$$SNR = \frac{CV_s}{q}$$

$$V_{\max} \quad V_s = I_{sig\ dig} \left( \frac{V_{\max}}{2^{10} - 1} \right)$$

$$g = \frac{I_{sig\ dig} \left( \frac{V_{\max}}{2^{10} - 1} \right)}{SNR}$$

## ■ Results

- What we measure is actually  $A \cdot g$ , where  $A$  is analog gain
- With  $A=1$ , approx. 20 electrons/count
- Assuming FSR of 1.5V,
  - $g = 70\mu\text{V}/\text{electron}$
  - This is “true” conversion gain

## ■ So in electrons

- Read noise = 17 electrons (A/D quantization noise)
- Full well = 20500 electrons

## ■ Absolute read noise floor can be lowered with $A$ gain

## ■ Results

- Analog gain = 16
- $\sigma_{read} = 3.2$  digital counts
- Approx. 2 electrons/count (theoretically 20/16)
- Actual pixel read noise = 4-6 electrons

## ■ May not want to operate at maximum analog gain

- Limits dynamic range
- A=8 is sufficient

- What are the results sensitive to?
  - Confident of read noise in digital counts
  - But read noise in electrons sensitive to conversion gain
    - So verify conversion gain
- Can verify using dark current shot noise
  - Dark conditions, long integration times (2.5s)
  - Just look at one pixel over 40 minutes (1000 frames)
    - 
    - Only assumption is that pixel dark current is constant over time

$$SNR = \frac{CV_s}{q}$$

## ■ Results

- Conversion gain,  $g = 1/50$  (counts/electron)
  - Assuming 1.5V swing,  $g = 30\mu\text{V}/\text{electron} \rightarrow C = 5.5\text{fF}$
  - Assuming 1.1V swing,  $g = 22\mu\text{V}/\text{electron} \rightarrow C = 7.4\text{fF}$
- Read noise,  $\sigma_{\text{read}} = 10$  electrons
  - Reproducible for  $A = 8$  and  $A = 16$
- Full well = 51,150 electrons
  - So peak SNR, ignoring PRNU, is 47dB (datasheet says 45dB)

## ■ Setup

- Dark conditions @ RT
- Long integration time (2.5s)
- Capture 1000 frames and average
- Mean intensity is dark current, spatial variation is DSNU

## ■ Results

- Mean dark signal = 2200 electrons, or 0.14fA (0.6nA/cm<sup>2</sup>)
- DSNU = 80 electrons or 0.005fA

# Characterization Summary

Read noise, $\sigma_{read}$	10 electrons
Dark current, $i_{dc}$	0.14fA (see next page for amps to electrons)
Dark signal non-uniformity, $\sigma_{i_{dc}}$	0.005fA (see next page for amps to electrons)
Full well capacity, $Q_{max}$	52000 electrons
Peak SNR	47dB
Dynamic range Think about noise-free dynamic range, meaning from 1000 electrons captured to well capacity, or maybe a little more to account for other noise components.	60dB (depends on duration because noise depends on duration)
Pixel conversion gain, $g$	22-30 $\mu$ V/e <sup>-</sup>
Quantum efficiency (550nm)	0.5-0.6

1 Amp is a one coulomb (unit of charge) per second

the charge of an electron is  $1.6 \times 10^{-19}$  so the number of electrons in one coulomb is  $1/1.6 \times 10^{-19}$

$= 6.25 \times 10^{18}$  electrons

so for one Amp that would be  $6.25 \times 10^{18}$  electrons per second flowing around the circuit/component

Femto is  $10^{-15}$

Pico is  $10^{-12}$

Nano is  $10^{-9}$

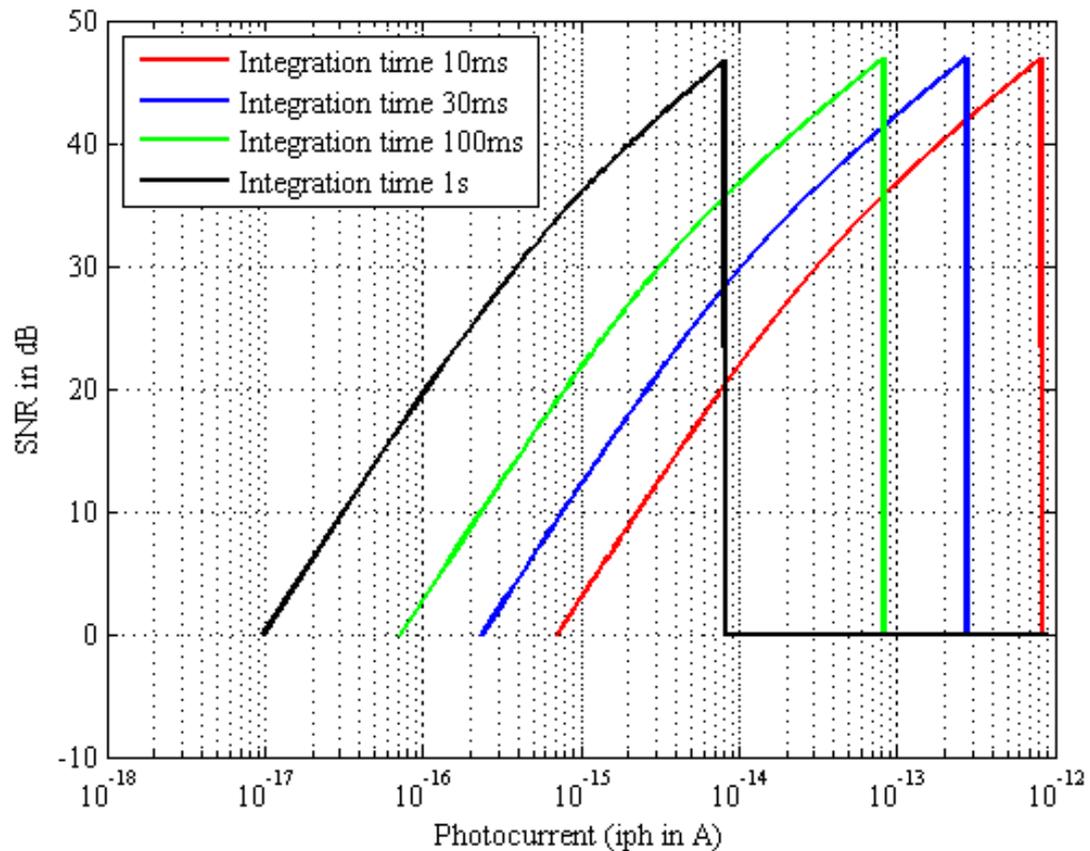
Micro is  $10^{-6}$

So .14 femto amps is  $6.25 \times 10^{18} \times 10^{-15} \times .14$  electrons per second  
 $= (.14 \times 6.25) \times 10^3$  e-/sec

So for a sensor like this, in 10 ms, you would have  $0.010 \times 10^3$  e which is about 10 electrons of dark current.

# Complete Sensor Model

- SNR vs. photocurrent ( $A = 1$ )



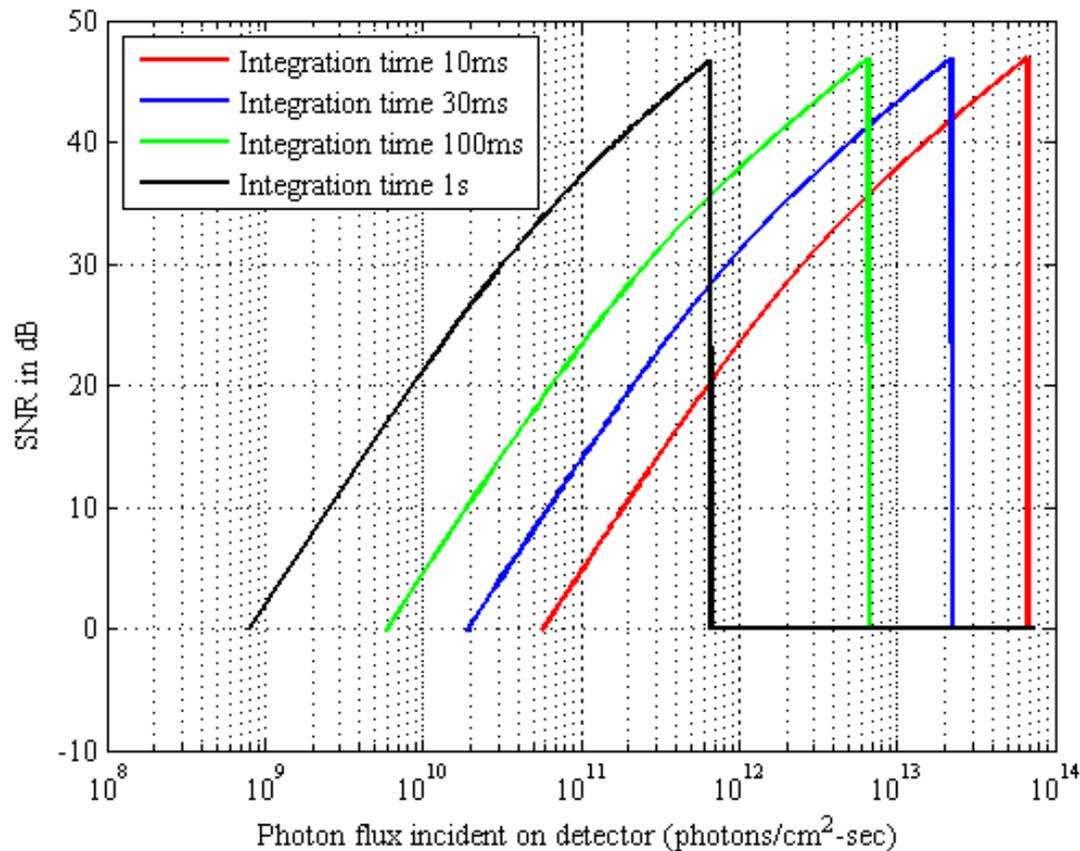
$$\sigma_{read} = 44 \text{ electrons}$$

$$\text{Peak SNR} = 47\text{dB}$$

$$\text{DR} = 60\text{dB}$$

# Complete Sensor Model

- SNR vs. photon flux ( $A = 1$ )



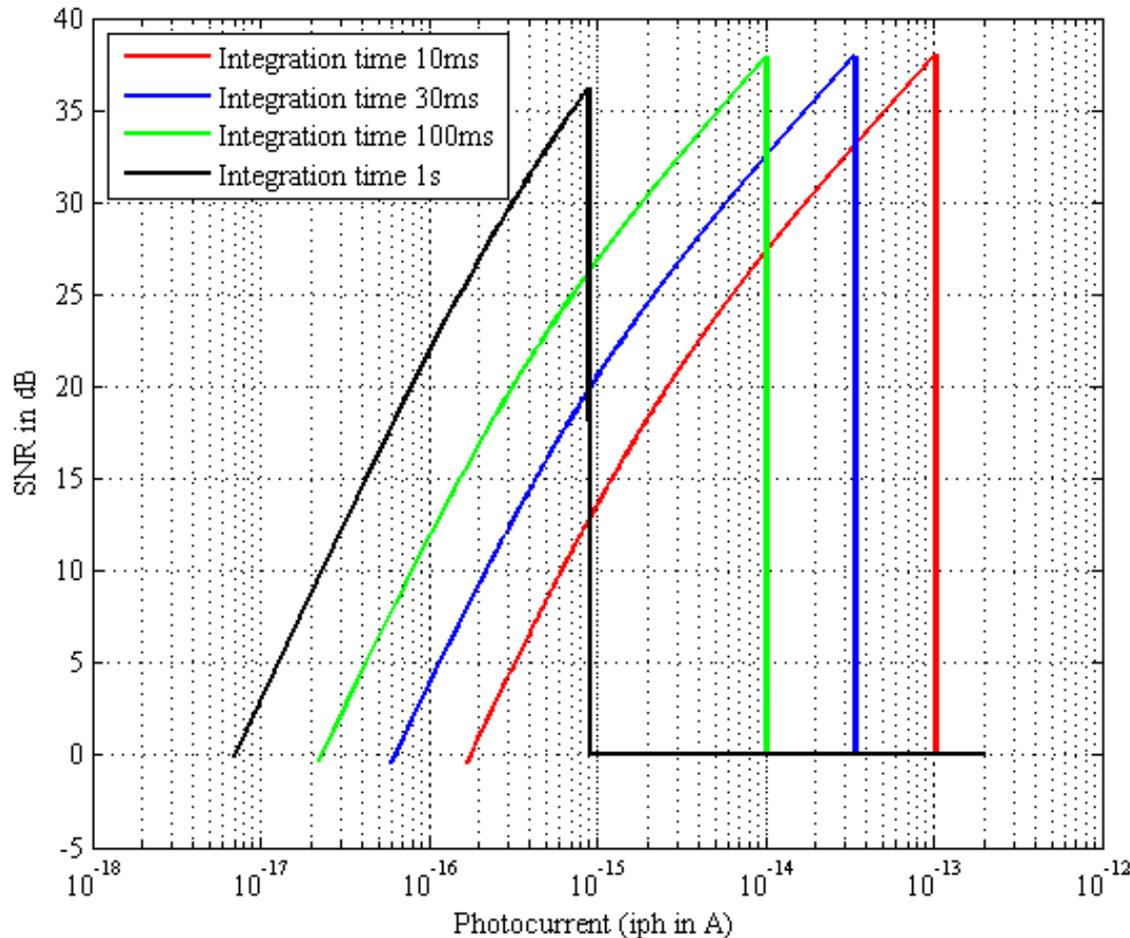
$\sigma_{read} = 44$  electrons

Peak SNR = 47dB

DR = 60dB

# Complete Sensor Model

- SNR vs. photocurrent ( $A = 8$ )



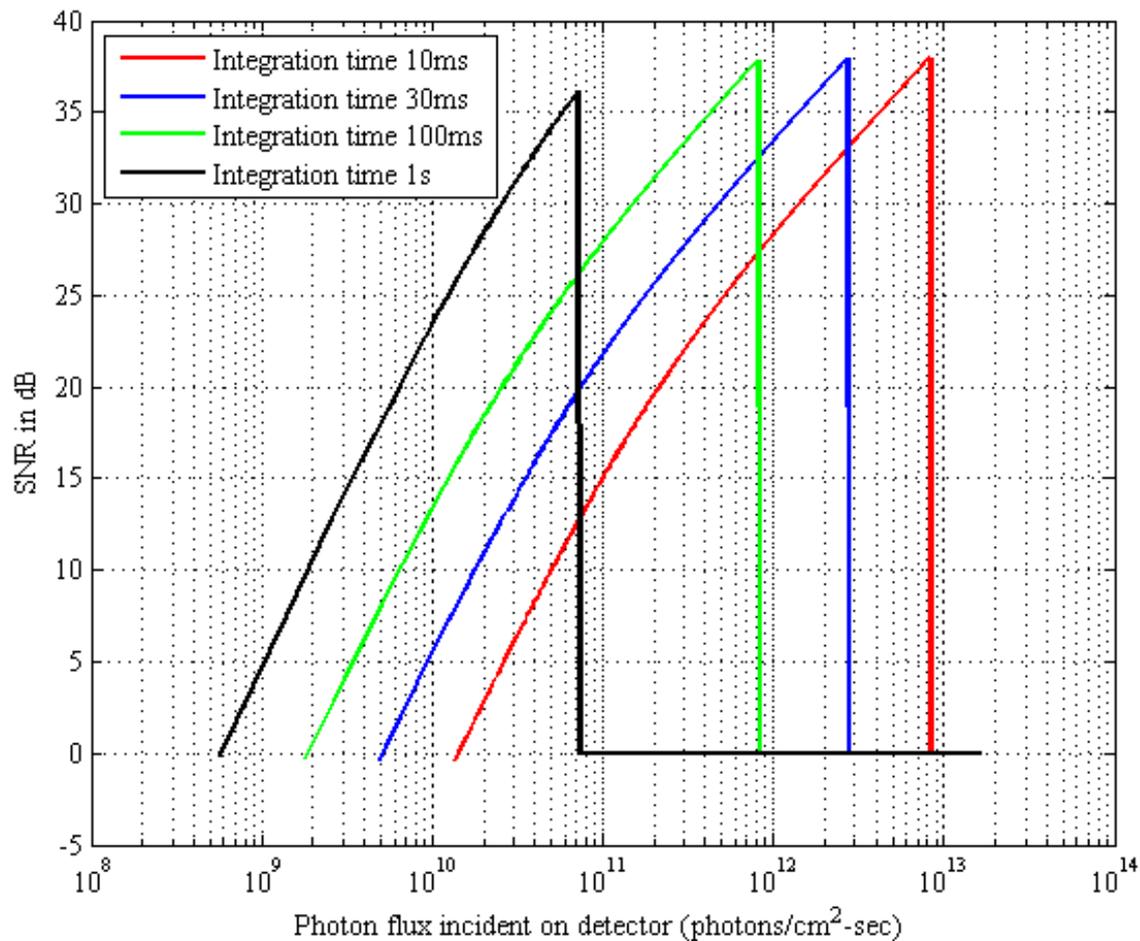
$\sigma_{read} = 10$  electrons

Peak SNR = 38dB

DR = 56dB ( $t_{int} < 100ms$ )

# Sensor Noise Model

## ■ SNR vs. photon flux ( $A = 8$ )



$$\sigma_{read} = 10 \text{ electrons}$$

$$\text{Peak SNR} = 38\text{dB}$$

$$\text{DR} = 56\text{dB} (t_{int} < 100\text{ms})$$